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THIRD ANNUAL REPORT - FISCAL YEAR 1964
Volume II - Analytical Study

November 1965

AFSC PROGRAM STRUCTURE NO. 750G PROJECT NO. 3059, TASK NO. 305906

(PREPARED UNDER CONTRACT AF 04 (611)-9067 by NORTHROP CAROLINA, INC. Asheville, N.C.)



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ROCKET PROPULSION LABORATORY
AIR FORCE SYSTEMS COMMAND
Edwards Air Force Base, California

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(Unclassified Title)

DUAL-CHAMBER

CONTROLLABLE SOLID PROPELLANT ROCKET MOTOR (U)

THIRD ANNUAL REPORT - FISCAL YEAR 1964

Volume II - Analytical Study

Prepared under Contract AF 04(611)-9067

by

Northrop Carolina, Inc., Asheville, North Carolina A Subsidiary of Northrop Corporation

November 1965

APPROVED BY:

B. L. Vohnson
Program Manager

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FOREWORD

This annual report for the continued development of a dual-chamber controllable solid propellant rocket motor (DCCSR) describes the progress during the third year of this program, which is sponsored by the Air Force Rocket Propulsion Laboratory, Edwards Air Force Base, California. The research and development efforts of the program are being performed by Northrop Carolina, Inc., a Subsidiary of Northrop Corporation, Asheville, North Carolina, under Air Force Contract AF 04(611)-9067. This report is presented in two volumes: Volume I - Research and Development Efforts, and Volume II - Analytical Study. This volume (Volume II) presents the results of a study to determine the effect of motor performance parameters and propellant characteristics on the mass fraction, burnout velocity, and motor envelope of the dual-chamber controllable solid propellant rocket motor.

SCANIE .

NOTICE

Northrop Carolina, Inc., has been assigned a patent application by the U. S. Patent Office to cover the Controllable Solid Propellant Rocket Motor invention disclosed in this publication, and the Commissioner of Patents has issued a secrecy order thereon. This secrecy order requires that those who receive a disclosure of the subject matter be informed of the existence of the secrecy order and of the penalties for the violation thereof.

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SECTION I - INTRODUCTION

1. GENERAL

Northrop Carolina, Inc., a subsidiary of Northrop Corporation, has been developing a dual-chamber controllable solid propellant rocket motor (DCCSR) under sponsorship of the Air Force Systems Command, Rocket Propulsion Laboratory, Edwards Air Force Base, California. This program, now in its third year, is funded under Contract AF 04(611)-9067. The progress of the program has been reported in quarterly and annual technical documentary reports (References 1 through 13). This volume presents the results of a separate parametric study conducted as part of the third year's effort.

The DCCSR concept is fully described and illustrated in Volume I. However, a brief description is given here to provide a better understanding of the information and data presented in this volume. The concept utilizes two propellant chambers separated by a throttle valve. The forward chamber contains a cool-burning fuel-rich propellant; the aft, an oxidizer-rich propellant. The fact that the forward-chamber combustion products are relatively cool burning (2800°F) permits state-of-the-art materials to be used on the aft chamber, where high-temperature combustion takes place. A multiple pyrogen ignition system is included as a part of the forward chamber. (Confidential)

Thrust is initiated by igniting the forward propellant with a single pyrogen. The relatively cool combustion products from the forward chamber are throttled through the control valve into the aft chamber where additional thermochemical reaction occurs, resulting in more energy release. The aft propellant will not burn without the heat supplied by the forward propellant. Throttleability is achieved by varying the forward-chamber pressure (and burning rate) by varying the position of the valve. The aft propellant actively supports combustion when the combustion gases from the forward propellant pass over it. (Confidential)

Thrust can be terminated at any time during the burning period by suddenly increasing the valve flow area, which produces a rarefaction wave that extinguishes combustion of the forward propellant. Since the aft propellant will not sustain combustion except at high chamber pressures and/or temperatures above 300°C without an external heat source, it too is extinguished. The on-off cycle operation can be repeated on command by reigniting the forward propellant using another pyrogen igniter of the multiple ignition system for each restart. (Confidential)

2. PURPOSE OF STUDY

This study was conducted in order to establish trends and optimum conditions of mass fraction, boost velocity, and motor envelope with variations in motor performance parameters and propellant characteristics for the dual-chamber controllable solid propellant rocket motor concept. It should be noted that the results presented herein do not necessarily represent optimum designs; rather, off-optimum as well as optimum conditions have been examined.

3. SCOPE

Five independent variables (motor performance parameters and propellant characteristics) were selected for this study: (1) total impulse, (2) minimum thrust, (3) thrust throttling range, (4) number of on-off cycles available, and (5) motor specific impulse. The first four variables define the capability of a throttleable stop-restart motor, and each directly affects mass fraction, boost velocity, and motor envelope. The fifth variable, which is a function of propellant composition, directly affects motor size and boost velocity.

The range of total impulse, minimum thrust, and thrust throttling range values included in this study are presented in Table I. Minimum thrust was varied from 1/500 to 1/20 of total impulse, that is, for maximum burn times of 20 to 500 sec. The thrust throttling ranges considered were 1 to 1, 5 to 1, and 20 to 1, and the number of on-off cycles used was 1, 10, 20, and 40. Vacuum specific impulse, at an expansion ratio of 20 to 1, was varied from 265 to 280 to 300 lb-sec/lb. It was felt that these ranges of independent variables would encompass those required in most applications of a DCCSR. (Confidential)

The analysis was divided into two phases. In Phase I, the independent variables listed above were investigated separately, with propellant properties and structural materials fixed. In Phase II, case

TABLE I - TOTAL IMPULSE AND THRUST RANGES
FOR PARAMETRIC ANALYSIS

Total Impulse	Minimum Thrust	Max	imum Thrust (lb	$P_{\mathbf{f}}$)
(lb _f -sec)	(1b _f)	Case 1	Case 2	Case 3
10,000	20	20	100	400
10,000	50	50	250	1,000
10,000	100	100	500	2, 000
10,000	500	500	2, 500	10,000
100,000	200	200	1,000	4,000
100,000	500	500	2, 500	10,000
100,000	1,000	1,000	5,000	20,000
100,000	5,000	5,000	25,000	100, 000
500,000	1,000	1, 000	5,000	20, 000
500,000	2, 000	2, 000	10,000	40,000
500,000	5,000	5, 000	25,000	100,000
500,000	25, 000	25, 000	125, 000	500,000
1,000,000	2, 000	2, 000	19,000	40,000
1,000,000	4,000	4,000	20,000	80,000
1,000,000	10,000	10,000	50,000	200,000
1,000,000	50,000	50,000	250,000	1, 000, 000

(Confidential)

material, propellant mixture ratio, burning-rate constants, and burning-rate pressure exponents were varied as follows:

- 1. The effect of three case materials (steel, titanium and fiberglass) was evaluated for (1) the four thrust levels in the 100,000-lb-sec motor, (2) the other impulse levels at a minimum thrust corresponding to 200-sec operating time, and (3) for throttling ratios of 1, 5, and 20.
- 2. The effect of aft-to-forward-chamber propellant mixture ratios (2 to 1, 3 to 1, and 4 to 1) was investigated over the total impulse and minimum thrust range at a constant throttling ratio of 5 to 1.
- 3. The effect of burning-rate constants was investigated for the four thrust levels in the 100,000-lb-sec motor at a throttling ratio of 5 to 1.
- 4. The effect of propellant burning-rate (pressure) exponent was evaluated at throttling ratios of 1 to 1, 5 to 1, and 20 to 1 at a minimum thrust of 500 lb in the 100,000-lb-sec motor. The burning-rate exponents evaluated were:

 (1) for the forward chamber, 0.6, 0.8, and 0.9; (2) for the aft chamber, 0.8, 1.0, and 1.1.

 (Confidential)

The range of variables and constants used in this study are listed in detail in Section II, paragraph 1.

4. METHOD OF COMPUTATION

This study was carried out by means of Northrop Carolina's IBM 1620 Data Processing System and an IBM 1622 Card Read Punch, which assured accurate and rapid processing of the required data. The data processing system's limited storage capacity (20,000 digits) necessitated the processing of data through four separate computer subroutines. These subroutines, prepared by Northrop Carolina, consisted of (1) a steady-state internal ballistics subroutine, (2) a grain configuration subroutine, and (3) two weight subroutines. The information flow through these subroutines is shown in Figure 1. A detailed description of the subroutines and the overall computer program is presented in Section II.

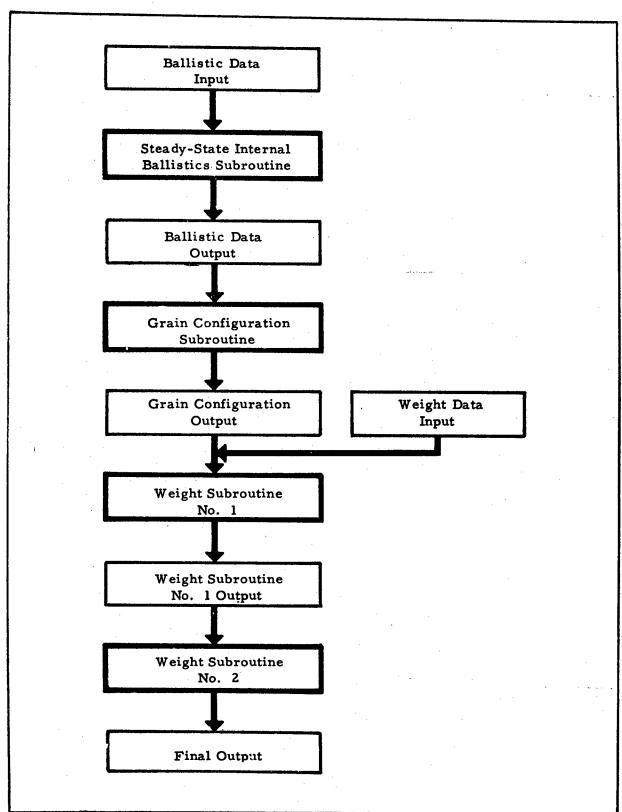


Figure 1 - Computer Program Diagram, Showing Information Flow through Subroutines

SECTION II - TECHNICAL APPROACH

PARAMETER SELECTION

a. General

As mentioned in Section I, this parametric study was conducted in two phases. The effect of the major ballistic parameters was investigated in Phase I; the remaining, less significant parameters in Phase II. As a result, more computer runs were required for Phase I than for Phase II.

Table II summarizes the parameters investigated in each phase, showing which were varied and which held constant. Note that, as shown in Table II, Phase II was subdivided into Phases IIa through IId, depending on the parameters that were held constant, as follows:

Phase	<u>Variable</u>
II a	Case material
II b	Burning rate
II c	Propellant burning rate exponent
II d	O/F ratio, 0 (theta)

The values and ranges of the parameters investigated in each phase are listed in paragraphs b and c, below, respectively.

b. Phase I Parameters

The values of the constants used in Phase I are listed below.

Constant	Value
Case material	Steel
O/F ratio, θ	3.0
Forward propellant density (1bm/in. 3)	0.053
Aft propellant density (lbm/in.3)	0.070

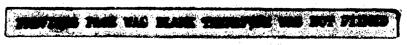


TABLE II - PARAMETERS INVESTIGATED IN EACH PHASE*

	Phase				
Parameter —	I	II a	-II-b	II c	II d
Total impulse, vacuum (lb _f -sec)	v	v	С	С	v
Specific impulse, vacuum (lbsec/lb.)	v	C.	С	С	С
Minimum thrust (lb _f)	v	v	v	С	v
Thrust ratio, maximum/minimum	v	v	С	v	С
Starts	v	С	С	С	С
Case material	С	v	С	С	С
Aft propellant rate constant (in. /sec)	С	С	v	С	C
Forward propellant rate constant (in./sec)	С	С	v	С	С
Aft propellant burning-rate exponent	С	С	С	v	С
Forward propellant burning-rate exponent	С	С	С	v	С
O/F ratio, θ	С	С	С	С	v
Aft propellant density (lbm/in.3)	C	С	С	С	С
Forward propellant density (lbm/in. 3)	С	С	С	С	С
Aft propellant flame temperature (°F)	С	C	С	С	С
Forward propellant flame temperature (°F)	C	С	С	С	С
Aft chamber C _d (sec ⁻¹)	С	С	С	С	С
Forward chamber C _d (sec ⁻¹)	С	С	С	С	С
Minimum aft chamber pressure (psia)	С	С	C	С	С
Minimum forward chamber pressure (psia)	С	С	С	С	С
Expansion ratio	С	ć	С	С	С

^{*}C and V denote constant and variable, respectively.

(Confidential)

Constant	Value
Forward propellant exponent, n	0.80
Aft propellant exponent, n	1.00
Forward propellant rate constant (in. /sec)	0.0008
Aft propellant rate constant (in. /sec)	0.0004
Forward propellant flame temperature (°F)	2700
Aft propellant flame temperature (°F)	5500
C _d , forward chamber (sec ⁻¹)	0.00765
C _d , aft chamber (sec ⁻¹)	0.00643
Minimum forward-chamber pressure (psia)	100.0
Minimum aft-chamber pressure (psia)	50.0
Expansion ratio	20. 0

(Confidential)
The range of the variables used for Phase I are as
follows:

Variable	Range
Total impulse (lb _f -sec)	10 ⁴ to 10 ⁶
Maximum/minimum thrust ratio	1, 5, 3
Minimum thrust (lb _f)	26 to 1,000
Specific impulse, vacuum (lb _f -sec/l)	26 280, 300
Starts	1, 10, 20
(Co	onfidential)

c. Phase II Parameters

The less significant parameters (case material, burn rate, pressure exponent, and theta) were varied in Phase II. The range of these variables and the values of the constants used in each portion of Phase II are listed below.

Phase II a

Constants - Same as Phase I, except for the following:

Case Material	Listed below
Specific impulse, vacuum (lb _f -sec/lb _m)	280
Starts	20
Variables	
Maximum/minimum thrus	t ratio 1, 5, 20
Case material	Steel, Fiberglass, Titanium
Total impulse (lb _f -sec)	10 ⁴ to 10 ⁶
Minimum thrust (1b _f)	50 to 5000
Phase II b	
Constants - Same as Phase I, e	except for the following:
Burn rate constants	Listed below
Specific impulse, vacuum (lb _f -sec/lb _m)	280
Starts	20
Maximum/minimum thru	st ratio 5
Total impulse (lb _f -sec)	10 ⁶
Variables	
Aft propellant burn rate constant (in /sec)	0.0001 to 0.0010
Forward propellant burn	rate
constant (in. /sec)	0.0002 to 0.0032
Minimum thrust	200 to 500
Phase II c	
Constants - Same as Phase I,	except for the following:
Burn rate exponents	Listed below
Specific impulse, vacuur (lb _f -sec/lb _m)	n 280
Starts	20

	Total impulse (lb _f -sec)	10 ⁵		
	Minimum thrust (lb _f)	500		
Varia	bles			
-	Aft propellant exponent	0.8 to 1.1		
	Forward propellant exponent	0.6 to 0.9		
	Maximum/minimum thrust ratio	1, 5, 20		
Phase II d				
Constants - Same as Phase I, except for the following:				
	Theta	Listed below		
	Specific impulse, vacuum (lb _f -sec/lb _m)	280		
	Starts	20		
	Maximum/minimum thrust ratio	5		
Vari	ables			
	Theta	2. 0 to 4. 0		
	Total impulse (lb _f -sec)	10 ⁴ to 10 ⁶		
	Minimum thrust (lb _f)	50 to 5000		

d. Output Parameters

The parameters listed in <u>c</u> and <u>d</u>, above, were used as inputs to the computer program. The chief dependent variables calculated (computer outputs) were:

- 1. Mass fraction
- 2. Delta velocity, ideal (fps)
- 3. Total motor length (in.)
- 4. Total motor diameter (in.)
- 5. Grain design

For some computer runs, other values were calculated as data checks; however, they are not presented here.

(Confidential)

2. INTERNAL BALLISTICS SUBROUTINE

The internal ballistics subroutine was prepared to calculate ballistic design and performance parameters for the DCCSR motor under steady-state operating conditions. This subroutine contains two principal options which permit the program to be used to design aft-chamber parameters and calculate performance for test motors (Option I) or to design motors to meet specified thrust and total impulse requirements (Option II). The general subroutine logic is shown in the diagram in Figure 2; the actual IBM 1620 computer subroutine listing is given in Appendix A.

The equations employed in this subroutine are conventional ballistic relationships which have been modified for dual-chamber motors, as outlined previously (Reference 1). The forward chamber, with choked flow at the valve, operates as a conventional rocket motor. Aft-chamber parameters are calculated as a function of the ratio of aft-to-forward mass flow, θ , which under steady-state conditions is defined as:

$$\theta = \frac{(\rho SaP^{n})_{aft}}{(\rho SaP^{n})_{fwd}}, \qquad (1)$$

where

p = propellant density,

S = burning area,

a = burn-rate constant,

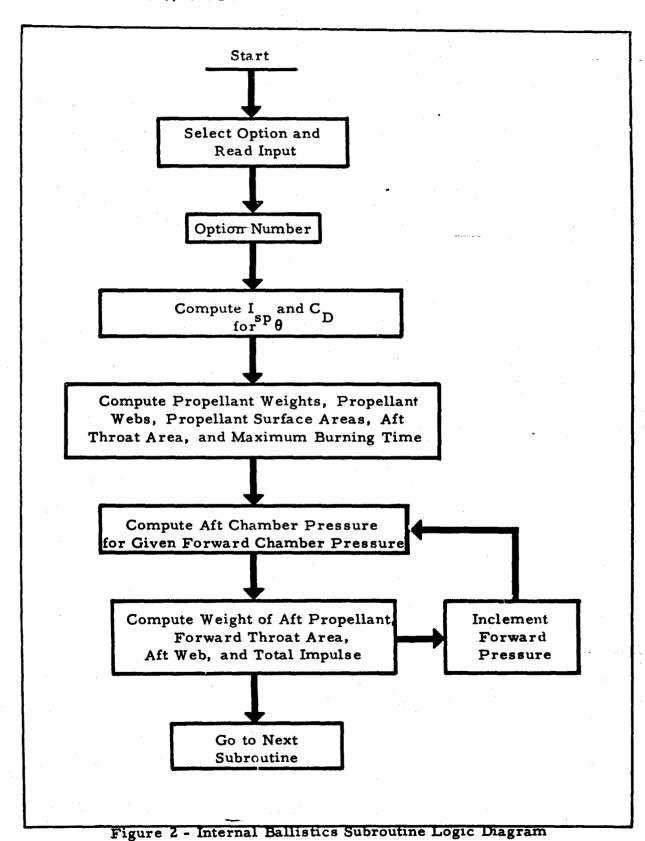
P = operating pressure, and

n = pressure exponent

The aft-chamber surface area was calculated by rearranging this equation, as follows:

$$S_{aft} = \theta \frac{\left(\rho SaP_{min}^{n}\right)_{fwd}}{\left(\rho aP_{min}^{n}\right)_{aft}}.$$
 (2)

^{*} Also referred to as burning-rate exponent herein.



The over-all mass flow balance for the motor is

$$\dot{M}_{fwd} + \dot{M}_{aft} = \dot{M}_{tot} = (C_d P A_t)_{aft}, \qquad (3)$$

where

C_d = discharge coefficient at aft nozzle, and A₊ = aft nozzle throat area.

Hence,

$$(\rho SaP^{n})_{fwd} + (\rho SaP^{n})_{aft} = (C_{d} P A_{t})_{aft}, \qquad (4)$$

or

$$1 + \theta = \frac{(C_d P A_t)_{aft}}{(\rho SaP^n)_{fwd}}.$$
 (5)

The aft-chamber throat area was calculated by rearranging Equation 5; that is,

$$A_{t_{aft}} = (1 + \theta) \frac{(\rho SaP_{min}^{n})_{fwd}}{(C_{d}P_{min})_{aft}}.$$
 (6)

Aft-chamber pressure was calculated as a function of forward-chamber pressure from Equation 4 by an iterative procedure. Initially, an estimate of aft-chamber pressure was substituted into the left side of Equation 4, and the aft-chamber pressure on the right side was calculated from

$$P_{aft} = \frac{(\rho SaP^n)_{fwd} + (\rho SaP^n_{est})_{aft}}{(C_d A_t)_{aft}}.$$

Phis conculated pressure was then compared with the estimated pressure. If the two did not agree within 0.5 percent, another estimated pressure was obtained by

$$P_{est_n} = 2P_{calc_{(n-1)}} - P_{est_{(n-1)}}$$

and the procedure repeated until convergence was achieved.

When the calculated pressure agreed with the estimated pressure within 0.5 percent, θ was calculated from Equation 1 and compared with the estimated θ from which C_{d} was obtained. If these did not

agree within 0.5 percent, a new θ was estimated and aft-chamber pressure was calculated using a new $C_{\mbox{d}}$. This procedure was

repeated until convergence was achieved. Thrust was then calculated from the product of specific impulse at the final θ value and mass flow rate.

3. GRAIN CONFIGURATION SUBROUTINE

The grain configuration subroutine was prepared for determining the most suitable grain configurations for the DCCSR forward and aft chambers. The subroutine calculated the diameter, length, port area, and volumetric loading of the grains, but did not calculate the detailed grain design. The four basic grain types employed, in order of increasing mass flow requirements, were end burning, cylindrically (center) perforated, star; and wagon-wheel designs. These configurations were selected for either a cylindrical or spherical forward chamber and for a cylindrical aft chamber, either in tandem or around the outside of the forward chamber. The required input for this subroutine, supplied by the steady-state internal ballistics subroutine, consisted of forward- and aft-grain burning surface areas and web thicknesses,, and aft-chamber throat area. The subroutine output provided the dimensions necessary for case and insulation design. The subroutine logic is shown in the diagram in Figure 3, while the actual computer subroutine listing is given in Appendix A.

The equations employed in this subroutine are general geometry equations that relate diameters to areas and volumes of both cylinders and spheres; the actual equations used are shown in the program listing for this subroutine in Appendix A. The subroutine initially established the forward-grain configuration and its dimensions, based on forward-grain surface area and web thickness inputs. First, a cylindrical end-burner design was assumed and the grain diameter calculated from the inputs. If the length-to-diameter ratio of this design was less than 0.5, the cylindrical end-burner design was rejected and a spherical end burner assumed. The program thus proceeded from designs with high web fractions to those with low web fractions until a design with a reasonable length-to-diameter ratio was obtained. The program then printed out the type of configuration, grain outside diameter, length, and volumetric loading. For cylindrical

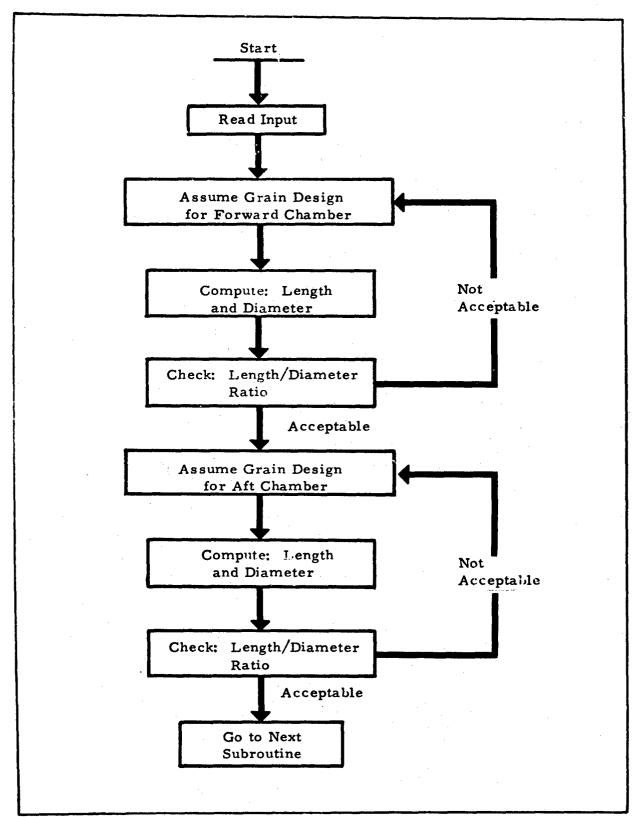


Figure 3 - Grain Configuration Subroutine Logic Diagram

center perforated and star designs, the program would, when feasible, give an alternate spherical forward-chamber design.

After the forward grain configuration was selected, the subroutine had the option of proceeding to another case or establishing the aft-grain configuration. The aft-grain program was similar to the forward one in that designs with increasing web-to-diameter ratios were considered until a design giving a reasonable length-to-diameter ratio was achieved. An attempt was made to design an aft grain with an outside diameter equal to that of the forward. If this diameter proved to be unsatisfactory, larger or smaller diameters were used. For forward-chamber designs with high length-to-diameter ratios, the aft-chamber subroutine considered the feasibility of placing the aft chamber around the forward chamber, rather than in tandem, to reduce the over-all length-to-diameter ratio for the dual-chamber system. Figure 4 shows some typical configurations for chambers in tandem and with one chamber inside the other.

The subroutine assumed that the surface-time history of the selected grain configuration was neutral. This assumption is true for end-burning grains and can be made approximately so for the star and wagon-wheel configurations. Although most of the cylindrically perforated designs would not be neutral, this can be corrected in a detailed design by using slotted-tube configurations of approximately the same diameter and length.

4. WEIGHT SUBROUTINES

a. General

As mentioned in Section I, the weight calculation subroutine was divided into two parts (A and B) to facilitate computation in Northrop Carolina's IBM 1620 computer. The subroutine
calculated the weight and dimensions of the forward and aft
motor case, end closures, insulation, nozzle, igniters, and
the control valve. The weights and dimensions were selectively
calculated, depending on geometrical constraints such as the
forward- and aft-chamber grain configurations and the
materials used for each individual component. The generalized
flow diagrams for the two weight subroutines are shown in
Figures 5 and 6, respectively. The subroutine program listings
are given in Appendix A.

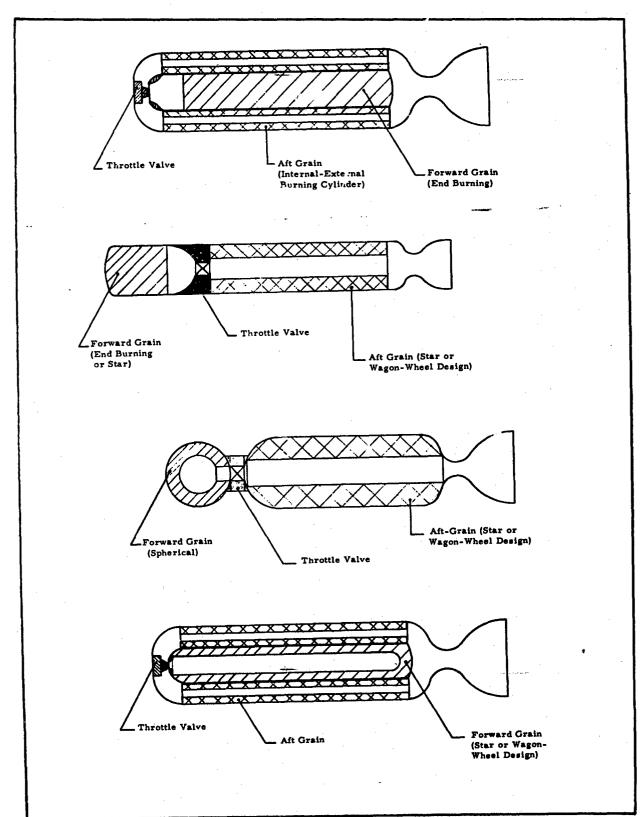


Figure 4 - Typical Configurations Considered in Grain Configuration Subroutine

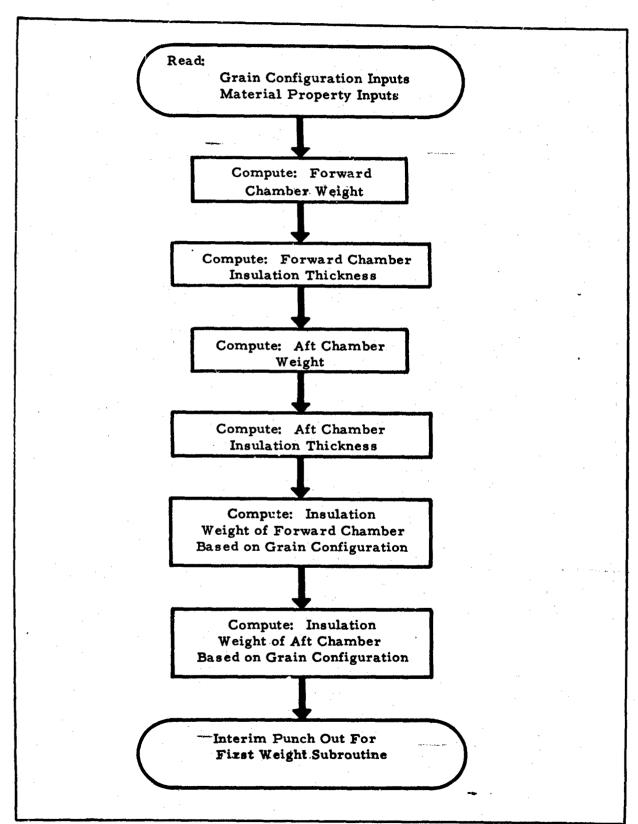


Figure 5 - Weight Subroutine A Logic Diagram

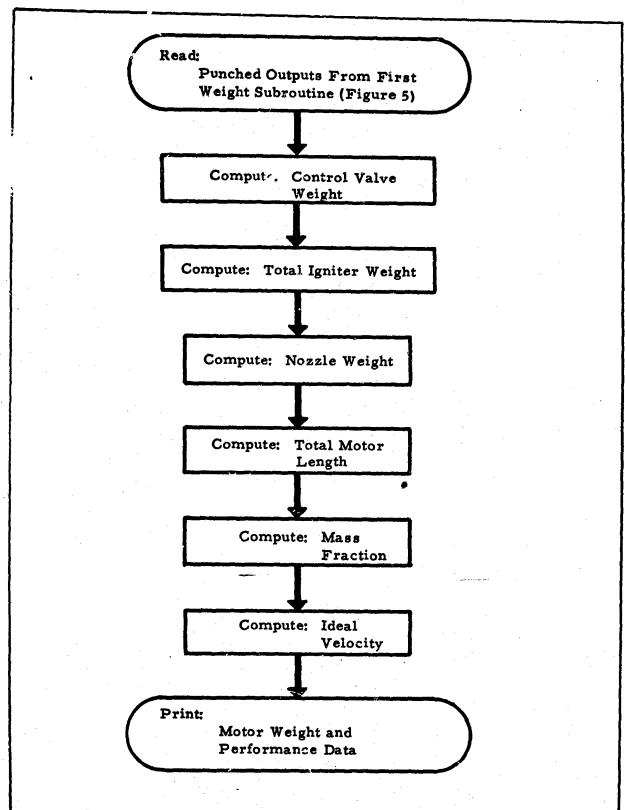


Figure 6 - Weight Subroutine B Logic Diagram

b. Chamber Weights

Chamber weights were calculated by multiplying the chamber surface area by the thickness of the particular section (based on the operating pressure times material density. The weight of the head closures was calculated from

$$W_{\text{ellipsoid}} = t_{\text{ell}} \rho \pi \left[R^2 + \left(\frac{b^2}{2e} \right) \left(\ln \frac{1+e}{1-e} \right) \right], \quad (7)$$

where

$$t_{ell} = \frac{PRSF}{\sqrt{2\sigma}}$$
, and

$$e = \frac{\sqrt{R^3 - b^3}}{R^3}.$$

The cylindical chamber weight was calculated from

$$W_{cyl} = t_{cyl} \rho 2\pi R, \qquad (8)$$

where

$$t_{cyl} = \frac{PRSF}{\sigma}$$
.

The symbols used in Equations 7 and 8 are defined below:

Wellipsoid = total head closure weight (1bm)

W = total cylindrical chamber weight (lbm)

tell = thickness of h. ad closure (in.)

t = thickness of cylindrical chamber (in.)

 ρ = material density (lb_m/in.³)

R = major case radius (in.)

b = minor ellipse radius (in.)

e = ellipse eccentricity ratio

= material yield strength (lb_s/in. 2)

SF = safety factor

P = operating pressure (psia)

c. Valve and Power Supply Weights

Valve and power supply weights were determined by a parametric derivation of each component's contribution to total control weight as a function of valve size. The weight equations used for each component are listed below:

Component	Weight Equation	
Intermediate plate	$W = 0.00939 D_t^3 (\Delta I)$	5) ³
Intermediate plate insulation	$W = 0.0025 D_t^2 t_b$	_
Housing insulation	$W = 0.0225 D_{t}^{2}$ $W = 0.00233 D_{t}^{2} t_{b}$ $W = 0.02097 D_{t}^{2}$	$(t_b < 9 \text{ sec})$ $(t_b \ge 9 \text{ sec})$ $(t_b < 9 \text{ sec})$
Tube insulation	$W = 0.0053 D_t^2 t_b$ $W = 0.0476 D_t^2$	$(t_b \ge 9 \text{ sec})$ $(t_b < 9 \text{ sec})$
Piston insulation	$W = 0.00162 D_{t}^{2} t_{b}$ $W = 0.0146 D_{t}^{2}$	(t _b ≥9 sec) (t _b <9 sec)
Pintle	$W = 0.0282 D_t^3$	$(D_t \ge 1.07$ and
	$W = 0.0302 D_t^2$	$L = f(D_t)$ $(D_t < 1.07)$
Power pack	$W = 0.33 D_t^3$	
Servovalves	$W = 0.59 D_t^3 + 0.9$	
Piston	$W = 0.022 D_t^2 + 0.0$	00676 D _t ³
	- -	$(D_t^{\geq} 2.67)$
	$W = 0.0403 D_t^2$	$(D_{t} < 2.67)$

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4.53	Component	Weight Equation	
	End of piston	W = 0.022 + 0.00	
		•	$(D_{t} \ge 0.68)$
ľ	e e e e e e e e e e e e e e e e e e e	$W = 0.22 D_t^2 + 0.000$	00 294 D _t /P (D _t < 0.68)
	Cylinder	$W = 0.0297 D_t^3$	(D _t ≥ 2.9)
Lè		$W = 0.00792 D_t^{*} + 0.$. 027 D _t *
		•	$(D_t < 2.9)$
	Duct	$W = CD_t^3 = 0.0056$	3 D _t a
		. •	$(D_t \ge 10.7)$
		$W = CD_t^2 = 0.0602$	D _t ² (D _t < 10.7)
	Struts	$W = 0.000301 D_t^3 P$	
r 1	Housing	$W = 0.0966 D_t^a$. •
		$W = 0.0934 D_t^{.2} + 0.$	•
	where		(D _t < 2. 38)
	 $D_{t} = \sqrt{\frac{4 V_{f}}{\pi C}} (input)$	1t),	· · · · · · · · · · · · · · · · · · ·
Π	t _b = burn time,		
п	ΔP = forward-char pressure (magnetic pressure p	mber pressure - aft-cha aximum),	amber
i i	C = constant inp	ıt, and	
	V _f = final free vo	lume of forward chambe	er.

d. Insulation Weights

Insulation weight was determined as a function of exposed insulation area, flame temperature, burning time, and insulation density, by means of the following equation:

$$W_{ins} = A_{ins} \rho t_{ins}$$

where

$$t_{ins} = 0.007 t_b \left(\frac{T_c + 460}{5806} \right)^4 + 0.05,$$

A = exposed insulation surface area (in. 2)

 ρ = insulation density (lb_m/in.³)

th = maximum duration (sec), and

T = chamber flame temperature (°F).

e. Nozzle Weights

Nozzle weight was determined by the following empirically derived equation, which is dependent upon the yield strength of the material used in each component of the nozzle, flame temperature, expansion ratio, throat area, chamber pressure, maximum burn time, and propellant C*:

$$W_{\text{noz}} = \frac{(104 + 9.65^{\epsilon})}{10^{6}} {(A_{t})}^{1.5} P_{c_{\text{max}}} + 1.53 (A_{t})^{0.8}$$

$$+ \left[\frac{0.00268 t_{b} (\frac{C^{*}}{32.2})^{1.7} (P_{c_{\text{max}}})^{0.8} + 0.1}{10^{6}} \right] \times (0.0865) (\epsilon - 4) A_{s},$$

where

€ = expansion ratio,

 $A_t = \text{throat area (in.}^2)$

P_c = maximum chamber pressure (lb_f/in.²)

t_b = maximum burn time (sec), and

C* = propellant characteristic velocity (fps).

f. Subroutine Output Data

Output data from these subroutines was very complete. An attempt was made to summarize all motor characteristics, dimensions, and weights in one tabulation, shown in Table III. Output data are coded by a line heading that increases from 100 to 1800.

rable III - output format of weight subroutin

Total Impulse		Diameter, Forward Chamber		Insulation Density, Forward Chamber		Igniter Mass Fraction	Thermal Conductivity, Forward Propellant	Discharge Coefficient, Aft Chamber	Motor Configuration, Forward Grain				Density of Forward Chamber Material		Cylinder Weight		Motor L/D
Strength/Density, Forward Chamber	Minimum Aft- Chamber Pressure	Diameter, Aft Chamber	Maximum Burn Time	Insulation Density, Aft Chamber	Propellant Burn Rate Constant, Forward Chamber	Ignition Constant	Thermal Conduc- tivity, Aft Propellant	Propellant Density, Forward Chamber	Total Insulation Weight,Aft Chamber		Motor Configuration, Aft Grain		Density of Aft Chamber Material		Duct Weight	Expension Ratio	Ideal Velocity
Strength/Density, Aft Chamber	Maximum Forward- Chamber Pressure	Ellipse Ratio, Forward Chamber	Propellant Weight, Forward Chamber	Maximum Propellant Surface Area, Forward Grain	Propellant Burn Rate Constant, Aft Chamber	Percent of Gas in Ignition Exhaust		Propellant Density, Aft Chamber	Insulation Weight of Cylinder, Aft Chamber	Total Insulation Weight, Forward Chamber	Weight of Aft Chamber	Weight of Aft Chamber	Thickness of Insulation, Forward Chamber	Piston Pintle Housing Weight	Strut Weight	Nozzle Insulation Weight	Mass Fraction
Strength/Density, Nozzle Exit	Maximum Aft- Chamber Pressure	Ellipse Rr.cio, Aft Chamber	Propellant Weight, Aft Chamber	Maximum Propellant Surface Area, Aft Grain	Gas Molecular Weight, Forward Chamber	Number of Igniters		Individual Igniter Weight	Insulation Weight of Aft Closure, Aft Chamber	Insulation Weight of Cylinder, Forward Chamber	Weight of Cylinder, Aft Chamber	Weight of Cylinder, Forward Chamber	Thickness of Cylinder, Forward Chamber	Pieton End Weight	Intermediate Plate Weight	Nozzle Throat Weight	Maximum Motor Length
Strength/Density, Nozzle Throat	Flame Temperature, Forward Chamber	L/D Forward Chamber		Throat Area, Forward Chamber	Gas Molecular Weight, Aft Chamber	Gas Molecular Weight, Igniter	n, Forward Propellant	igniter Propellant Weight	Insulation Weight of Forward Closure, Aft Chamber	Insulation Weight of Aft Closure, Forward Chamber	Weight of Aft Closure, Aft Chamber	Weight of Aft Closure, Forward Chamber	Thickness of Insulation, Aft Chamber	Valve Insulation Weight	Power Pack Weight	Nozzle Structure Weight	Maximum Motor Diameter
Strength/Density, Nowzle Structure	Flame Temperature, Aft Chamber	L/D Ait Chamber	Number of Chambers	Throat Area, Aft Chamber	Flame Temperature of Igniter	Igniter Safety Factor	n, Aft Propellant	Total Igniter Weight	Total Insulation Weight	Insulation Weight of Forward Chamber	Weight of Forward Closure, Aft Chamber	Weight of Forward Closure, Forward Chamber	Thickness of Cylinder, Aft Chamber	Total Valve Weight	Servo Weight, Power Pack Intermediate Plate	Nozzle Weight	Total Motor Weight
100	200	300	400	800	009	700	800	006	1000	1100	1200	1300	1400	1500	0091	1700	1800

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SECTION III - DISCUSSION OF RESULTS

1. GENERAL

The over-all results of the parametric study are presented and discussed in this section. The data from the computer runs have been plotted in semi-logarithmic form to facilitate analysis. The data from these basic plots, which are presented sequentially in Appendix B by phase and variable, have been cross-plotted and presented in this section to highlight the trends observed.

This section is organized by study phase, with the effect of each independent variable discussed separately.

2. PHASE I

a. General

In Phase I, the effect of specific impulse, thrust ratio, number of starts, total impulse, and minimum thrust on mass fraction and delta velocity was studied. The effect of each of these variables is discussed below.

b. Specific Impulse

The effects of specific impulse on mass fraction and delta velocity, for a thrust ratio of 1 and 10 starts, are shown in Figures 7 and 8, respectively. As shown in Figure 7, mass fraction decreases slightly with increasing specific impulse. However, delta velocity increases as specific impulse is increased. Curves for higher thrust ratios and other than 10 starts are similar, but the mass fraction and delta velocity levels differ. (Confidential)

c. Thrust Ratio

In Figures 9 and 10, the effects of thrust ratio (that is, maximum thrust/minimum thrust) on mass fraction and delta velocity are shown, for 10 starts and a specific impulse of 280 lb_f-sec/lb_m. For thrust ratios up to 5, the penalty on

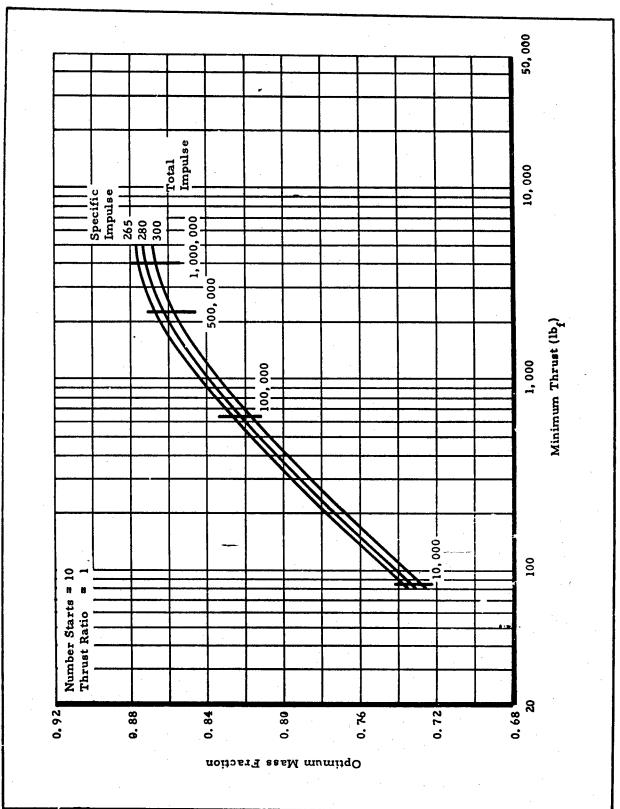


Figure 7 - Effect of Specific Impulse on Mass Fraction

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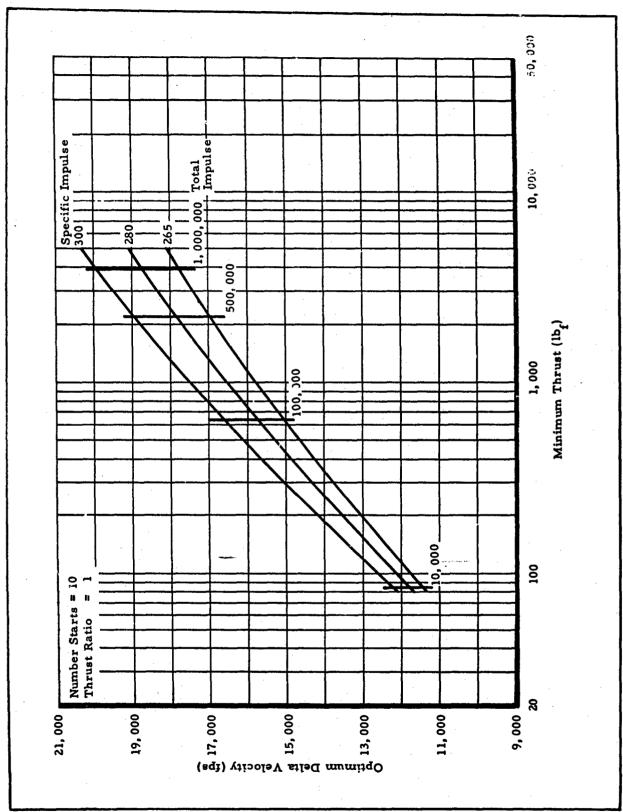


Figure 8 - Effect of Specific Impulse on Delta Velocity

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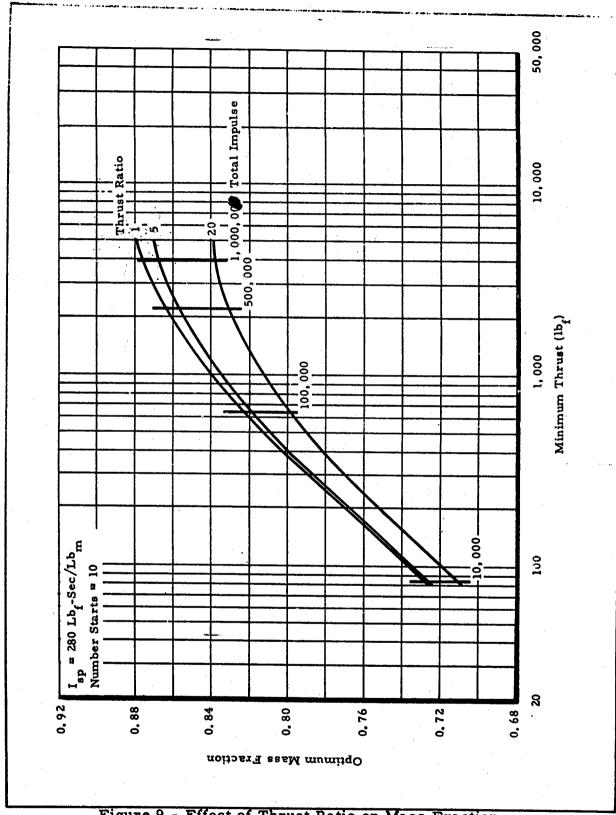


Figure 9 - Effect of Thrust Ratio on Mass Fraction

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Table 1

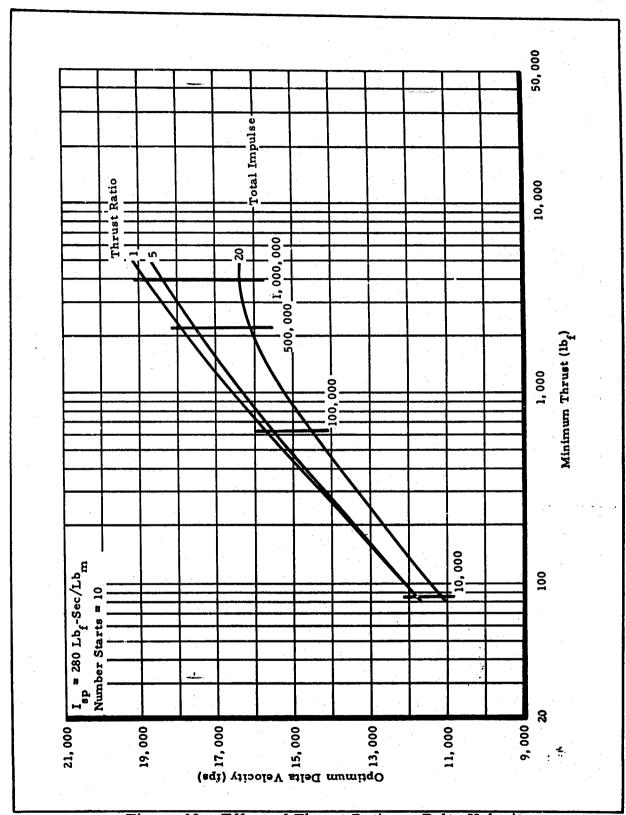


Figure 10 - Effect of Thrust Ratio on Delta Velocity

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mass fraction and delta velocity is small. This penalty becomes more pronounced, however, for a thrust ratio of 20, particularly for the larger motors. For example, the mass fraction is decreased 2.7 percent at a 20-to-1 thrust ratio for a 10,000-lb-sec motor, compared to a decrease of 4.5 percent for a 1,000,000-lb-sec motor. This penalty is due to the effect of the higher chamber pressure, required for the 20-to-1 thrust ratio, non case thickness, resulting in a greater weight penalty in the large-diameter (high total impulse) motors. However, the 20-to-1 throttling range imposes very little penalty over that of a stop-restart motor alone (thrust ratio of 1) at the lower total impulse levels. (Confidential)

d. Number of Starts

The effects of the number of starts, for a restartable motor, on mass fraction and delta velocity are shown in Figures 11 and 12, respectively. The differences represent the weight penalty imposed by the multiple pyrogen units for restart capability. The weight of a valve for termination was included for all motor designs, including the motor with one start. The mass fraction penalty for 20 starts, compared to one start, is 1.8 percent for the 10,000-lb-sec motors, and 1.2 percent for the 1,000,000-lb-sec motors. (Confidential)

e. Total Impulse and Minimum Thrust

The effects of total impulse on mass fraction and delta velocity are shown in Figures 13 and 14, respectively, for motors with thrust ratios of 1, 5, and 20 to 1. The mass fraction for each total impulse level corresponds to that at the optimum minimum thrust level, derived from Figure B-5. Figure 15 is a contour map of mass fraction as a function of total impulse and minimum thrust for a thrust ratio of one. A similar plot for a thrust ratio of 20 is given in Figure 16. The dotted constant mass fraction lines in Figures 15 and 16 are extrapolated values. These plots give the optimum minimum thrust levels corresponding to various total impulse level motors. (Confidential)

Figure 17 shows the effects of minimum thrust and total impulse on motor diameter. The dotted lines connect the values for constant total impulse designs, and the solid lines connect values for motor designs with similar grain configurations.

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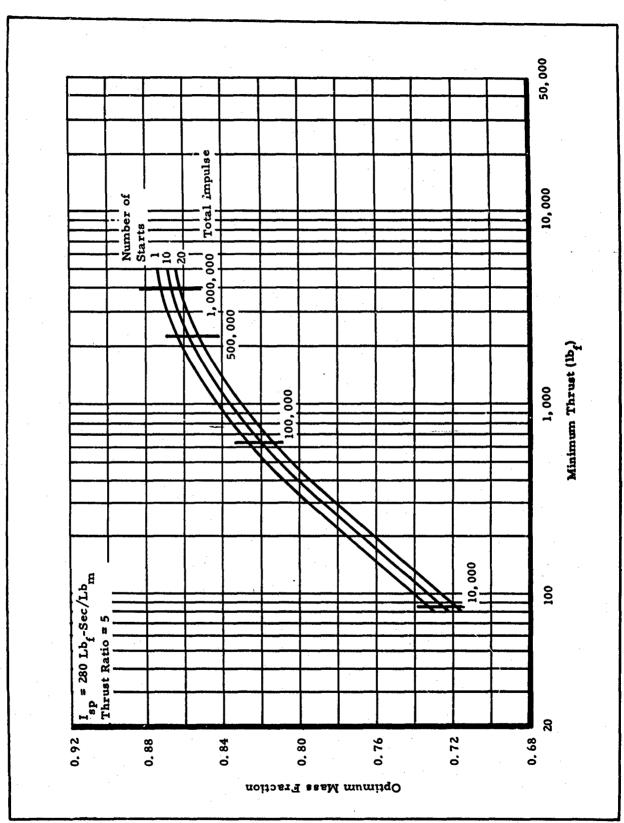


Figure 11 - Effect of Number of Starts on Mass Fraction

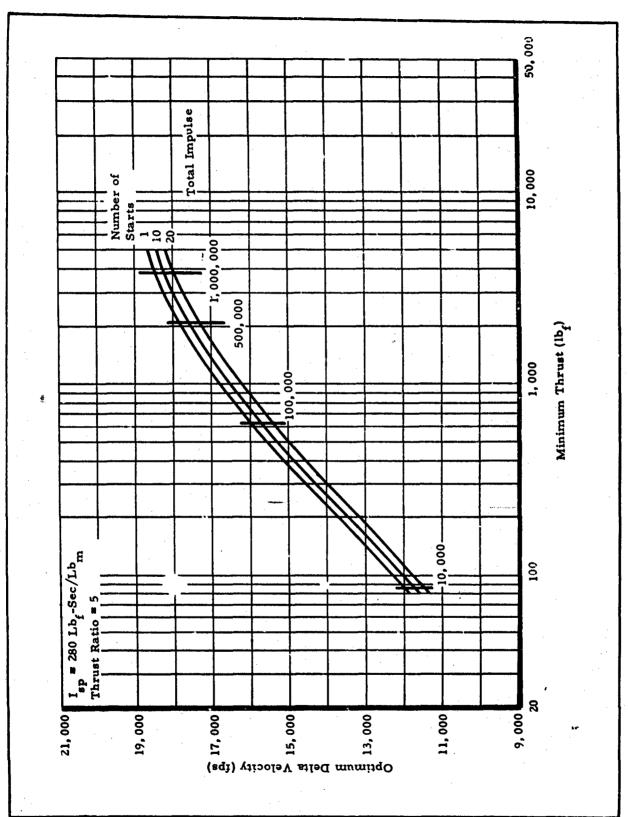


Figure 12 - Effect of Number of Starts on Delta Velocity

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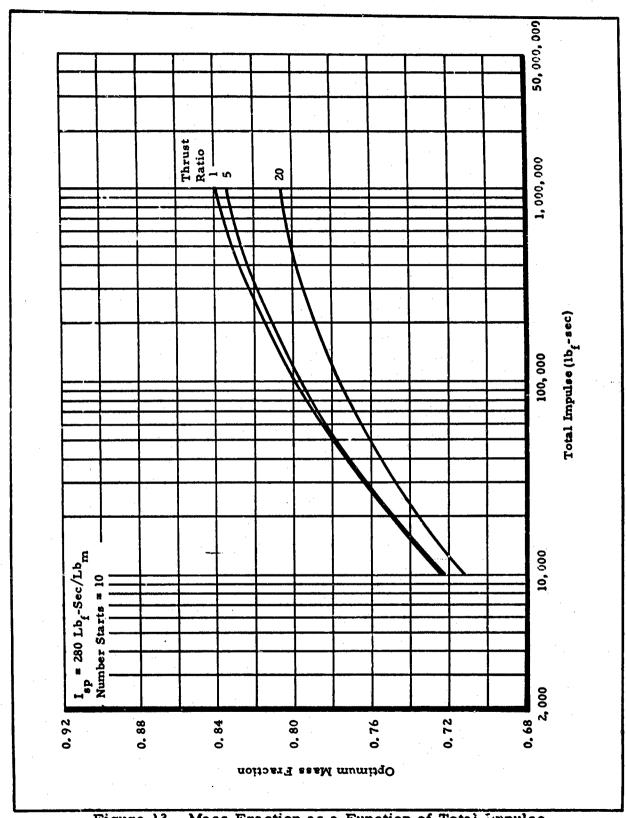


Figure 13 - Mass Fraction as a Function of Total impulse

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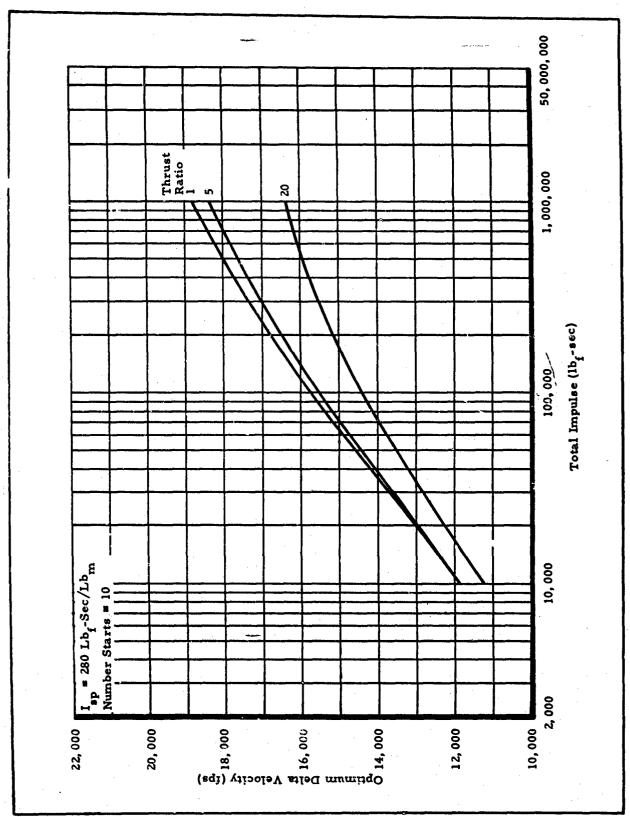


Figure 14 - Delta Velocity as a Function of Total Impulse

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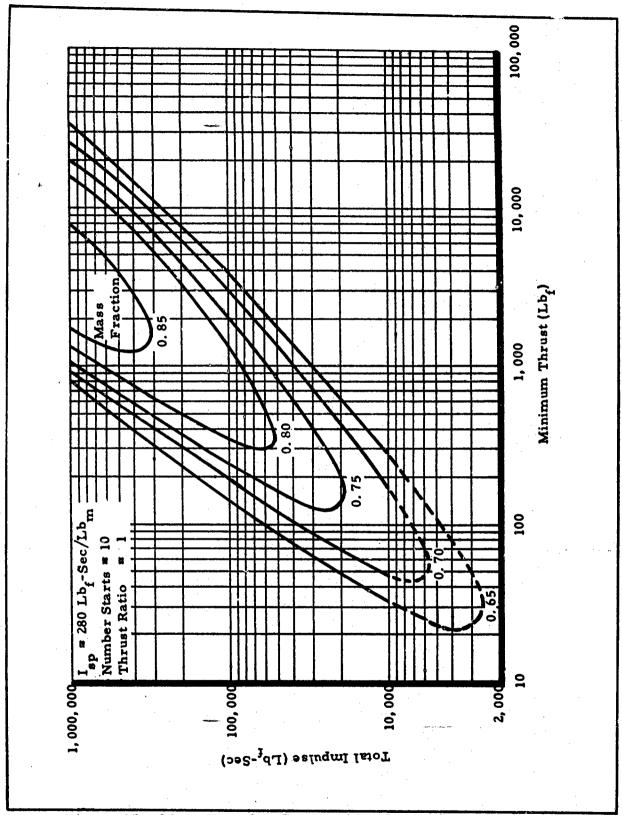


Figure 15 - Mass Fraction Contour Map for a Thrust Ratio of 1

-37-

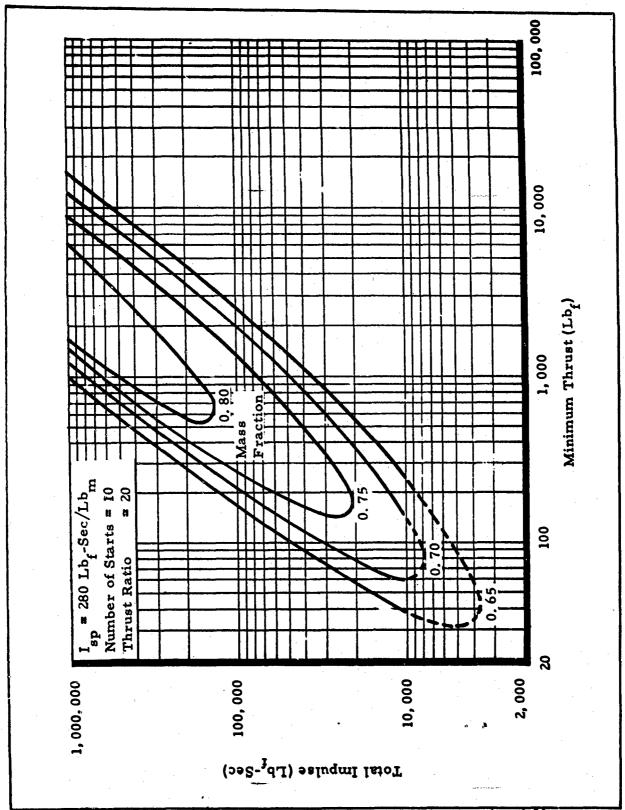


Figure 16 - Mass Fraction Contour Map for a Thrust Ratio of 20

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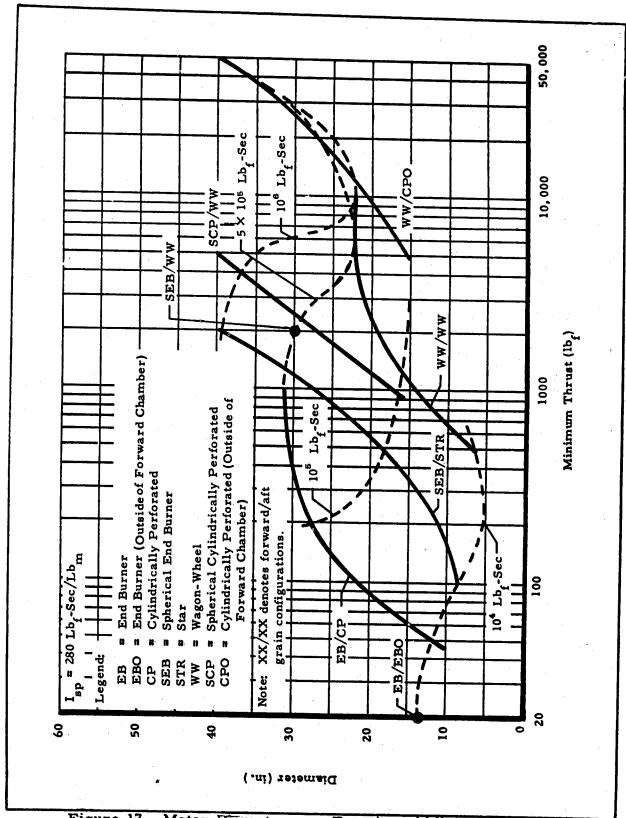


Figure 17 - Motor Diameter as a Function of Minimum Thrust and Total Impulse

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A minimum diameter is obtained for each total impulse level motor at different minimum thrust levels. Note that the optimum minimum thrust level increases with increasing total impulse.

In Figure 18, the effects of total impulse and minimum thrust on motor length are shown; the dotted lines connect designs with similar grain configurations. This graph shows that total impulse affects grain length much less than minimum thrust. This is also borne out in Figure 19 in which the band of motor length is plotted as a function of minimum thrust.

3. PHASE II

a. General

The results of Phase II, in which case material, burning rate constants, pressure exponents, and weight flow ratios were investigated, are presented in the following paragraphs.

b. Case Material

Three case materials, fiberglass, titanium, and steel, were investigated in Phase IIa. The effect of the mass fraction ratio of fiberglass to steel motors and titanium to steel motors as a function of minimum thrust is shown in Figure 20 for 100,000-lb-sec total impulse motors. The effect of delta velocity ratio for these same conditions is shown in Figure 21. The advantages of fiberglass and titanium over steel become more significant at the higher thrust levels. (Confidential)

The effects of case material on mass fraction and delta velocity as a function of thrust ratio are presented in Figures 22 and 23, respectively. As thrust ratio increases, which corresponds to higher chamber pressures, the effect of the three materials on mass fraction and delta velocity becomes more pronounced. (Confidential)

c. Burning-Rate Constants

The effects of forward- and aft-propellant burning-rate constants on optimum mass fraction and optimum delta velocity are shown in Figures 24 and 25, respectively, for 100,000-lb-sec motors. For this motor size the highest forward rate constant

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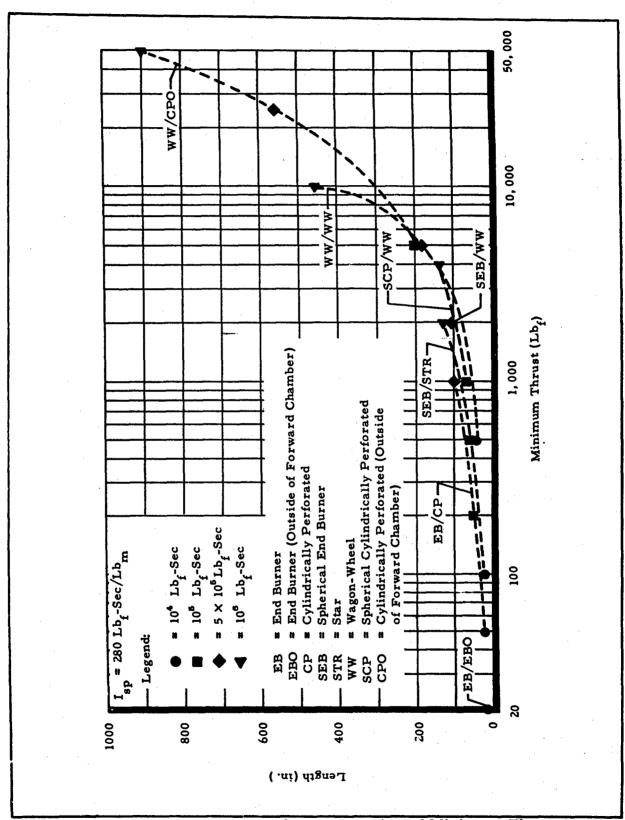


Figure 18 - Motor Length as a Function of Minimum Thrust and Total Impulse

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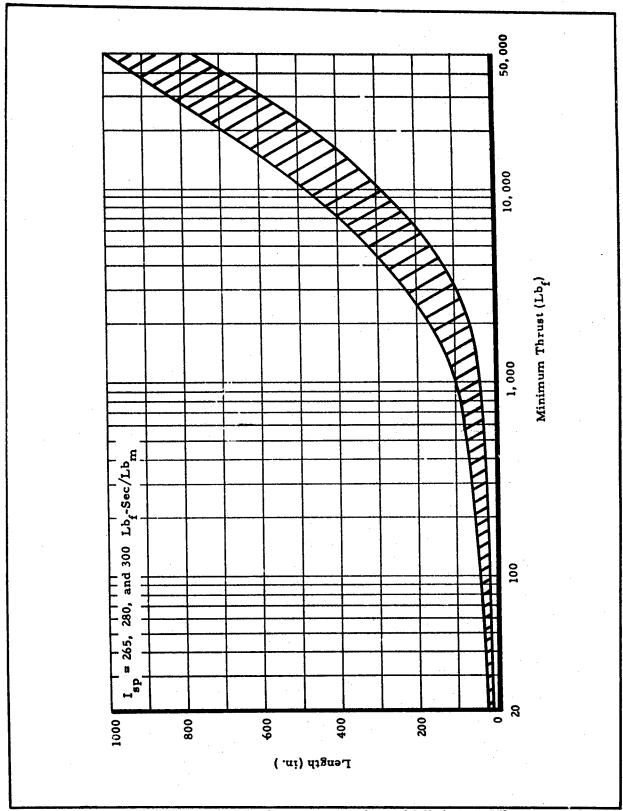


Figure 19 - Motor Length as a Function of Minimum Thrust

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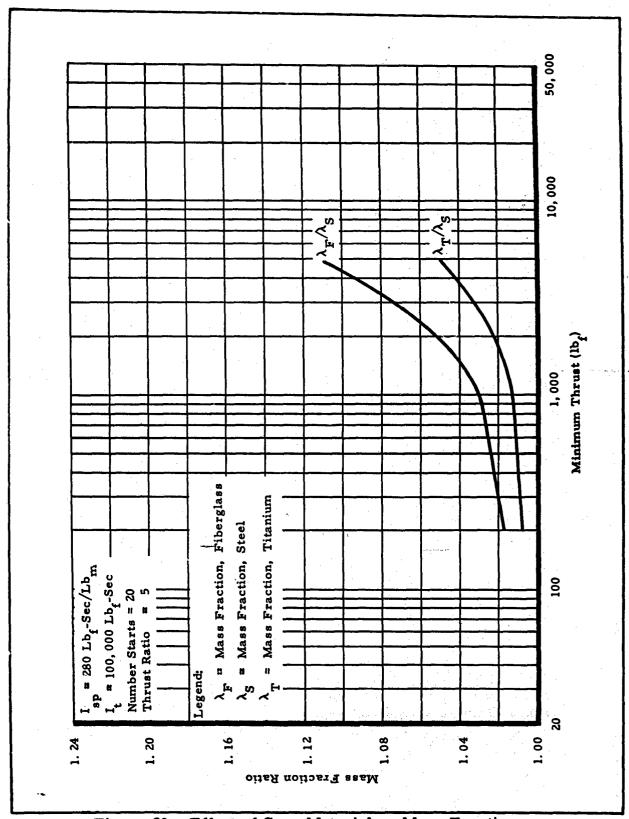


Figure 20 - Effect of Case Material on Mass Fraction

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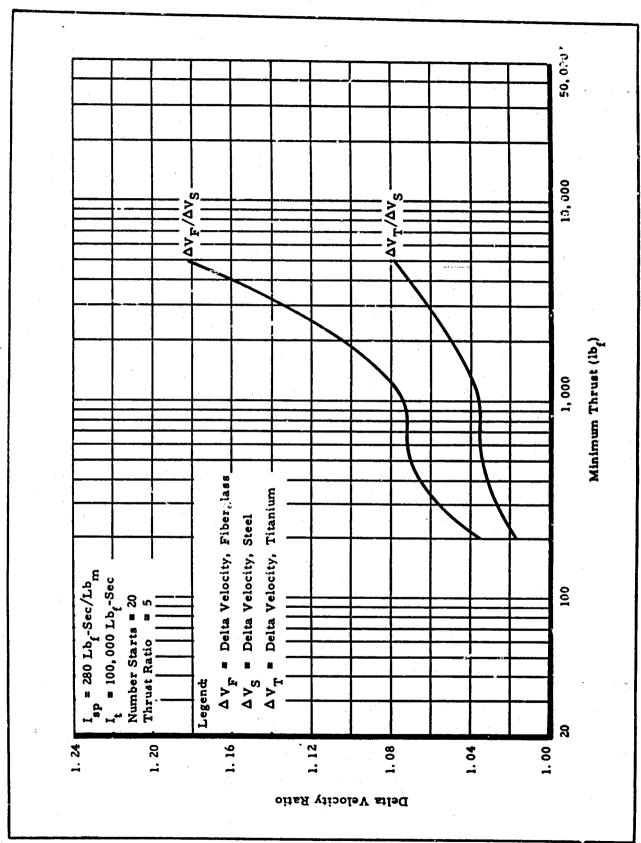


Figure 21 - Effect of Case Material on Delta Velocity

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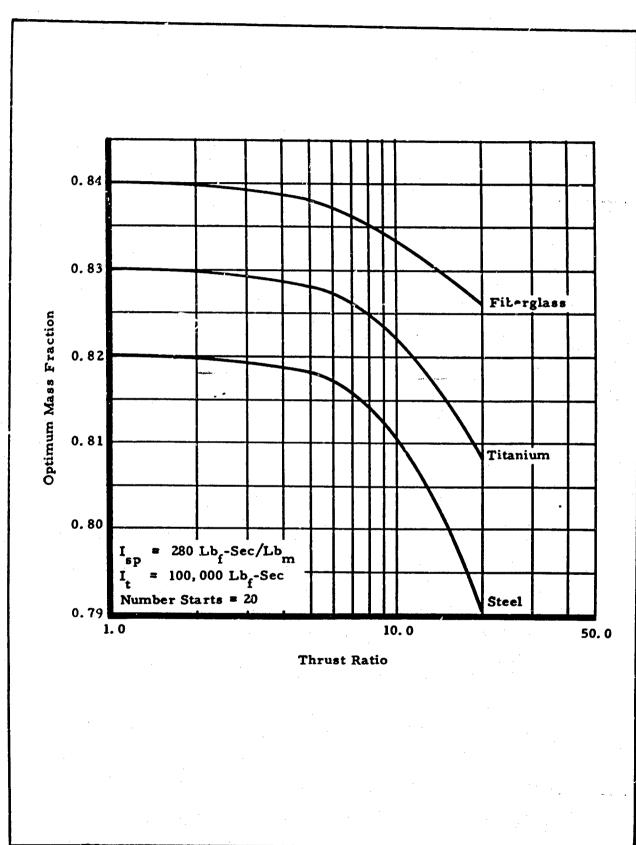


Figure 22 - Mass Fraction as a Function of Thrust Ratio for Three Case Materials

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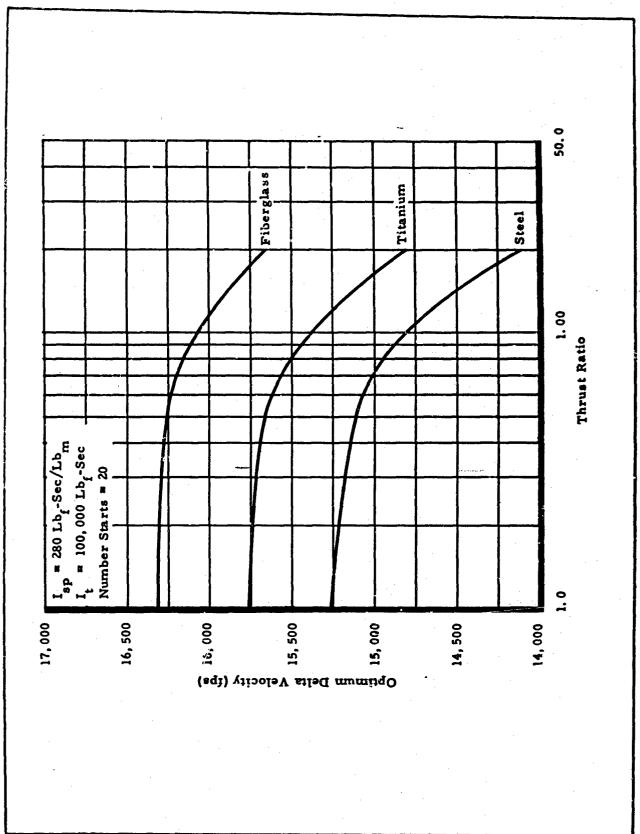


Figure 23 - Delta Velocity as a Function of Thrust Ratio for Three Case Materials

CONFIDENTIAL

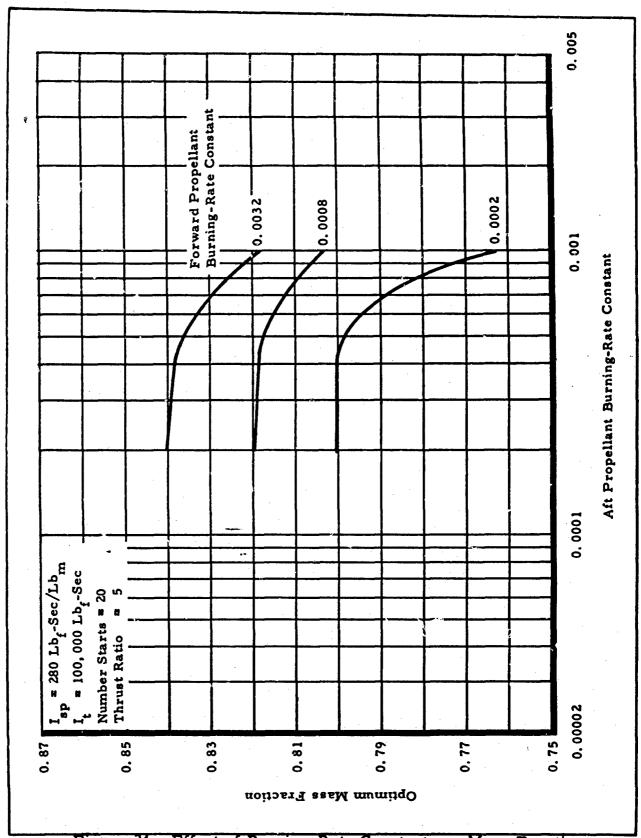


Figure 24 - Effect of Burning-Rate Constants on Mass Fraction

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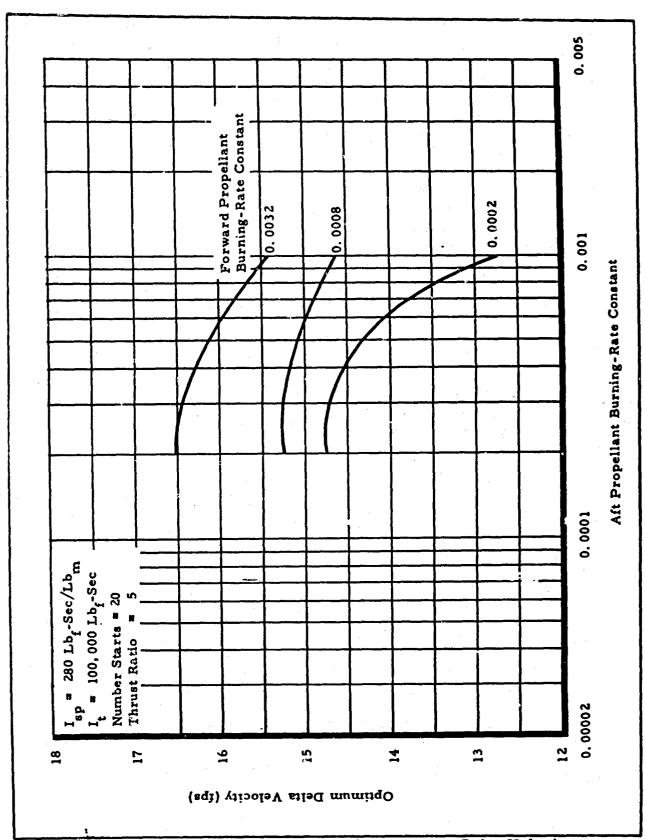


Figure 25 - Effect of Burning-Rate Constants on Delta Velocity

and lowest aft rate constant investigated produced the highest mass fraction and boost velocity. These constants gave motor designs with smaller diameters than others, as shown in Appendix B. The higher forward rate constant permitted an end-burning forward-grain configuration to be used, while the lower aft rate constant allowed a star aft-grain configuration to be employed. These optimize mass fraction and delta velocity values were calculated at a minimum thrust of 500 lb. At lower minimum thrust values, lower forward rate constants were more advantageous. (Confidential)

d. Pressure Exponents

As expected, the higher burning-rate pressure exponents give higher mass fractions and boost velocities for throttleable motors, as shown in Figures 26 and 27. At a thrust ratio of 20, the effects of forward and aft exponents are very pronounced. For example, as the forward exponent increases from 0.60 to 0.90 and the aft exponent changes from 0.80 to 1.00 (Figure 26), mass fraction increases from 0.52 to 0.81. For a thrust ratio of 5 to 1, on the other hand, the effect of the exponents is very slight. (Confidential)

e. Aft-to-Forward Weight Flow Ratio

The effects of ait to forward weight flow ratio (θ) on mass fraction and delta velocity are shown in Figures 28 and 29, respectively. The higher θ values are advantageous because, at these conditions, the aft chamber operates at a lower pressure than the forward chamber and has a higher aft propellant density. A θ of 4 produces less than a 4-percent increase in mass fraction over a θ of 2, but provides a 7.5-percent increase in delta velocity (Confidential)

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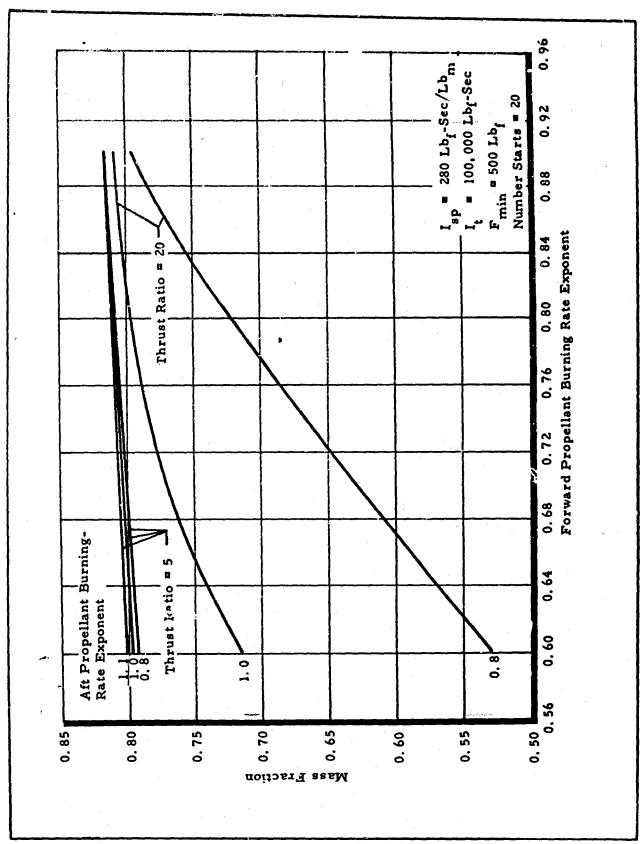


Figure 26 - Effect of Burning-Rate Pressure Exponents on Mass Fraction

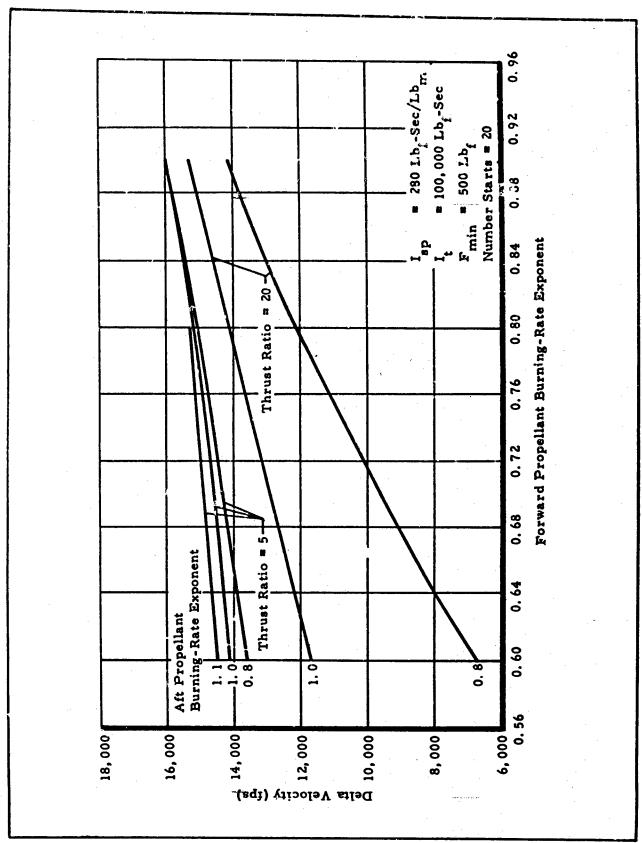
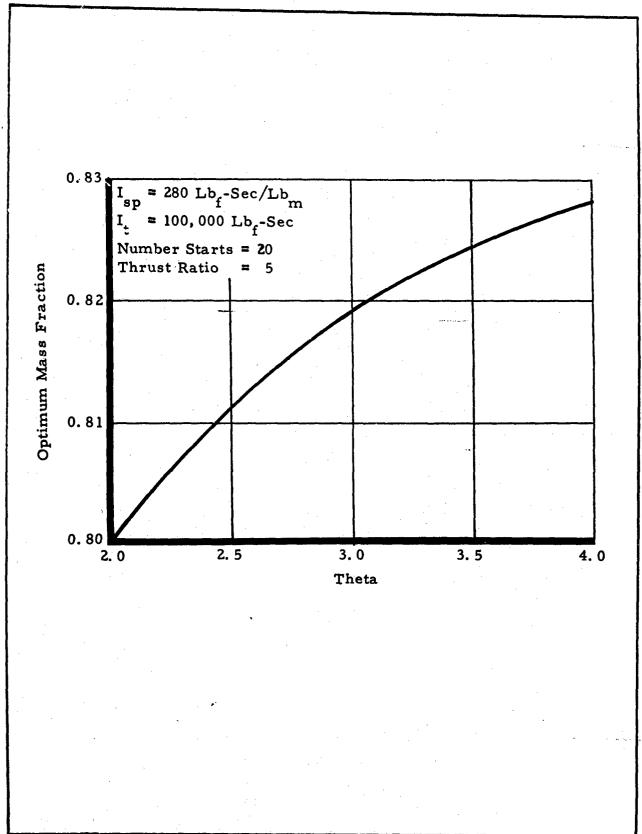


Figure 27 - Effect of Burning-Rate Pressure Exponents on Delta Velocity



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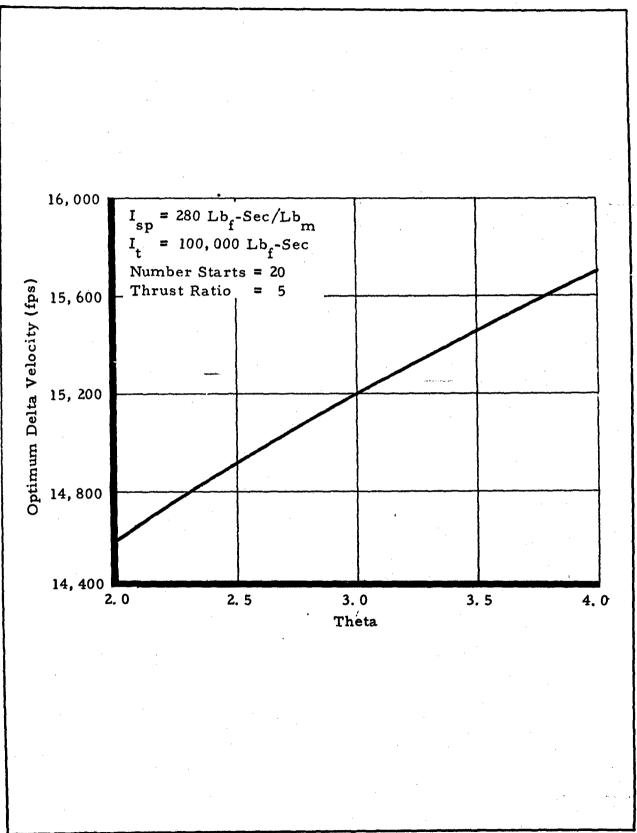


Figure 29 - Effect of θ on Delta Velocity

-53-

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SECTION IV - SUMMARY

Although the performance values for mass fraction, delta velocity, and envelope generated in this study are not intended to represent those that would be obtained from detailed designs, the values agree fairly well with those previously calculated in detail for individual motors.

It was found that, by increasing specific impulse, mass fraction is reduced but delta velocity and total motor weight are increased. For 10,000-lb-sec motors, an increase in specific impulse from 265 to 300 lb-sec/lb increased delta velocity by 7 percent, whereas for 1,000,000-lb-sec motors, the increase was 12 percent. (Confidential)

The mass fraction penalty imposed by a 20-to-1 thrust modulation was 2.5 percent for low-impulse (10,000 lb-sec), low-thrust (100 lb_f) motors. This penalty increased to above 4 percent as impulse increased to 1,000,000 lb-sec and thrust to 4,000 lb_f. These values were based on the characteristics of available propellants. Improved propellant pressure exponents would reduce the penalties. (Confidential)

For motors having stop-restart capability (that is, an on-off valve), the number of restarts available had little effect on mass fraction and delta velocity. The mass fraction penalty for additional igniters was less than 0. 1 percent per restart.

At each impulse level, there was an optimum thrust range for throttleable motors which was close to the optimum thrust level for nonthrottling motors. If the thrust was increased or decreased beyond this range, both mass fraction and delta velocity decreased.

Fiberglass and, to a lesser degree, titanium were found to be very advantageous for motor case materials, compared to steel, for motors with high thrust levels and high throttling requirements.

The highest forward propellant burning-rate constant and lowest aft propellant burning-rate constant investigated gave the highest mass fraction and delta velocity values for the 100,000-lb-sec motor size.

Mass fraction was more sensitive to forward and aft propellant pressure exponents than to any other propellant characteristics at high



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throttling ratios. Aft propellant pressure exponent significantly affected mass fraction for motors with low forward exponents. However, with high forward exponents, the effect of the aft exponent was much less. Conversely, forward exponent change is less significant with high aft exponents. (Confidential)

Increasing the aft-to-forward grain weight flow ratio from 2 to 4, for the 100,000-lb-sec motor size, increased mass fraction from 0.80 to 0.83. (Confidential)

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- 2. APR-7-2: Development of an Intermittent Operating Variable Thrust
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- 4. APR-7-4: Development of an Intermittent Operating Variable Thrust
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- 8. APR-21-5: <u>Dual-Chamber Controllable Solid Propellant Rocket</u>

 <u>Motor (U).</u> (Fourth Quarterly Report). Amcel Propulsion Company,

 Asheville, North Carolina, May 1964. (Confidential Report)

LIST OF REFERENCES (CONT'D)

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 <u>Motor (U)</u>. (Fifth Quarterly Report). Amcel Propulsion Company,
 Asheville, North Carolina, August 1964. (Confidential Report)
- 10. APR-21-7: <u>Dual-Chamber Controllable Solid Propellant Rocket</u>

 <u>Motor (U).</u> (Sixth Quarterly Report). Amcel Propulsion Company,
 Asheville, North Carolina, November 1964. (Confidential Report)
- 11. APR-21-8: <u>Dual-Chamber Controllable Solid Propellant Rocket</u>

 <u>Motor (U).</u> (Seventh Quarterly Report). Amcel Propulsion Company,

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- 12. APR-21-9: <u>Dual-Chamber Controllable Solid Propellant Rocket</u>

 <u>Motor (U).</u> (Eighth Quarterly Report). Amcel Propulsion Company,

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- 13. APR-21-4: Controllable Solid Propellant Rocket Motor (U). (Second Annual Report Fiscal Year 1963). RPL-TDR-64-52. Amcel Propulsion Company, Asheville, North Carolina, September 1964. (Confidential)

APPENDIX A - COMPUTER PROGRAMS

A printout of the entire computer program is presented on the following pages. The program is arranged by subroutine in the sequence shown in Figure 1. The individual subroutines are shown in more detail in Figures 2, 3, 5, and 6, respectively.

```
-5500
                    CSR STEADY STATE BALLISTIC PROGRAM. FOR PARAMETRIC STUDY
-6600
          C
                    DR. ALLEY M.K. OPPRECHT
                                                             AUGUST 1964
-6500
          C
                   REVISION BY W. OSTERHOUT OCTOBER 1,1961
-6500
-6500
               C(1)
C(2)
C(5)
C(5)
C(5)
-6500
                       IS CODE 1 - CODE FOR OPERATION OF STEADY STATE PROGRAM
-5500
                       IS CODE 2
                                      # CODE FOR OPERATION OF GRAIN CONFIGURATION PROGRAM
                      IS RHOF = FVD. PROP. DENSITY

IS ALPF = FVD. PROP. BURN RATE CONSTANT

IS ENPF = FVD. PROP. EXPONENT

IS RHOA = AFT. PROP. DENSITY
-5500
-5500
          Ċ
-5500
          C
-5500
-5500
-5500
-5500
                           ENPY = FWH. PROP. EXPONENT
RHOA = AFT. PROP. DENSITY
ALPA = AFT PROP. BURN RATE CONSTANT
EMPA = AFT PROP. EXPONENT
CDF = FWD. PROP. CD
S DELPF = DELTA FWD PRESSURE
S FMN = MINIMUM THRUST
S FMV = MAYIMUM THRUST
          0000000
               C(3)
C(3)
C(9)
C(10)
                       18
                       15
-5500
-5500
               C(112)
C(112)
C(112)
C(112)
C(112)
-6500
-6500
                            FMX = MAXIMUM THRUST
                            PFMI = FWD CHAMBER MINIMUM PRESSURE
-6600
                        15
                            THEPR = THETA PRIME
-5500
                        IS
                             PAMN = AFT CHAMBER MINIMUM PRESSURE
-5500
          C
                            XIPR = TOTAL IMPULSE AT THETA PRIME
                        IS
-6600
          C
                        15
                            WF = FVID PROP VIEIGHT
               C(131
-6600
          C
                        IS ASF = FVD PROP AVERAGE SURFACE AREA
-6600
          C
                        IS PFMX = FVD CHAMPER MAXIMUM PRESSURE
               C(19)
-6600
          C
               C(20)
                        IS ASA = AFT PROP AVERAGE SURFACE AREA
-6600
          C
               C(2.1)
                        IS BLANK
-6600
          C
               C(22)
                        IS BLANK
               C(23)
C(24)
C(25)
C(25)
-5600
          C
                        IS BLAIK
-6600
          C
                        IS BLANK
          C
-6500
                        IS BLANK
-6600
          C
                        IS BLANK
               C(28)
C(28)
C(30)
C(31)
C(32)
-6500
          C
                        IS ATA = AFT THROAT AREA
-6600
          CCC
                        IS WEBF = FWD WEB THICKNESS
-6600
                        IS WEBA = AFT WEB THICKNESS
-6600
                        IS WA # AFT PROP WEIGHT
-6600
                        IS
                            TBMX = MAXIMUM WER TIME
-6500
                        IS PAMX = MAXIMUM AFT PRESSURE
-6600
               C(33)
C(34)
                        IS CD = CDO
-6500
                       IS ATF = MAXIMUM OPERATING FUD THROAT AREA
          C
-6600
               C(35) IS BLANK
-6600
               18 FORMAT (11HTHETA PRIME, F14.2)
                              (11HTHETA PRIME, F14.2)
(11HAFT SURFACE, F14.2)
(10HAFT THROAT, F16.3)
(7HAFT VEB, F18.2)
(13HAFT PROP. WT., F12.2)
(11HFWD SURFACE, F14.2)
(7HFWD WEB, F18.2)
(13HFWD PROP. WT., F17.2)
(12HMAX WEB TIME, F13.2)
(7HFWD WEB, F18.2)
-6652
               19 FORMAT
-6704
               20 FORMAT
-6751
               23 FORMAT
-6798
               24 FORMAT
-6354
               25 FORMAT
               26 FORMAT
-6906
-6950
               27 FORMAT
-7006
               28 FORMAT
-7060
               51 FORMAT
                              (7HFWD WEB, F18.2)
-7101
               03 FORMAT (30H
30 FORMAT(/36H P FV/D
31 FORMAT (/)
              103 FORMAT
                                                                                   .F20.6.15)
THRUST)
-7198
                                                     P AFT
                                                                     THETA
-7300
               35 FORMAT (/13HPA GREATER PF)
43 FORMAT( F9.1,F9.1,F9.2,F9.0,F9.2,F9.4)
52 FORMAT(36X,36H WT AFT IMPULSE WEB AFT AT FW
-7322
-7378
-7436
-7540
              101 FORMAT( 14)
102 FORMAT( 3F20.10)
 -7562
```

```
-759%
               SWITCH 1 OFF TO PUNCH C(1) THRU C(35)
SWITCH 2 OFF TO ACCEPT THRUT CHANGES ANYWHERE IN C(1) THRU C(25)
-7591
. 7396
                SWITCH 3 OF STOPS ALL OUTPUT PRINTING EXCEPT SUPERY LINE
-799h
-759%
                DIMENSION THE (30), XISP (30), CD (30), C(35)
-759%
           50% PRINT 21
-750%
-7505
                READ 103
                PRINT 103
-7513
-7570
                SIIIICH 103
-7552
                KK=1
                IF (SENSE SWITCH 2)512,510
-7151
           510 PRINT 31
-7574
-7535
                READ 101.11
                100 499 K=1.4
-7710
           499 READ 107, THE(K), XISP(K), CD(K)
-7722
           DO 501 J=1,35

READ 103,C(J)

IF(C(J))550,501,550

550 PRINT 103,C(J)
-7373
מרדל...
-7933
-3013
-3055
           501 CONTINUE
-3102
                 30 TO 520
           512 READ 103, X, HP
17(X)511,520,511
511 PRINT 103, X, HP
-3110
-3145
-3202
                 C(IIP)=X
-3233
                 GO TO 512
-3274
            520 PRINT 31
-3292
                 S4=C(13)
 -3294
                 S5=C(14)
 -9306
                 S6=C(15)
 -3313
                 !!F=0
 -9330
                 LL=C(1)
 -9342
                 F1=C(11)
 -3373
                 P1=C(13)
 -3390
                 GO TO(10,:1,21),LL
 -8402
                 10=0PTION IA
 -3432
         C
                 11=0PTION IB
 -3432
                 21=0PT10H 11
 -3482
              10 C(20)=C(14)*C(3)*C(18)*C(4)*C(13)**C(5)/(C(6)*C(7)*C(15)**C(3))
 -3432
                 GO TO 12
 -3535
              11 C(14)=C(6)*C(20)*C(7)*C(15)**C(8)/(C(3)*C(18)*C(4)*C(13)**C(5))
 -9594
 _9303
              12 M=1
              13 THE I=C(14)
 -3910
 -8922
                 K=1
              14 IF(THE(K+1)-THE1)15.16.16
 -3934
              15 K=K+1
 -9025
                  GO TO 14
  -9052
              15 RATIO=(THEI-THE(K))/(THE(K+1)-THE(K))
  -9070
                  XISPO=XISP(K)+RATIO+(XISP(K+1)-XISP(K))
              GO TO(17,75,37) M
17 C(27)=(1.+C(15))*(C(3)*C(18)*C(13)*C(13)**C(5))/(C(33)*C(15))
PRINT 19,C(16)
PRINT 19,C(16)
  -9??5
  -9359
  -91490
  -9570
  -976?
                  PRILIT 19,C(20)
  -9735
                  PRINT 20 C(27)
C(28)=C(17)/(C(3)*C(19))
  -9910
  -9334
```

```
-9332
                   PRINT 51,C(28)
-9905
                   GO TO 29
-9914
              21 M=2
-9925
                   GO TO 13
              27 C(17)=C(16)/(XISPO*(1.+C(14)))
C(30)=C(17)*C(14)
C(31)=C(16)/C(11)
C(28)=C(31)*(C(4)*C(13)**C(5))
C(29)=C(31)*(C(7)*C(15)**C(8))
C(18)=C(17)/(C(3)*C(28))
C(20)=C(30)/(C(6)*C(29))
-9934
-99911
J0030
J0055
J0126
J0136
10234
J0232
                   C(27)=(1.+C(14))*C(3)*C(18)*C(4)*C(13)**C(5)/(C(33)*C(15))
J0450
                   PRINT 20,C(27)
J0474
                   PRINT 19,C(20)
J0493
                   PRINT 23,C(29)
J0522
                   PRINT 24,C(30)
J0546
                   PRINT 25,C(18)
J0570
                   PRINT 26,C(28)
                   PRINT 27,C(17)
PRINT 28,C(31)
J0594
J0613
JO5/17
              29 PRINT 30
70654
                   PRINT 52
J0ናኛና
                   PRINT 31
J0678
              14 CON1=C(3)*C(18)*C(4)*C(13)**C(5)
32 GOU3=C(6)*C(20)*C(7)*C(15)**C(8)
J0774
J0370
                   PACAL-(CON1+CON3)/(C(27)*C(33))
                   IF(PACAL-C(13))50,34,34
J0951
J1022
               34 PRINT 35
                   GO TO 46
J1034
              50 IF(PACAL-.998*C(15))40,36,48
48 IF(PACAL-1.002*C(15))36,46,49
J1042
J1134
J1226
              49 C(15)=2.*PACAL-C(15)
J1274
                   GO TO 32
J1232
               36 THECA=CON3/CON1
               IF(THECA-.998*C(14))38,39,37
37 IF(THECA-1.002*C(14))39,39,38
J1318
J1410
               38 C(
J1502
                         :=0.5*(C(14)+THECA)
J1550
                   M-3
J1562
                   GO 1
               39 F=X1 PO*(CON1*(1.+THECA))
J1570
J1630
             507 C(30)=C(17)*THECA
                   C(34)=CON1/(C(9)*C(13))
J1666
                   C(29)=C(28)*C(7)*PACAL**C(8)/(C(4)*C(13)**C(5))
XV=C(17)*(1.+THECA)*XISPO
J1714
J1858
             GO TO(509,508),KK
509 GO TO(40,40,41),LL
J1918
J1994
J2074
                   40=OPTION I
J2074
                   41=0PT10H 11
             40 IF(C(13)-C(19))42,42,46

41 IF(F-C(12))42,42,46

42 IF(SENSE SWITCH 3)513,514

514 PRINT 43,C(13),PACAL,THECA,F,C(30),XI,C(29),C(34)

513 IF(NF)1001,1002,1001
J2074
J2142
J2210
J2730
J2338
                   S1=C(29)
S?=C(30)
J2394
            100?
J2406
J2418
                    S3=C(34)
J2430
```

```
171112
            1001 F1=F
J2454
                   P1=PACAL
J2456
                   C(13)=C(13)+C(10)
GO TO 45
J2502
J2510
               45 KK=2
                  C(32)=((C(12)-F1)/(F-F1))*(PACAL-P1)+P1
C(19)=(C(12)/XISPG)-C(6)*C(20)*C(7)*C(32)***C(3)
C(19)=(C(19)/(C(3)*C(18)*C(4)))**(1./C(5))
THECA=(C(6)*C(7)*C(20)*C(32)**C(8))/(C(3)*C(4)*C(18)*C(19)**C(5))
J2522
J2666
J2322
J2954
J3158
                   GO TO 507
             508 PRINT 31 PRINT 43,C(19),C(32),THECA,C(12),C(30),XI,C(29),C(34)
J3166
J3178
J3286
                   C(30) = 52
J3298
J3310
                   C(34) = S3
J3322
                   C(13) = S4
J3334
                   C(14)=S5
J3346
                   C(15) = S6
J3358
             506 PAUSE
J3370
                   IF(SENSE SWITCH 1)502,503
             503 DO 504 J=1,35
504 PUNCH 102,C(J)
J3390
J3/102
J3496
                   GO TO 502
13494
                   END
PROCESSING COMPLETE
START
```

```
-6500
                  GRAIN CONFIGURATION PROGRAM FOR CSR PARAMETRIC STUDY
-5500
                  DR ALLEY
                                     H K OPPRECHT
                                                             AUG 64
-6500
          C
                  REVISION BY W. OSTERHOUT
                  DECEMBER 10,1964
PDO FORTRAIL PROGRAM
-6500
          C
-5500
         C
-5500
~5500
                  C(18) IS
                                 FORWARD CHAMBER AVERAGE SURFACE SO IN
                                                                                                  ASF
-5500
                  C(28) 1S
                                 FORWARD CHAMBER WER THICKNESS, IN
                                                                                                 WESF
-5500
                  C(27) 1S
         C
                                 AFT THROAT AREA. SO IN
                                                                                                  ATA
         C
                                 AFT AVERAGE SURFACE AREA, SO IN
-6500
                   C(20) IS
                                                                                                  ASA
-6600
                                 AFT WEB THICKNESS. IN
                                                                                                  WERA
-6600
-6600
                1 FORMAT(30H
                                                                              ,F20.6,13)
-6594
                2 FORMAT (F20.6)
-6716
                3 FORMAT (/22H FWD GRAIN IS A CYL EB)
-6790
                4 FORMAT(12H FWD PROP OD.F10.2)
               5 FORMAT(13H FWD PROP LEN,F10.2)
6 FORMAT(13H FWD PROP L/D,F10.2)
7 FORMAT(722H FWD GRAIN IS A SPH EB)
8 FORMAT(722H FWD GRAIN IS A CYL CP)
9 FORMAT(18H FWD CHAM VOL LOAD,F10.4)
-6844
-6900
-6956
-7030
-7104
              10 FORMAT (/22H FWD GRAIN IS A SPH CP)
11 FORMAT (/24H FWD GRAIN IS A CYL STAR)
-7170
-7244
-7322
               12 FORMAT (/24H FWD GRAIN IS A SPH STAR)
-7400
               13 FORMAT(/22H FWD GRAIN IS A CYL WW)
             102 FORMAT(/19H AFT GRAIN IS AN EB)
103 FORMAT(14H AFT GRAIN DIA, F10.3)
-7474
-7542
             103 FORMAT(19H AFT GRAIN DIA,FT0.3)
104 FORMAT(19H AFT GRAIN LEN,F10.3)
105 FORMAT(19H AFT GRAIN VOL LOAD,F10.3)
106 FORMAT(15H AFT GRAIN PORT,F10.3)
107 FORMAT(/18H AFT GRAIN IS A CP)
103 FORMAT(25H AFT PORT TO THROAT RATIO,F10.3)
109 FORMAT(/20H AFT GRAIN IS A STAR)
110 FORMAT(/18H AFT GRAIN IS A WW)
111 FORMAT(/20H AFT GRAIN IS A WW)
-7600
-7658
-7726
-7736
-7952
-7932
-3002
-8068
              111 FORMAT (/39H AFT GRAIN IS AN EB OUTSIDE OF FWD CHAM)
 -8176
             112 FORMAT (/38H AFT GRAIN IS A CP OUTSIDE OF FWD CHAM)
 -3232
             500 FORMAT (30H
-9366
                   DIMENSION C(37)
-9366
                   FORWARD CHAMBER CALCULATIONS OR PYROGEN CALCULATIONS
-9366
            1002 READ 500.11
-8390
                   PUNCH 500 N
                   PRINT 500 N
-8414
-8438
                   CONTROL 102
-9450
                   DIAA=0.
                   XLODA=0.
CONTROL 102
-8462
 -3474
                   DO 501 J=1,37
 -3486
              501 C(J)=0.
 -8493
                   DO 21 K=1,35
 -8570
               21 READ 2,C(K)
 -8582
 -8666
                    J=1
 -8678
                    L=1
                   DIAF=(C(18)/.7854)**.5
 -8690
```

```
-3739
                XLF=C(23)
-3750
                XLODF=XLF/DIAF
-9735
                IF(XLODF-.5)23,22,22
-3354
            ?? PRINTS
-7755
                C(37)=2.
-9373
                PRINTA, DIAF
PRINTS, XLF
PRINTS, XLODE
GO TO A5
-8902
-3925
-3350
            23 IF(XLODF-.2)25,24,24
24 DIAF=((C(18)*C(28))/.4199 )**(1./3.)
-3953
-9026
-31 :5
                ٧LF=.٩
-9170
                PRINT?
-3183
                C(37)=3.
            43 PRINTA, DIAF
-9:9%
                PRINT9, VLF
-9213
-9242
                XLODF=1.
-9254
                60 TO 45
-9262
            25 DIAF=C(29)/.35
-9298
                !4--1
-9310
            25 DIAFS=DIAF*DIAF
-93116
                VLF=(DIAFS-(DIAF-(2.*C(29)))**?.)/DIAFS
                XLF=C(18)*C(29)/(.7854*VLF*DIAFS)
-9454
-9550
                XLODF=XLF/DIAF
            1F(XLODF-3.)29,27,27
27 GO:TO (23,31),M
28 DIAF=C(28)/.3
-9536
-9654
-9730
-9765
                11=2
-9778
                GO TO 26
            29 PRINTS
-9786
-9793
                C(37)=1.
-9810
                J=?
            72 PRINT4, DIAF
-9322
                PRINTS, XLF
PRINT6, XLODF
-9346
-9370
                PRINT9, VLF
-9894
                GO TO 45
-9919
-9926
            31 DIAF=C(28)/.25
-9952
                M= 1
-9974
            VLF=.85
32 XLF=(C(18)*C(28))/(.7854*VLF*DIAF*DIAF)
-9993
J0106
                XLODF=XLF/DIAF
            IF(XLODF-3.)35,33,33
33 GO TO (34,37),H
J0142
J0210
40286
             34 M=2
J0298
                DIAF=C(28)/.2
J0331
                VLF=.8
J0358
                GO TO 32
             35 PRINT11
J0366
J0378
                C(37)=1.
J0390
                J=3
J01102
                GO TO 72
             37 DIAF=C(28)/.15
38 XLF=C(18)*C(28)/(.7854*VLF*DIAF*DIAF)
J0410
304/26
 J0554
                 XLODF=XLF/DIAF
```

```
J0590
                  IF(XLODF-3.)40,41,41
J0553
              40 PRINT13
J0670
                  C(37)=1.
J0532
                  GO TO 72
10590
              41 GO TO (45,42,40),44 42 DIAF=C(28)/.1
J0770
J0:305
                  M=3
J0313
                  VLF=.7
J0312
                  GO TO 38
J0350
                  AFT GRAIN DESIGN IF C(2)=1.
            45 1F(C(2))51,73,51
73 GO TO (81,20),L
81 GO TO (20,502,502),J
502 DIAF=(C(18)*C(28)/.4189)**(1./3.)
10350
20906
10932
J1052
J1132
                  VLF=.8
              GO TO (20,74,77),J
74 IF(C(23)-.3*DIAF)75,75,20
J1206
J1286
J1379
              75 PRINT 10
J1390
                  C(37)=1.
J1102
              76 PRINT 4, DIAF
                  PRINT 9, VLF
J1426
J1450
                  XLODF=1.
J1462
                  L=2
J1474
                  IF(C(2))80,20,80
              77 IF(C(28)-.2*DIAF)78,20,20
J1530
J1622
              78 PRINT12
J1634
                  C(37)=1.
                  XLODF=1.
J1646
                  GO TO 76
J1658
J1666
              51 CONTROL 102
J1678
                  CONTROL 102
              80 IF(XLODF-3.)65,65,63
65 DIAA=((C(20)+2.*C(27))/.786)**.5
J1690
J1753
J1830
                  XLODA=C(29)/DIAA
J1866
                  IF(XLODA-.5)55,53,53
J1934
              53 XLA=C(29)
J1946
                  APA=2.*C(27)
J1932
                  VLA=1.-APA/(DIAA*DIAA*.786)
J2066
                  PRINT102
                  C(36)=2.
J2078
J2090
              54 PRINT103, DIAA
                  PRINTIO4, XLA
J2114
                  PRINT105, VLA
J2138
                  PRINT106, APA
J2162
J2196
                  GO TO 73
J2194
              55 DIAA=DIAF
             55 DIAN=DIAF
WFA=C(29)/DIAA
IF(WFA-.3)60,56,56
56 IF(WFA-.4)90,59,59
90 APA=(DIAA-2.*C(29))**2.*.786
IF(APA-2.*C(27))59,57,57
57 VLA=1.-APA/(DIAA*DIAA*.786)
XLA=C(29)*C(20)/(.786*DIAA*DIAA*VLA)
DTA-APA/C(27)
J2206
J2212
J2310
J2378
 J2462
 J2554
 J2638
 J2746
                   PTA=APA/C(27)
 J2782
                   PRINT107
```

```
J2734
               C(35)=1.
J2305
           53 PRINTIOS, DIAA
               PRINTION, XLA
PRINTIOS, VLA
J2330
12354
J2373
               PRINTIOS, PTA
J2902
               GO TO 73
J2910
           59 APA=2.*C(27)
J2946
               DIAA=2.*C(29)+(APA/.786)**.5
               VLA=1.-APA/(DIAA*DIAA*.786)
XLA=C(29)*C(20)/(.786*DIAA*DIAA*VLA)
J3042
J3126
J3234
               PTA=?.0
J3245
               PRINT107
J3258
               C(36)=1.
J3270
               GO TO 58
J3278
            60 VLA=.85
J3302
            69 APA=(1.-VLA)*DIAA*DIAA*.786
12374
               IF (APA-2.*C(27))70,71,71
J37.55
            70 YLA=VLA-.05
J3502
               GO TO 69
J3510
               XLA=C(20)*C(29)/(.786*DIAA*DIAA*VLA)
1F(VFA-.2)62,61,61
J3513
J3686
               PRINT109
J3698
               C(36)=1
               GO TO 54
J3710
J3718
            62 PRINT110
J3730
               C(36)=1
            63 IF(C(29)-.6*XLF)64,66,66
J3742
J3750
            6/ IF(C(29)-.25*DIAF)68,65,65
66 APA=2.*C(27)
J3312
J3934
J3970
               DIAA=.2+((C(20)+APA+.786*DIAF*DIAF)/.796)**.5
XLA=C(29)
J4102
J4114
               VLA=C(20)/(C(20)+APA)
J4162
               PRINT111
J4174
               C(36)=3.
J4186
               GO TO 54
            68 APA=2.*C(27)
J4194
               DIAA=2.*C(29)+((APA+0.786*(2.*C(29)+DIAF+.2)**7.)/.786)**.5
CONI=.786*DIAA*DIAA-.786*(DIAF+0.2)**2.-APA
J4230
J4398
               VLA=CONI/(CONI+APA)
J4542
               XLA=C(29)*C(20)/CON1
J4590
J4638
               PRINT112
J4650
               C(36)=4.
J4662
               GO TO 54
J4670
               PUNCH OUTPUT UNLESS SENSE SWITCH 1 IS ON
        C
J4670
            20 IF(SENSE SWITCH 1)1002,1003
J4690
          1003 C(22)=DIAF
                C(23)=DIAA
J4702
                C(24)=XLODF
J4714
J4726
                C(25) = XLA/DIAA
J4762
                C(26)=C(2)
                DO 1001 K=1,37
J4774
J4786
          1001 PUNCH 1,C(K),K
J4382
                PAUSE
J4894
                GO TO 1002
14902
                END
PROCESSING COMPLETE
START
```

```
-6600
        C.
               CSR COMBINED WEIGHTS ANALYSIS PROGRAM
-6600
                PROGRAM 5017A 24 NOV 64 M A TODD
-6600
               DIMENSION C(70)
-6600
               DO 250 J=1.70
-6612
          250 C(J)=0
           10 READ 200 X, I
PUNCH 200 X, I
-6708
-6744
-6780
           201 READ 200 X. I
               IF(X-9999999))204,17,17
-6816
           204 C(1)=X
-6884
               GO TO 201
-6920
            17 MCAG=C(36)
-6928
               RHOF = C(3)
ALPF = C(4)
-6964
-6976
               ENPF = C(5)
-6988
               RHOA=C(6)
-7000
               ALPA=C(7)
-7012
               ENPA=C(8)
-7024
                PAMN=C(15)
-7036
                XIPR = C(16)
-7049
                WF=C(17)
-7060
                ASF = C(18)
-7072
                PFMX=C(19)
-7094
 -7096
                ASA=C(20)
               DIAF=C(22)
DIAA=C(23)
 -7108
-7120
                CHBNU = C(26)+1.
 -7132
                ATA=C(27)
 -7169
                WA=C(30)
 -7180
                TBMX=C(31)
 -7192
 -7204
                PAMX=C(32)
                ATF=C(34)
 -7216
                MCFG=C(37)
 -7228
                ROCHF=C(38)
 -7264
                ERATA=C(39)
 -7276
                SDCHA==C(40)
 -7288
                ROCHA=C(41)
 -7300
                ROINF=C(42)
 -7312
                ROINA=C(43)
 -7324
                CD=C(44)
 -7336
                WMIG=C(45)
 -7348
                GS1G=C(46)
 -7360
                FLTP I=C(47)
 -7372
                CPF=C(48)
 -7384
                THCOF=C(49)
 -7396
 -7403
                WMFG=C(50)
                 TEMF=C(51)
  -7420
                 CONIG=C(52)
  -7432
  -7444
                 XMF1G=C(53)
  -7456
                 ENIG=C(54)
                 SFIG=C(55)
SDNTH=C(56)
SDNST=C(57)
  -7463
  -7430
  -7492
  -7504
                 SDNXN=C(58)
  -7516
                 EXPRIMEC(59)
```

```
-7503
              TEHM=0(50)
              THCOA=C(5%)
ERATF=C(5%)
-7510
-7552
-7554
              SDCHF=C(6';)
-7576
              PRCOUMC(S5)
-7533
              CPA=C(SS)
-7500
              WHAG =C(67)
-7512
              IF(C(25)-1.)31.31.32
-7530
           31 ELODA=0.
-7592
              ERATA=1.0000001
-7704
              GO TO 33
           32 ELODA=C(25)-(ERATA-1.)/2.
-7712
           33 IF(C(24)-1.)34,34,35
-7784
-7352
           34 ELODF=0.
              ERATF=1.0000001
-7354
-7876
              GO TO 39
-7884
           35 ELODF=C(24)-(ERATF-1.)/2.
           39 RDCHF=DIAF/2.
-7956
-7992
              RDCHA=DIAA/2.
            4 RAD=(1,-(1./ERATA)**2.)**.5
VCX = ((RDCHA/ERATA)**2./2.*RAD)
-3028
           -9112
-3134
-8252
-8420
              GO TO 47
-8516
-2524
           45 TFCL=RDCHA*((3.*PAMX)/4.*SDCHA*ROCHA)**.5
              AFCL = 3.14159*(RDCHA)**7.
-8520
-3652
           47 15(TFCL-.025)43,44,44
-3735
           43 TFCL=.025
-3750
           ILL WECL=AFCL*TECL*ROCHA
              ACYL = 12.556*RDCHA*RUCHA*ELODA
TCYL=(PAMX*RUCHA/SDCHA*RCC'A)
-3303
-3359
-4723
               IF(TCYL-.025) 11,42,42
           41 TCYL=.025
-3996
-9020
           42 WCYL=ACYL*TCYL*ROCHA
              WACL=(AFCL-2.*ATA)*TFCL*ROCHA
WCHBT=WFCL=WACL+WCYL
-9053
-9152
-9200
               TINS=.007*TBHX*(((TEMA+460.)/5906.)**1.)+.05
-9320
               WINFC=AFCL*TIUS*ROINA
-9353
               VIHAC=(AFCL-2.*ATA)*TINS*ROINA
-9452
               WINCY=ACYL*TINS*ROINA
-9500
            IF(CHBUU-2.)209,8,8
8 F AD=(1.-(1./ERATF)**2.)**.5
-9500
-9553
               WFCX=((RDCHF/ERATF)**2./2.*F AD)
-9652
          IF(ERATF-2.5) 160,460,450
460 FAFCL=(WFCX*LOG((1.+F AD)/(1.-F AD))+RDCHF**2.)*3.14159
-9724
-9792
                                         )/(1,414*SDCHF*ROCHF)
-9960
               FTFCL=(PFHX*RDCHF
               GO TO 470
J0056
           450 FTFCL=RDCHF*((3.*PFMX)/4.*SDCHF*ROCHF)**.5
J0054
               FAFCL = 3.14159*(RDCHF)**2.
J0160
           470 IF(FTFCL-.025)430,440,440
 J0208
 J0276
           430 FTFCL=.025
           1440 FWFCL=FAFCL*FTFCL*ROCHF
 J0300
               FACYL = 12.566*RDCHF*RDCHF*ELODF
 103113
```

```
J0408
                   FTCYL=(PFMX*RDCHF)/(SDCHF*ROCHF)
J0492
                   IF(FTCYL-.025)410,420,420
J0550
             410 FTCYL=_025
J0531
             120 FWCYL=FACYL*FTCYL*ROCHF
J0632
                   FWACL=(FAFCL-2.*ATF)*FTFCL*ROCHF
J0716
                   FCHRT=FWFCL+FWACL+FWCYL
J0764
J0334
                   FTINS=.007*TBMX*(((TEMF+460.)/5806.)**4.)+.05
                   FINFC=FAFCL*FTINS*ROINF
J0932
                   FINAC=(FAFCL-2.*ATF)*FTINS*ROINF
J1016
                   FINCY=FACYL*FTINS*ROINF
J1064
                   GO TO(210,211,212), MCFG FWD GRAIN IS A CYL OR SPH CP, STAR, WAGONWHEEL
J1064
J11144
J1144
             210 FWINS=FINAC+FINFC
J1130
                   GO TO 209
J1188
                   FWD GRAIN IS A CYL END BURNER
J1138
             211 FWINS=FINAC+(FINCY/2.)
                   GO TO 209
J1236
J1244
                   FWD GRAIN IS A SPH END BURNER
J1244
             212 FWINS=FINAC+(FINFC/2.)
J1292
          C
J1292
             209 GO TO(205,206,207,208),MCAG
J1376
          C
                   AFT GRAIN IS A CP, STAR, OR WAGONWHEEL
J1376
             205 WINS-WINFC+WINAC
J1412
                   GO TO 100
J1420
                   AFT GRAIN IS AN END BURNER
J1420
             206 WINS=WINAC+(WINCY/2.)
J1468
                   GO TO 100
                   AFT GRAIN IS AN END BURNER OUTSIDE OF FORWARD CHAMBER
J1476
J1476
             207 WINS=WINFC+WINAC+(WINCY/2.)+FINAC+(FINCY/2.)
J1620
                   GO TO 100
                   AFT GRAIN IS A CP OUTSIDE OF FORWARD CHAMBER
J1628
             208 WINS=WINFC+WINAC+FINAC+FINFC
J1628
J1688
              100 WCASE=WCHBT+FCHBT
                   WINSL=WINS+FWINS
J1724
                   WIGT = 0.0
 J1760
                   WIGP = 0.0
 J1772
 J1794
                   WIG = 0.0
                   PUNCH501, SDNST, SDNTH, SDNXN, SDCHA, SDCHF, XIPR
PUNCH 502, TEMA, TEMF, PAMX, PFMX, PAMN
PUNCH503, ELODA, ELODF, ERATA, ERATF, DIAA, DIAF
PUNCH 504, CHBNU, PRCON, WA, WF, TBMX, EXPRN
PUNCH 505, ATA, ATF, ASA, ASF, ROINA, ROINF
PUNCH 506, FLTPI, WMAG, WMFG, ALPA, ALPF
PUNCH 507, SFIG, WMIG, ENIG, GSIG, CONIG, XMFIG
PUNCH 508, ENPA, ENPF, CPA, CPF, THCOA, THCOF
PUNCH 509, WIGT, WIGP, WIG, RHOA, RHOF, CD
PUNCH 510, WINSL, WINFC, WINAC, WINCY, WINS, MCFG
PUNCH 511, FINFC, FINAC, FINCY, FWINS
PUNCH 512, WCASE, WFCL, WACL, WCYL, WCHBT, MCAG
PUNCH 513, FWFCL, FWACL, FWCYL, FCHBT
 J1796
J1796
J1880
 J1952
 J2036
 J2120
 J2204
 J2276
 J2360
 J2444
 J2528
 J2612
 J2672
                    PUNCH 513, FWFCL, FWACL, FWCYL, FCHBT
 J2756
                    PUNCH 514, TCYL, TINS, FTCYL, FTINS, ROCHA, ROCHF
 J2816
                                                                                ,F20.6,13)
               200 FORMAT (30H
 J2900
               501 FORMAT(4H 100,6F11.0)
 J2994
```

```
502 FORMAT(4H 200,6F11.4)
503 FORMAT(4H 300,6F11.5)
504 FORMAT(4H 400,6F11.3)
505 FORMAT(4H 500,6F11.3)
J3056
13118
J3130
J3242
                            505 FORMAT(4H 500,6F11.3)
505 FORMAT(4H 500,6F11.5)
507 FORMAT(4H 700,6F11.4)
508 FORMAT(4H 300,6F11.8)
509 FORMAT(4H 300,6F11.3)
510 FORMAT(4H1000,5F11.3,111)
511 FORMAT(4H1100,6F11.3)
512 FORMAT(4H1200,5F11.3,111)
513 FORMAT(4H1300,6F11.3)
514 FORMAT(4H1300,6F11.4)
60 TO 10
J3304
J3355
73/173
 131.90
 J2552
 3351%
 J2676
 .12733
J3362
J3362
J2070
                                            END
 PROCESSING COMPLETE
 START
```

```
-6600
                     CSR COMBINED WEIGHTS ANALYSIS PROGRAM
-6600
                       PROGRAM 5017B 27 OCT 64 M A TODD
-6600
                     DIMENSION C(31)
-6600
                10 DO 250 J=1.31
-6612
               250 C(J)=0
-6703
                     READ 200,X
                     PRINT 200.X
-67<u>3</u>2
                     READ 501, SDNST, SDNTH, SDNXN, SDCHA, SDCHF, XIPR
-6756
                     READ 502, TEMA, TEMF, PAMX, PAMN, PAMN
READ 503, ELODA, ELODA, ERATA, ERATA, DIAA, DIAA
READ 504, CHBNU, PRCON, WA, WF, TBMX, EXPRN
READ 505, ATA, ATF, ASA, ASF, ROINA, ROINF
READ 506, FLPI, WMG, WMFG, ALPA, ALPF
-6840
-6912
-6996
-7030
-7164
                               507, SFIG, WMIG, ENIG, GSIG, CONIG, XMFIG
508, ENPA, ENPF, CPA, CPF, THCOA, THCOF
509, WIGT, WIGP, WIG, RHOA, RHOF, CD
510, WINSL, WINEC, WINAC, WINCY, WINS, MCFG
511, FINEC, FINEC, FINEY, FWINS
-7236
                     READ
-7320
                      READ
-7404
                     READ
-7433
                      READ
-7572
                     READ
                               512, WCASE, WFCL, WACL, WCYL, WCHBT, MCAG
-7632
                     READ
                               513, FWECL, FWACL, FWCYL, FCHBT
513, TCYL, TINS, FTCYL, FTINS, ROCHA, ROCHE
-7716
                     READ
                      READ
-7950
                      RDCHA = DIAA/2.
-7895
                      RDCHF = DIAF/2.
                      IF(CHBNU-2.)7,19,19
VALVE WEIGHT CALCULATION
-7932
-8000
                 VFREE=C(1),DTHT=C(2),DTH2=C(3),DTH3=C(4),PL1NS=C(5)
COVIN=C(6),TUBIN=C(7),PISIN=C(8),TOINS,C(9),PISTN=C(10)
PINT=C(11),COVE=C(12),PIST=C(13),CYL=C(14),DUCT=C(15)
STRUT=C(16),PL1AT=C(17),POWPK=C(18),SERVO=C(19),VALVE=C(20)
19 C(1)=6.283*(RDCHF*,)*(ELODF+2./(3.*ERATF))
-8000
-8000
-8000
-8000
-8000
                      C(2)=(ATF/.7856)**.5
-8120
-8168
                      C(3)=C(2)**2.
-8204
                      C(4)=C(2)**3
                 IF(TBMX-9.)20,21,21
20 C(5)=.0225*C(3)
-8240
-8308
-83!14
                      C(5) = .02097 * C(3)
                      C(7) = .0476 * C(3)
-8380
                      C(8) = .0146 * C(3)
-8416
-8452
                      GO TO 22
                 21 C(5) = .0025*C(3)*TBMX
-8460
                      C(6) = .00233*C(3)*TBHX
-8508
-3556
                      C(7) = .0053*C(3)*TBHX
                      C(8) = .00162 * C(3) * TBMX
-3604
                 22 C(9)=C(5)+C(6)+C(7)+C(8)
-8552
                 1F(C(2)-.68)23,24,24
23 C(10)=(.022*C(3))+(.000029h*C(3)*(PFMX**.5))
-8712
-8790
                      GÓ TO 25
-8912
                 24 C(10)=(.022*C(3))+(.0000581*C(4)*(PFMX**.5))
25 IF(C(2)-1.07)26,27,27
 -9920
 -9052
                 26 C(11) = .0302 * C(3)
 -9120
 -9156
                       GO TO 28
 -9164
                      C(11) = .0282 \times C(4)
                 28 |F(C(2)-2.38)29,30,30
29 C(12)=(.0931**C(3))+(.0575*C(4))
 -9200
 -9768
                       Gr TO 31
 -9352
```

```
-9360
           30 C(12)=.0966*C(4)
           31 IF(C(2)-2.67)32,33,33
-9396
-945%
           32 \text{ C(13)=.0403*C(3)}
-9500
               GO TO 34
-9508
           33 C(13)=(.022*C(3))+(.00676*C(4))
-9592
           34 IF(C(2)-2.9)35.36.36
35 C(14)=(.00792*C(3))+(.027*C(4))
-9660
-9744
               GO TO 37
-9752
           36 C(14)=.0297*C(4)
-9738
           37 IF(C(2)-1.07)38,39,39
-9355
           38 C(15)=.0602*C(3)
               GO TO 40
-9392
-9900
           39 C(15)=.00563*C(4)
-9936
           40 C(16)=(.000301*C(4)*(PFMX**.666))
C(17)=(.00939*C'4)*((PFMX-PAMX)**.5))
J0020
J0115
               C(18)=.33*C(4)
J0152
               C(19)=(.59*C(4))+.9
               C(31)=C(9)+C(10)+C(11)+C(12)+C(13)+C(14)+C(15)+C(16)+C(17)
J0200
J0320
               C(20)=C(31)+C(18)+C(19)
J0358
               AS=ASF
J0380
               RH0=RH0F
J0392
               TEM=TEMF
J0404
               ENP=ENPF
J0416
               CP=CPF
J0428
               ALP=ALPF
J01+1+0
               THCO=THCOF
J0452
               WMG=WMFG
J0464
               GO TO 100
J0472
               IGHITER WEIGHT CALCULATION
J0472
             7 PRINT 70
101t31t
               C(1)=6.283*(RDCHA**3.)*(ELODA+2./(3.*ERATA))
J0604
               AS=ASA
               RHO=RHOA
J0616
J0628
               TEM-TEMA
J0640
               ENP=ENPA
J0652
               CP=CPA
               ALP=ALPA
J0664
J0676
               THCO=THCOA
J0688
               WMG=WMAG
J0700
          100 CON1=AS *RHO *TEM *18550./(C(1) *WM G)
               CON2=(CON1*2.*THCO *ENP )/(CP *ALP *RHO )
3080L
               PSTAR = (CONIG*CON2)**(1./(1.+ENP))
J0928
J1048
               WIGP=(WMIG*PSTAR*C(1) )/(GSIG*FLTPI*18550.)*SFIG
J1168
               WIG=WIGP/XMFIG
J1204
               WIGT=WIG*ENIG
J1240
               NOZZLE WEIGHT CALCULATION
               WHST=C(21), SDST=C(22), WHSTR=C(23), WHTH=C(24), SDTH=C(25)
WHTHT=C(26), WHXI=C(27), SDXH=C(28), WHXIH=C(29), WHOZ=C(30)
J1240
J1240
               C(21)=((104.+(9.65*EXPRN))*(ATA)**1.5)*PANX/1000000.
J1240
               C(22) = 773000 /SDNST
J1360
               C(23)=C(21)*C(22)
J1396
J1432
               C(24)=1.53*ATA**.9
               C(25)=129900 /SDNTH
J1480
               C(26)=C(24)*C(25)
J1516
               C(27)=.00219*ATA*(EXPRN-4.)*TBMX*(1./CD)**1.7*PAKN**.9/1000000.
J1552
```

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```
C(28)=40000./SINIXH
J1769
J130%
                          C(29)=C(27)*C(28)
C(30)=C(23)+C(26)+C(29)
11340
J1334
                      COMPONENT LENGTH CALCULATION
                          FWDLT=2.*RDCHF*((ELODF*ERATF+1.)/ERATF)
AFTLT=2.*RDCHA*((ELODA*ERATA+1.)/ERATA)
XHOLT=((ATA/3.11159)**.5*((EXPR!)**.5-1.))/.3153
J1338
J1976
J210%
12224
                      MOTOR WEIGHT, MASS FRACTION, AND DELTA VELOCITY CALCULATION
J2224
                          WCHR=WCASE +VINSL
32250
                          WINRT = (WCHB+C(20)+V/IGT+C(30))*1.02
J2332
                          WPROP=VIA+VIF
J2353
                          XMFRC=(WA+WF)/(WPROP+WINRT)
12452
                          DELV=(32.174)*(XIPR/WPROP)*LOG ((WINRT+WPROP)/(WINRT))
J2572
                          VMTP=VINRT+VPROP
J2603
                           IF GRAIN CONFIG IS TANDEM ADD ALL LENGTHS. IF GRAIN CONFIG IS
J2503
                          PARALLEL CHECK FOR LONGER OF FWD AND AFT CHANGERS AND ADD NOZZLE
J2608
J2675
                           IF(MCAG-3)300,301,301
                  300 RLGT=FVDLT+AFTLT+XNOLT
J272h
                          GO TO 304
                   301 IF(FWDLT-AFTLT)302,302,303
J2732
J2300
                  302 REGT=AFTLT+XNOLT
J2836
                           GO TO 304
12944
                  303 RIGT=FVDLT+XNOLT
                  301 IF(RDCHF-RDCHA)305,305,306
305 RDIA=2.*RDCHA+2.*TCYL+2.*TINS
J2830
J2943
                           GO TO 307
J3030
73033
                   305 RDIA=? * (RDCHF+FTCYL+FTINS)
                 305 RDIM=R.G. (RICHF4F C. P. SFITNS)
307 ELODM=RLGT/RDIA
1F(SENSE SWITCH 1)309,303
308 IF(SENSE SWITCH 2) B11,310
311 PRINT 511, C(1), CON1, PSTAR, FWDLT, AFTLT, XNOLT
310 PRINT501, SDNST, SDNTH, SDNXN, SDCHA, SDCHF, XiPR
PRINT 502, TEMA, TEMF, PAMX, PFMX, PAMN
PRINT503, ELODA, ELODF, ERATA, ERATF, DIAA, DIAF
PRINT 504, CHBNU, PRCON, WA, WF, TBMX, EXPRN
PRINT 505, ATA, ATF, ASA, ASF, ROINA, ROINF
PRINT 506, FLTP1, WMAG, WMFG, ALPA, ÅLPF
PRINT 507, SFIG, WMIG, ENIG, GSIG, CONIG, XMFIG
PRINT 509, WIGT, WIGP, WIG, RHOA, RHOF, CD
PRINT 509, WIGT, WIGP, WIG, RHOA, RHOF, CD
PRINT 510, WINSL, WINFC, VINAC, WINCY, WILLS, HICFG
PRINT 511, FINFC, FINAC, FINCY, FWINS
PRINT 512, WCASE, WFCL, WACL, WCYL, WCHBT, MCAG
PRINT 513, FWFCL, FWACL, FWCYL, FCHBT
PRINT 515, C(20), C(30), C(10), C(13), C(11), C(12)
PRINT 516, C(19), C(18), C(17), C(16), C(15), C(14)
PRINT 518, WMTR, RDIA, RLGT, XMFRC, DELV, ELODM
PUNCH 200, XMFRC, DELV, RLGT, RDIA
70 FORMAT (28HSINGLE CHAMBER MOTOR FOLLOWS)
13149
                   307 ELODM=RLGT/RDIA
J3134
13204
J2274
13303
13377
باكاأبهار
J35113
J3632
J3716
J3793
J3872
13955
74040
JA12A
J4134
J4269
Jk328
 j!s496
 J<sup>1</sup>-580
 J1652
 J4736
                     70 FORMAT (29HSINGLE CHAMBER MOTOR FOLLOWS)
 J':796
                   200 FORMAT(30H
501 FORMAT(4H 100,6F11.0)
502 FORMAT(4H 200,6F11.4)
 J4376
                                                                                                              .F11.3.F11.0.2F11.2)
 74980
 J5042
                   503 FORMAT(4H 300,6F11.5)
 J5101
```

```
50% FORMAT(%H %00,6F11.3)
505 FORMAT(%H 500,5F11.3)
505 FORMAT(%H 500,5F11.3)
507 FORMAT(%H 700,5F11.6)
503 FORMAT(%H 800,6F11.8)
509 FORMAT(%H 900,6F11.3)
510 FORMAT(%H1000,5F11.3,111)
511 FORMAT(%H1000,5F11.3,111)
512 FORMAT(%H1200,5F11.3,111)
513 FORMAT(%H1200,5F11.3)
514 FORMAT(%H1300,6F11.4)
515 FORMAT(%H1500,6F11.4)
516 FORMAT(%H1500,6F11.4)
517 FORMAT(%H1700,6F11.4)
513 FORMAT(%H1300,6F11.4)
513 FORMAT(%H1300,6F11.4)
J5155
15290
J5352
J5414
J5576
J5539
J5690
 J572h
 .15735
15310
 15910
 J5972
  15031
 J6095
                                                   COUTROL 102
 J6103
                                                   GO: TO 10
 J6115
                                                   EID
 PROCESSING COMPLETE
 START
```

APPENDIX B - PRESENTATION OF DATA

A detailed presentation of data from this study is given herein in Figures B-1 through B-66. For ease of reference, the figures are presented by phase, and are arranged in sequence. Figures B-1 through B-30 present the results from Phase I; the remaining figures are for Phase II.

The plots for Phase I are presented in the following sequence:

- Mass fraction versus minimum thrust at an I_{sp} of 265 lb_f-sec/lb_m for 1, 10, and 20 starts (Figures B-1, B-2, and B-3, respectively); at an I_{sp} of 280 lb_f-sec/lb_m for 1, 10, and 20 starts (Figures B-4, B-5, and B-6, respectively); and at an I_{sp} of 300 lb_f-sec/lb_m for 1, 10, and 20 starts (Figures B-7, B-8, and B-9). For each plot, curves are shown for total impulse values of 10⁴, 10⁵, and 10⁶ lb_f-sec at constant thrust ratios of 1, 5, and 20.
- Mass fraction versus total impulse for burn times of 20, 50, 200, and 500 sec (Figures B-10 through B-13, respectively). All curves are for 10 starts and constant specific impulse of 280 lb_f-sec/lb_m.
- Delta velocity versus minimum thrust at an I sp of 265 lb sec/lb for 1, 10, and 20 starts (Figures B-14, B-15, and B-16, respectively); at an I sp of 280 lb sec/lb for 1, 10, and 20 starts (Figures B-17, B-18, and B-19, respectively); and at an I sp of 300 lb sec/lb for 1, 10, and 20 starts (Figures B-20, B-21, and B-22, respectively). For each plot, curves are shown for total impulse values of 10⁴, 10⁵, and 10⁸lb sec at constant thrust ratios of 1, 5, and 20.
- Delta velocity versus total impulse for burn times of 20, 50, 200, and 500 sec (Figures B-23 through B-26, respectively). All curves are for 10 starts and constant specific impulse of 280 lb_f-sec/lb_m.

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- Length versus minimum thrust for I's of 265 and 300 lb -sec/lb (Figures B-27 and B-28, respectively). Curves of constant configuration are shown on each plot.
- Diameter versus minimum thrust for I_{sp} of 265 and 300 lb_f-sec/lb_f (Figures B-29 and B-30, respectively). Curves of constant configuration and constant total impulse values (10⁴, 10⁵, 5 × 10⁵, and 10⁶ lb_f-sec) are shown on each plot.

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The plots for Phase II are arranged as follows:

- Mass fraction versus minimum thrust at thrust ratios of 1, 5, and 20 (Figures B-31, B-32, and B-33, respectively). Curves for three materials are shown on each plot.
- Delta velocity versus minimum thrust at thrust ratios of 1, 5, and 20 (Figures B-34, B-35, and B-36, respectively). Curves for three materials are shown on each plot.
- Mass fraction versus minimum thrust for aft propellant burningrate constants of 0.0002, 0.0004, and 0.0010 (Figures B-37, B-38, and B-39, respectively). Curves for constant forward propellant burning rates of 0.002, 0.0008, and 0.0032 are shown on each plot.
- Delta velocity versus minimum thrust for aft propellant burning-rate constants of 0.0002, 0.0004, and 0.0010 (Figures B-40, B-41, and B-42, respectively). Curves for constant forward propellant burning rates of 0.0002, 0.0008, and 0.0032 are shown on each plot.
- Length versus aft propellant burning-rate constant at minimum thrust values of 200, 500, 1000, and 5000 lb (Figures B-43 through B-46, respectively). Curves for constant forward propellant burning rates of 0.0002, 0.0008, and 0.0032 are shown on each plot.
- Diameter versus aft propellant burning-rate constant at minimum thrust values of 200, 500, 1000, and 5000 lb, (Figures B-47, through B-50, respectively). Curves for constant forward propellant burning rates of 0.0002, 0.0008, and 0.0032 are shown on each plot.

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- Mass fraction versus thrust ratio at forward propellant burningrate exponents of 0.6 0.8, and 0.9 (Figures B-51, B-52, and B-53, respectively). Curves for constant aft propellant burning rate exponents of 0.8, 1.0, and 1.1 are shown on each plot.
- Delta velocity versus thrust ratio at forward propellant burningrate exponents of 0.6, 0.8, and 0.9 (Figures B-54, B-55, and B-56, respectively). Curves for constant aft propellant burning-rate exponents of 0.8, 1.0, and 1.1 are shown on each plot.
- Length versus thrust ratio at forward propellant burning-rate exponents of 0.6, 0.8, and 0.9 (Figures B-57, B-58, and B-59, respectively). Curves for constant aft propellant burning-rate exponents of 0.8, 1.0, and 1.1 are shown on each plot.
- Diameter versus thrust ratio at forward propellant burningrate exponents of 0.6, 0.8, and 0.) (Figures B-60, B-61, and B-62, respectively). Curves for constant aft propellant burningrate exponents of 0.8, 1.0, and 1.1 are shown on each plot.
- Mass fraction versus minimum thrust (Figure B-63). Curves for constant theta values of 2, 3, and 4 are shown.
- Delta velocity versus minimum thrust (Figure B-64). Curves for constant theta values of 2, 3, and 4 are shown.
- Length versus minimum thrust (Figure B-65). Curves for constant theta values of 2, 3, and 4 are shown.
- Diameter versus minimum thrust (Figure B-66). Curves for constant theta values of 2, 3, and 4 are shown.

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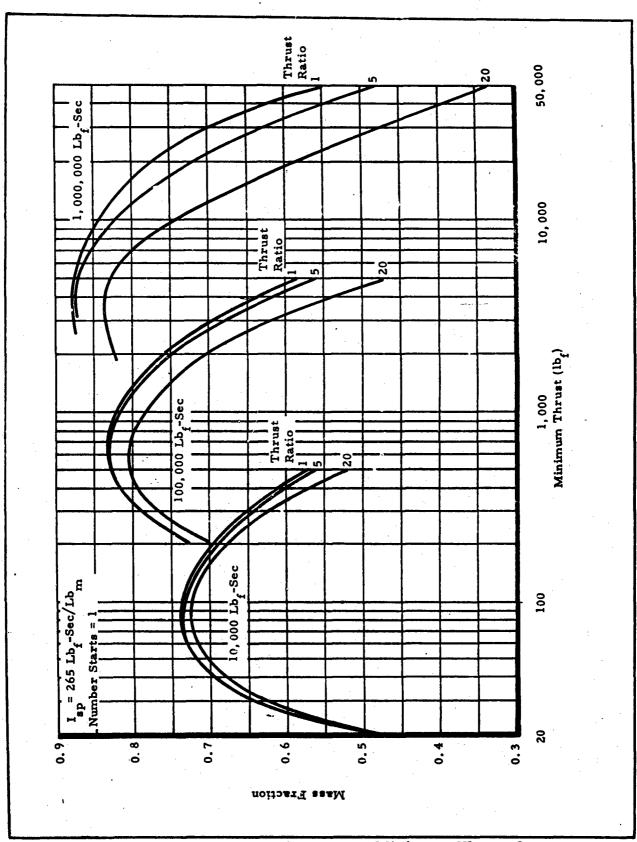


Figure P. 1 - Mass Fraction versus Minimum Thrust for
I = 265 Lb_f-Sec/Lb_m and 1 Start
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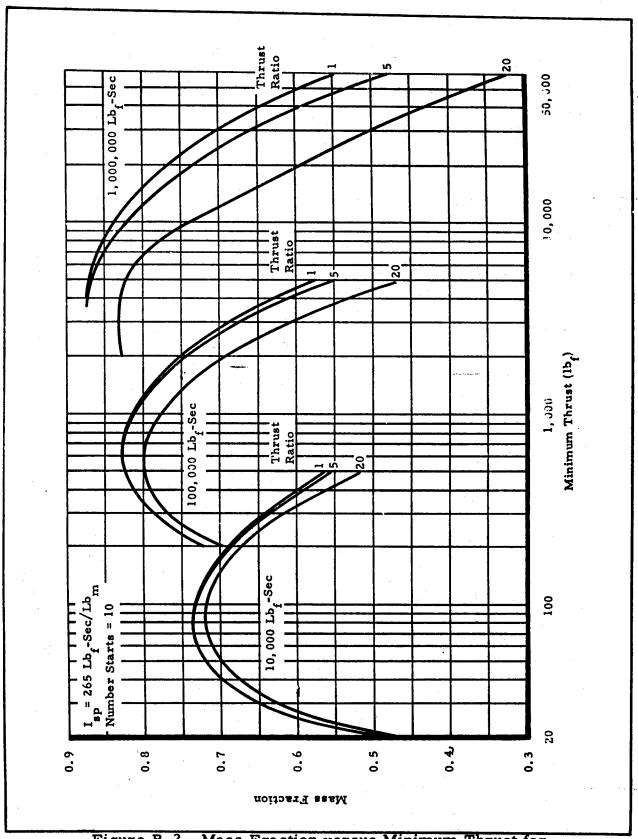


Figure B-2 - Mass Fraction versus Minimum Thrust for
I = 265 Lb_f-Sec/Lb_m and 10 Starts
CONFIDENTIAL

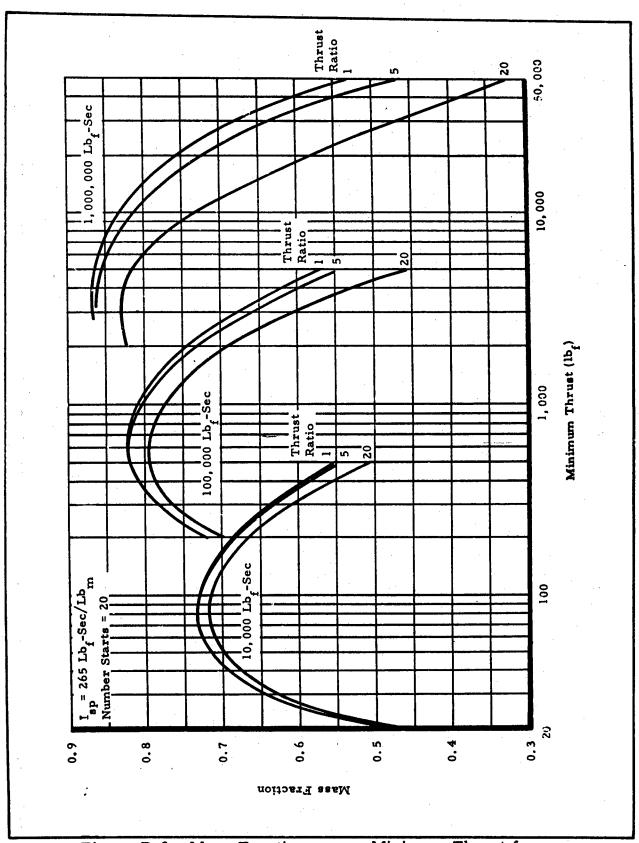


Figure B-3 - Mass Fraction versus Minimum Thrust for

I = 265 Lb_f-Sec/Lb_m and 20 Starts

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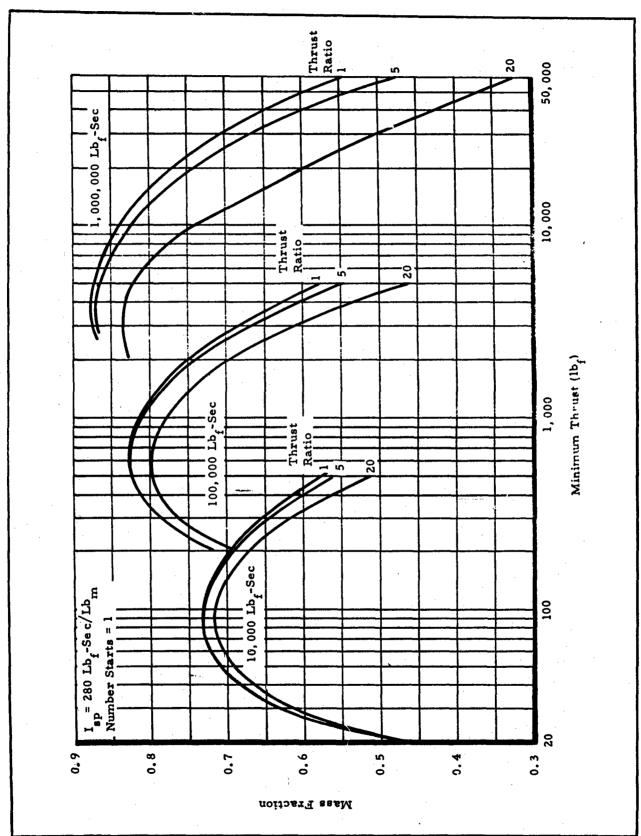


Figure B-4 - Mass Fraction versus Minimum Thrust for

I = 280 Lb_f-Sec/Lb_m and 1 Start

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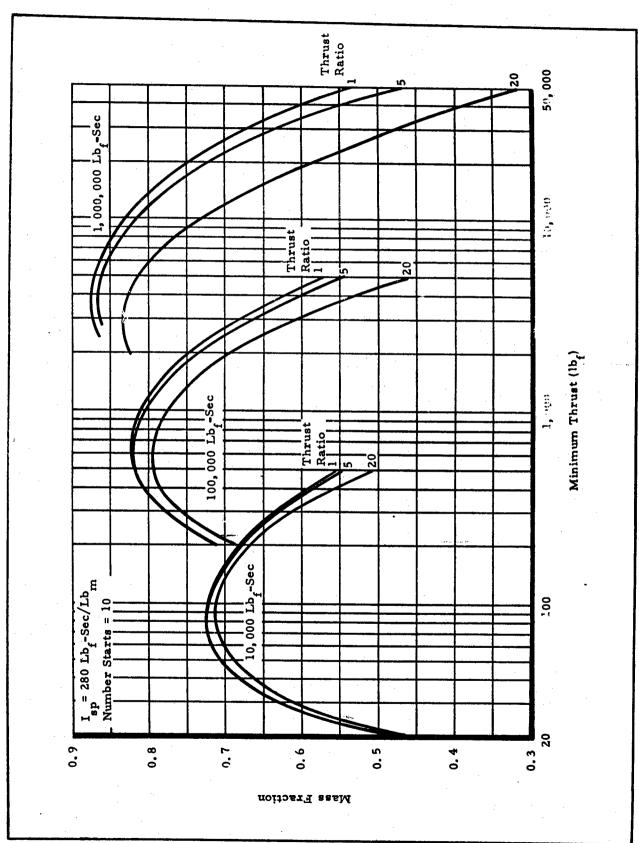


Figure B-5 - Mass Fraction versus Minimum Thrust for I = 280 Lb_f-Sec/Lb_m and 10 Starts

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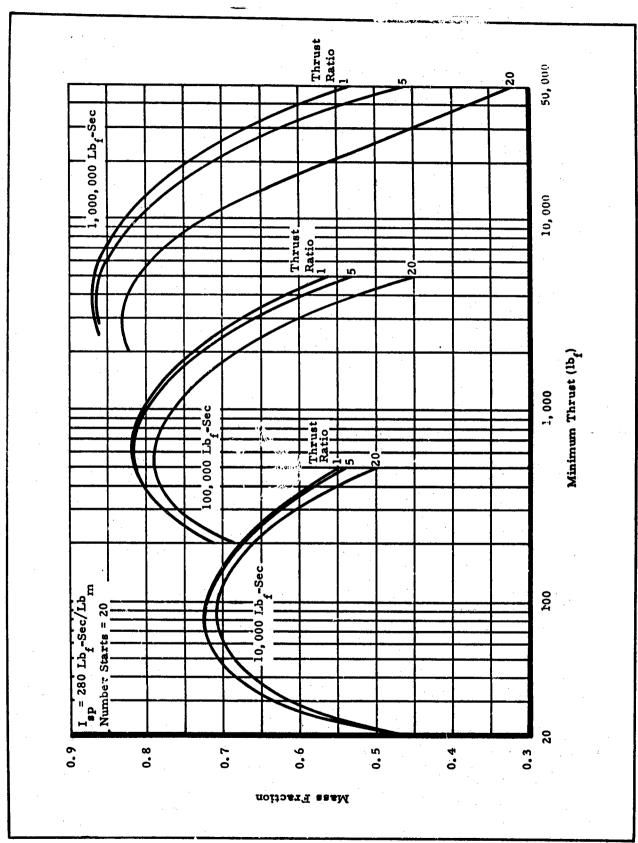


Figure B-6 - Mass Fraction versus Minimum Thrust for

I = 280 Lb - Sec/Lb and 20 Starts

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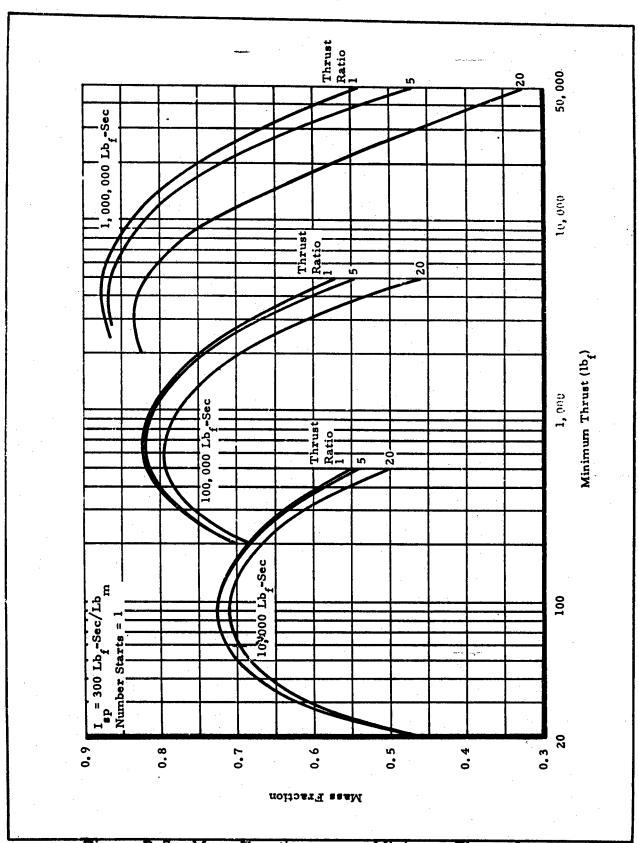


Figure B-7 - Mass Fraction versus Minimum Thrust for

I = 300 Lb_f-Sec/Lb_m and 1 Start

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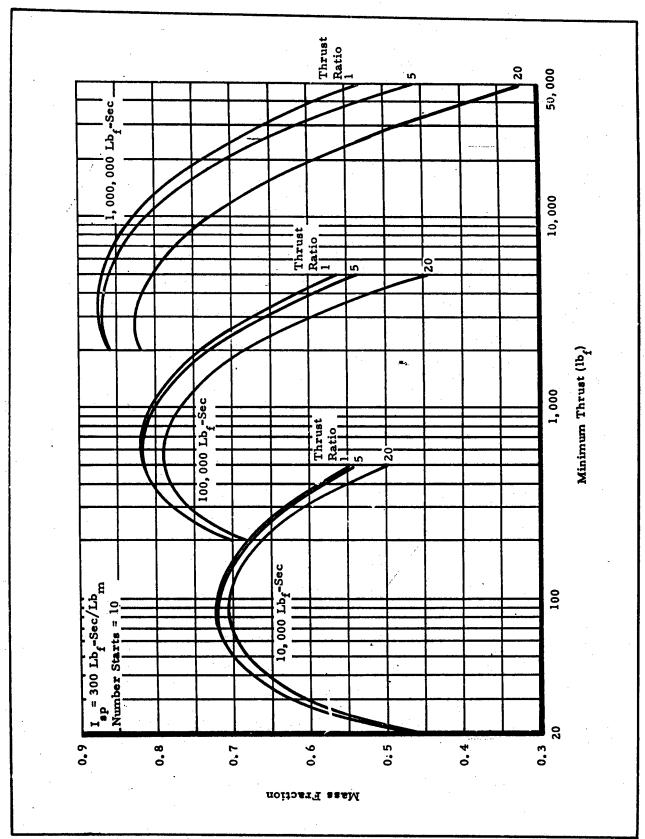


Figure B-8 - Mass Fraction versus Minimum Thrust for

I = 300 Lb_f-Sec/Lb_m and 10 Starts

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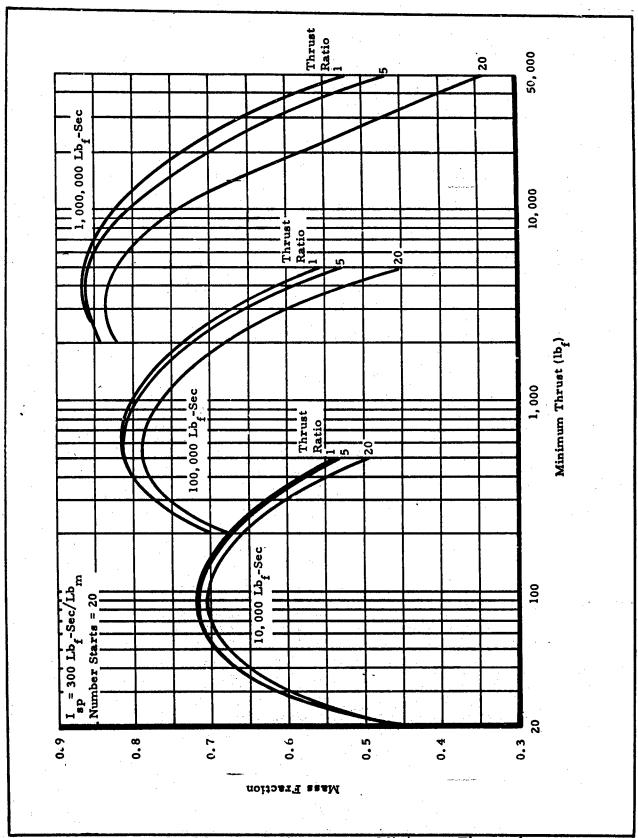


Figure B-9 - Mass Fraction versus Minimum Thrust for

I = 300 Lb_f-Sec/Lb_m and 20 Starts

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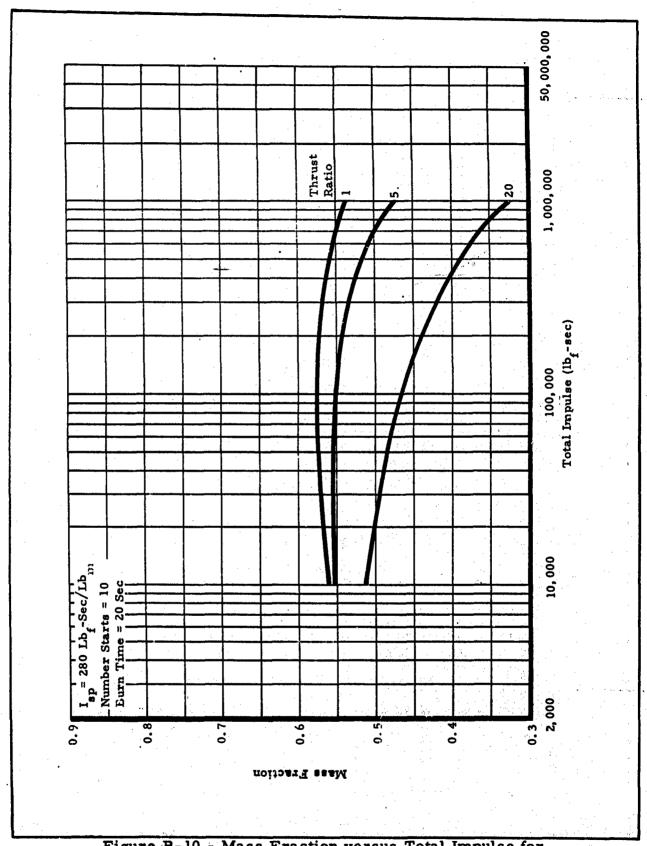


Figure B-10 - Mass Fraction versus Total Impulse for -20-Sec Burn Time

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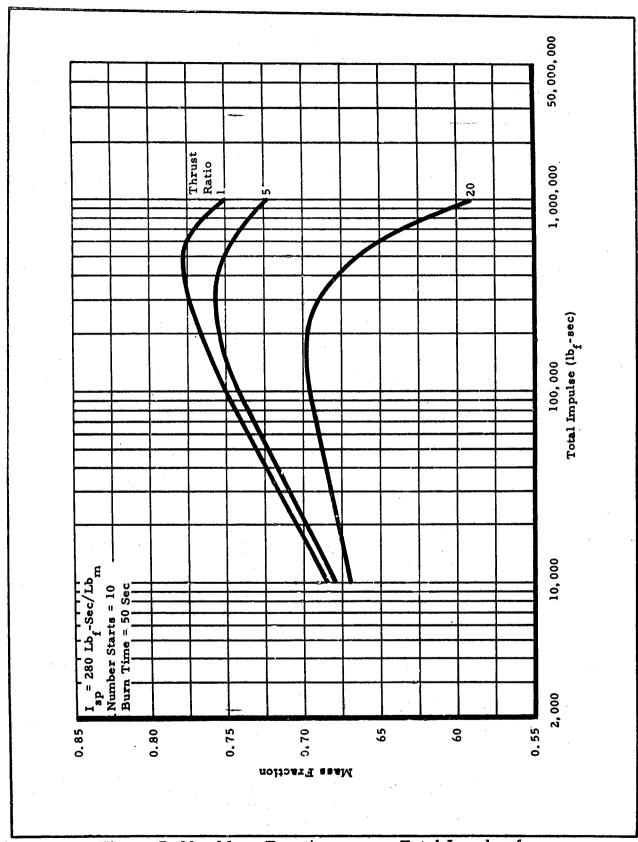


Figure B-11 - Mass Fraction versus Total Impulse for 50-Sec Burn Time

50-Sec Burn Time
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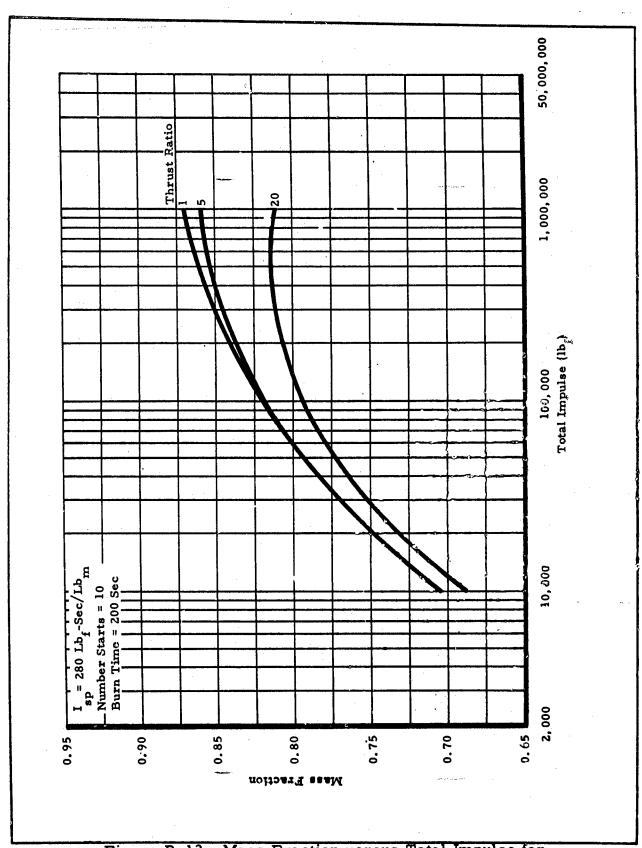


Figure B-12 - Mass Fraction versus Total Impulse for 200-Sec Burn Time

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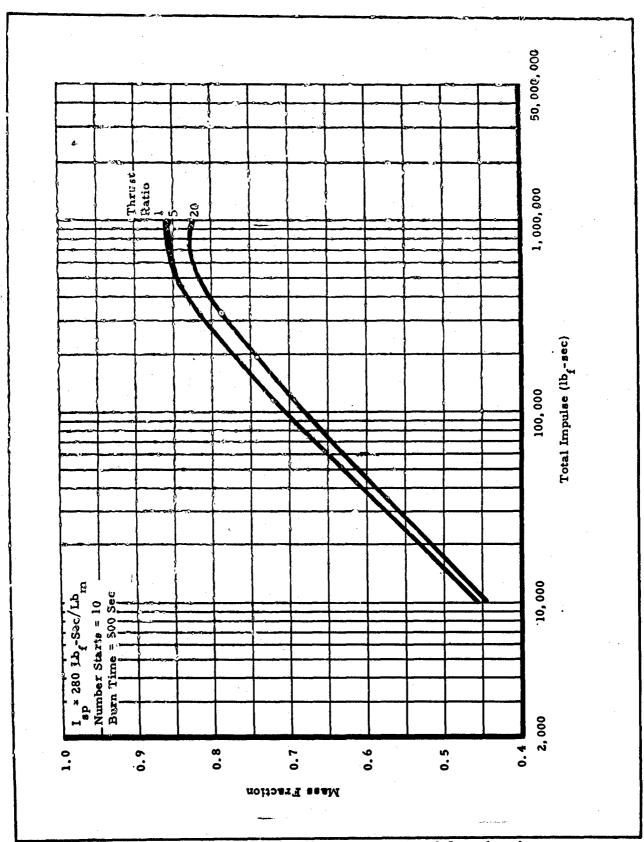


Figure B-13 - Mass Fraction versus Total Impulse for 500-Sec Burn Time

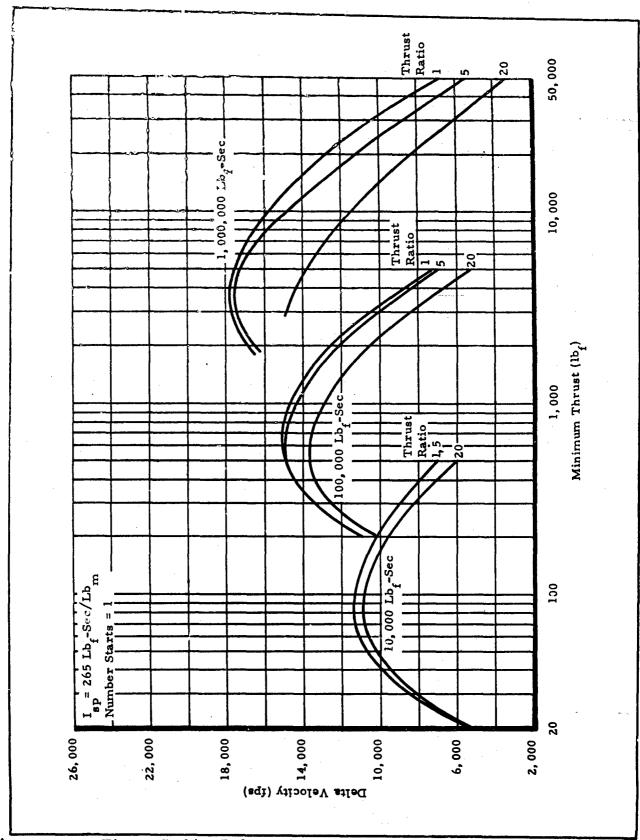


Figure B-14 - Delta Velocity versus Minimum Thrust for

I = 265 Lb_f-Sec/Lb_m and 1 Start

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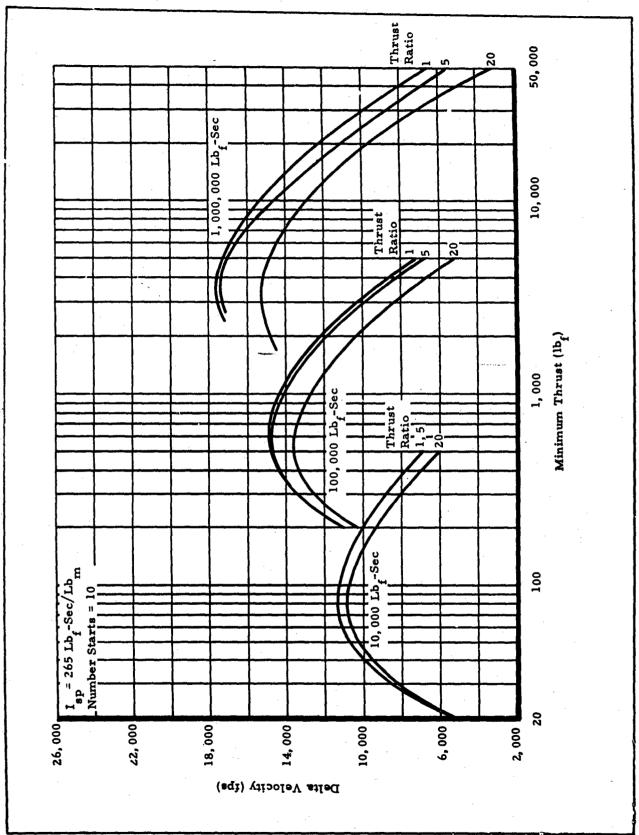


Figure B-15 - Delta Velocity versus Minimum Thrust for

I = 265 Lb_f-Sec/Lb_m and 10 Starts

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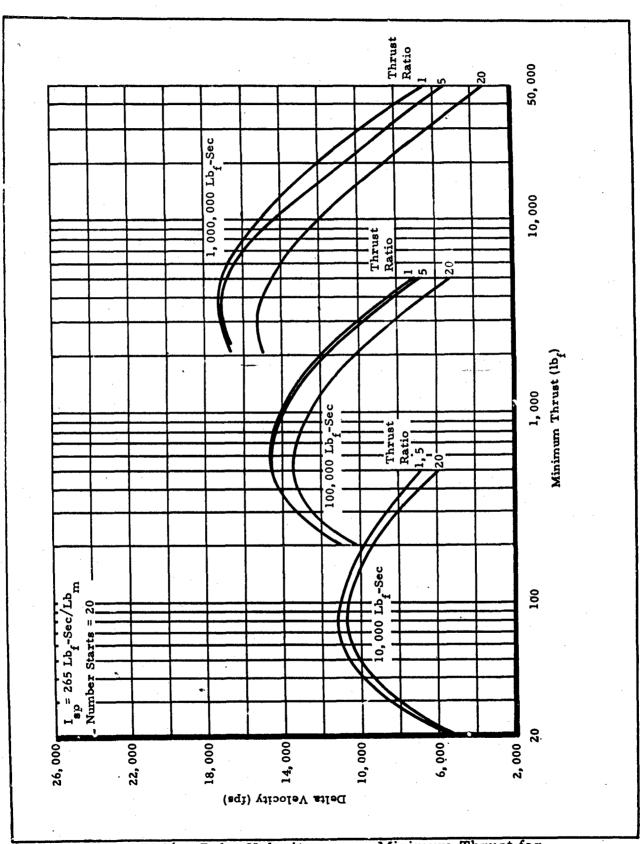


Figure B-16 - Delta Velocity versus Minimum Thrust for

I = 265 Lb_f-Sec/Lb_m and 20 Starts

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B-19

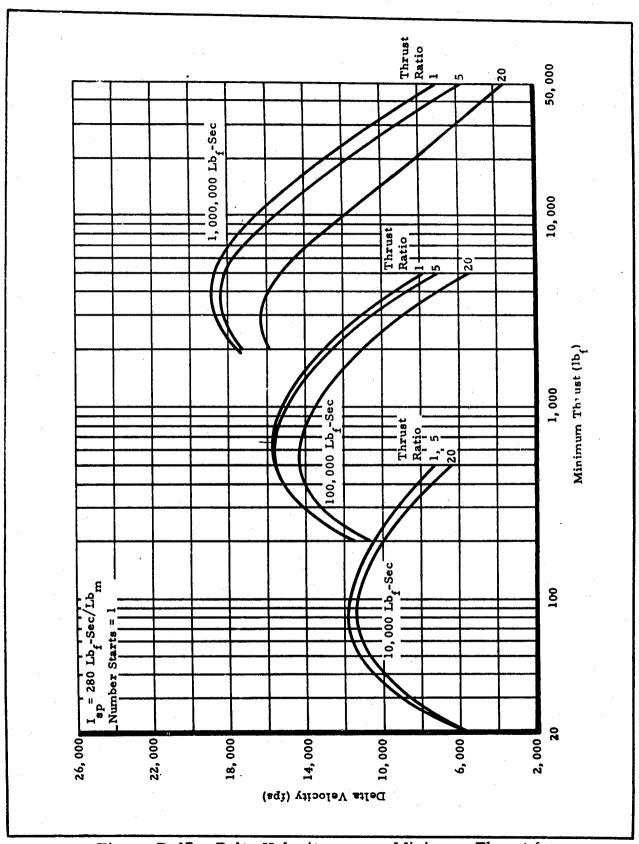


Figure B-17 - Delta Velocity versus Minimum Thrust for

I = 280 Lb - Sec/Lb and 1 Start

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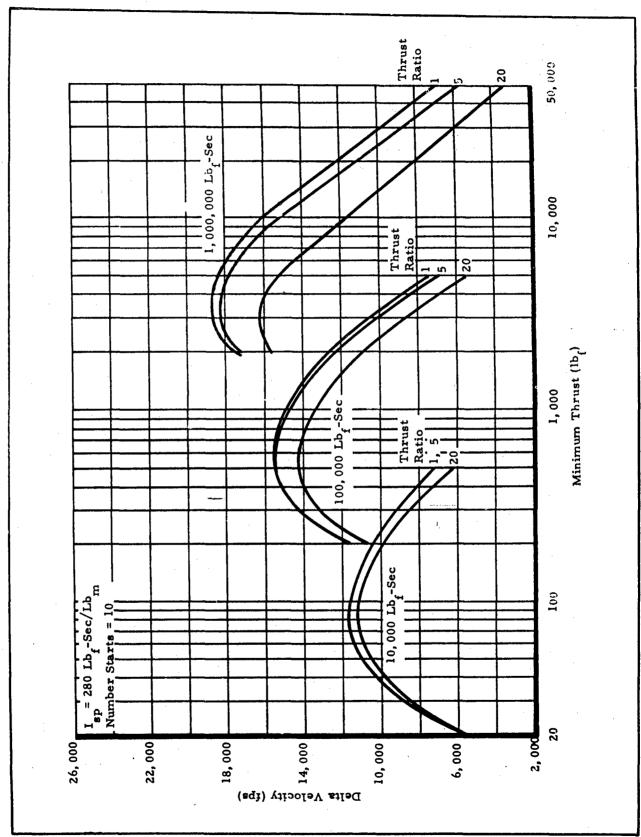


Figure B-18 - Delta Velocity versus Minimum Thrust for

I = 280 Lb_f-Sec/Lb_m and 10 Starts

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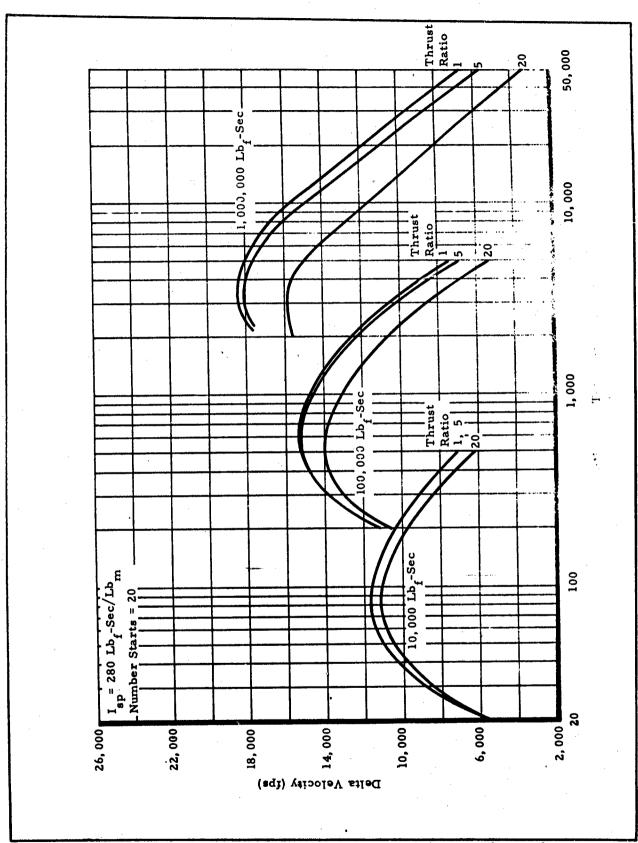


Figure B-19 - Delta Velocity versus Minimum Thrust for

I = 280 Lb_f-Sec/Lb_m and 20 Starts

CONFIDENTIAL

B-22

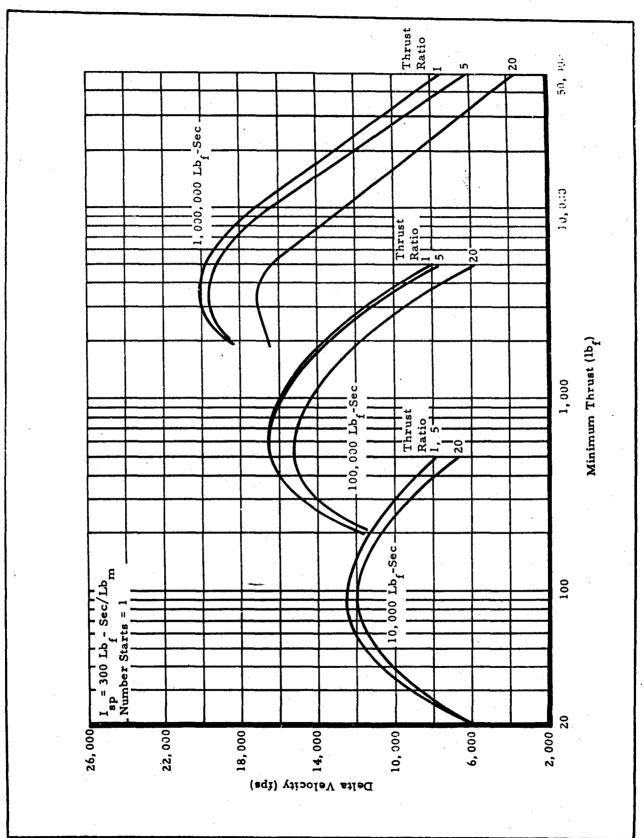


Figure B-20 - Delta Velocity versus Minimum Thrust for

I = 300 Lb_f-Sec/Lb_m and 1 Start

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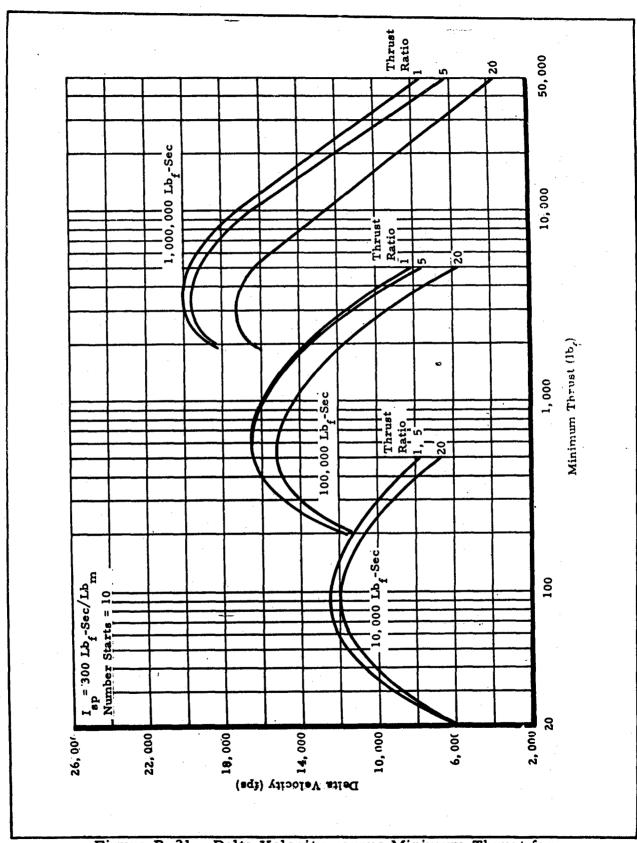


Figure B-21 - Delta Velocity versus Minimum Thrust for

I = 300 Lb_f-Sec/Lb_m and 10 Starts

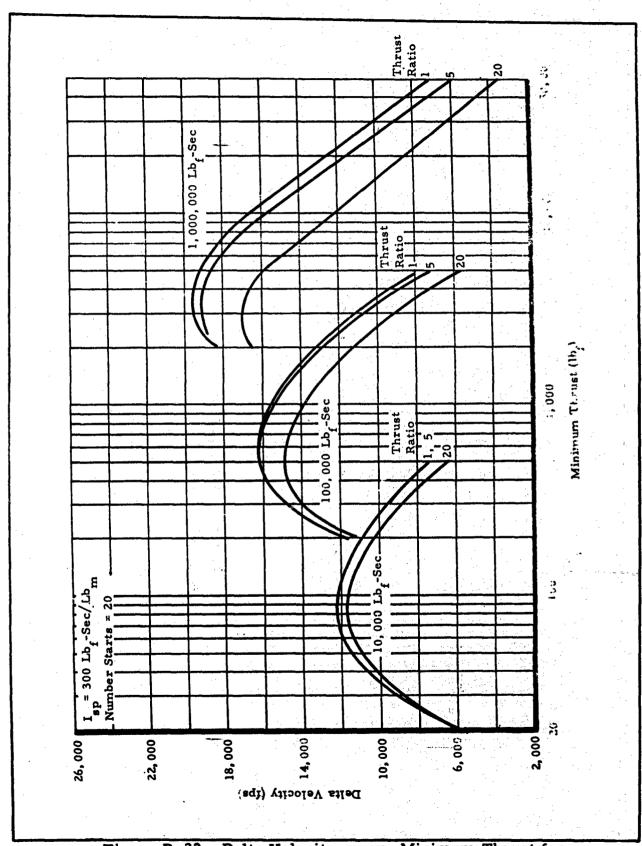


Figure B-22 - Delta Velocity versus Minimum Thrust for

I = 300 Lb_f-Sec/Lb_m and 20 Starts

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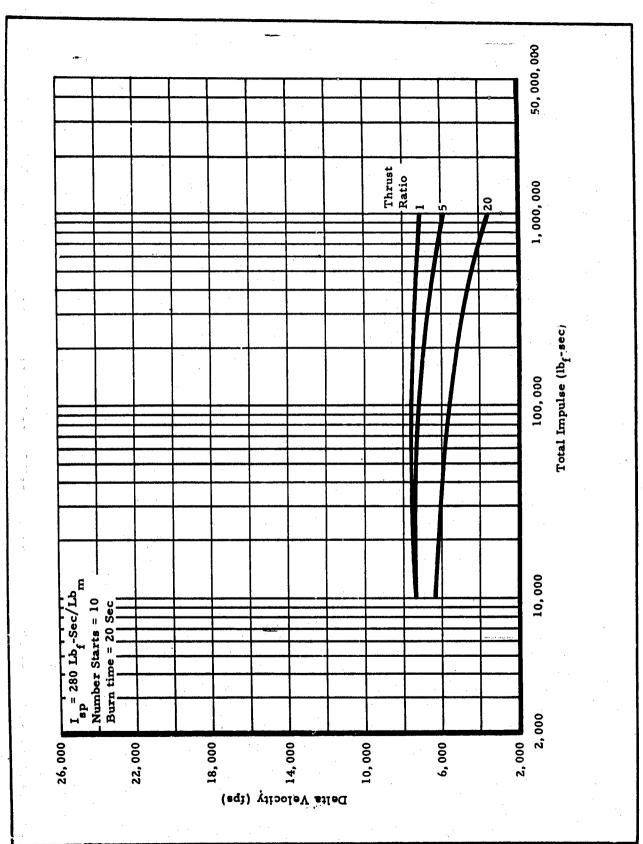


Figure B-23 - Delta Velocity versus Total Impulse for 20-Sec Burn Time

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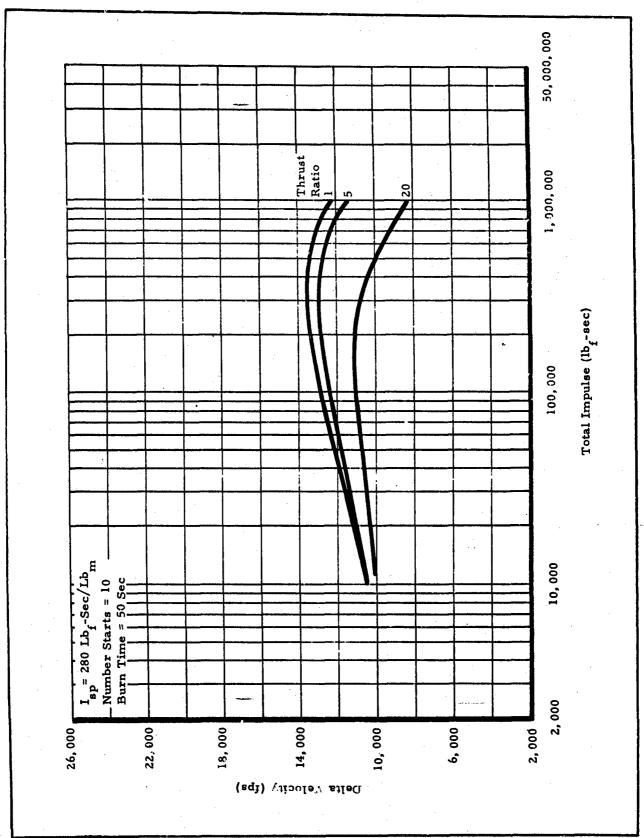


Figure B-24 - Delta Velocity versus Total Impulse for 50-Sec Burn Time

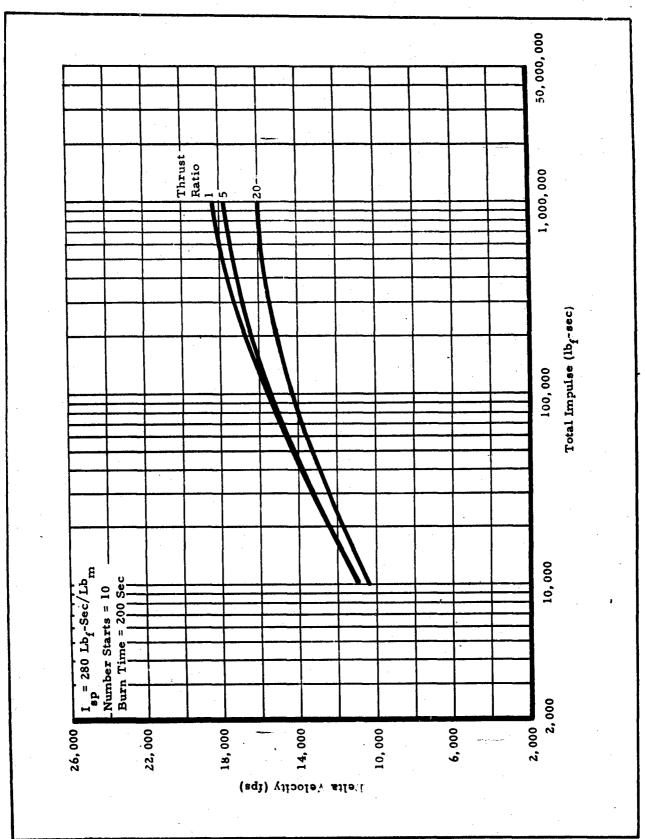


Figure B-25 - Delta Velocity versus Total Impulse for 200-Sec Burn Time

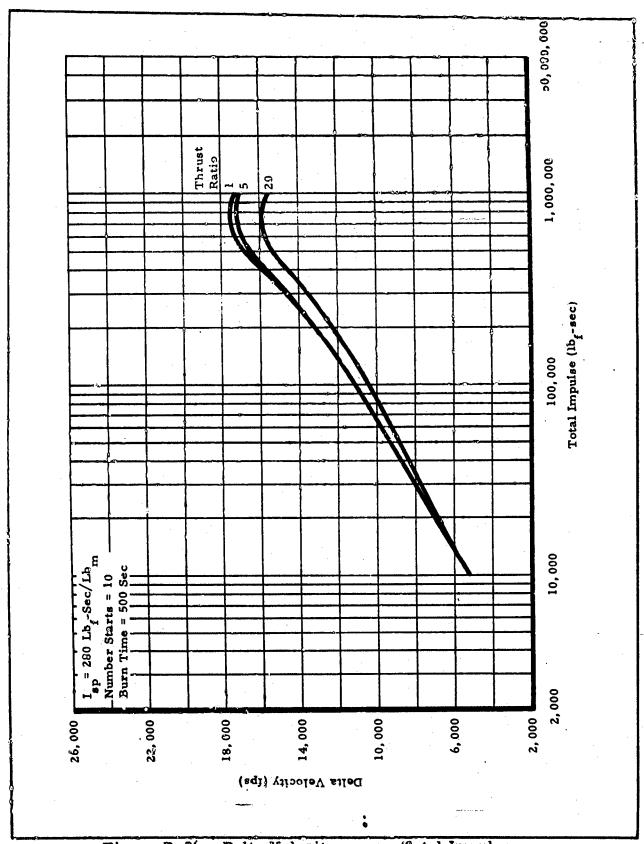


Figure B-26 - Delta Velocity versus Total Impulse for 500-Sec Burn Time

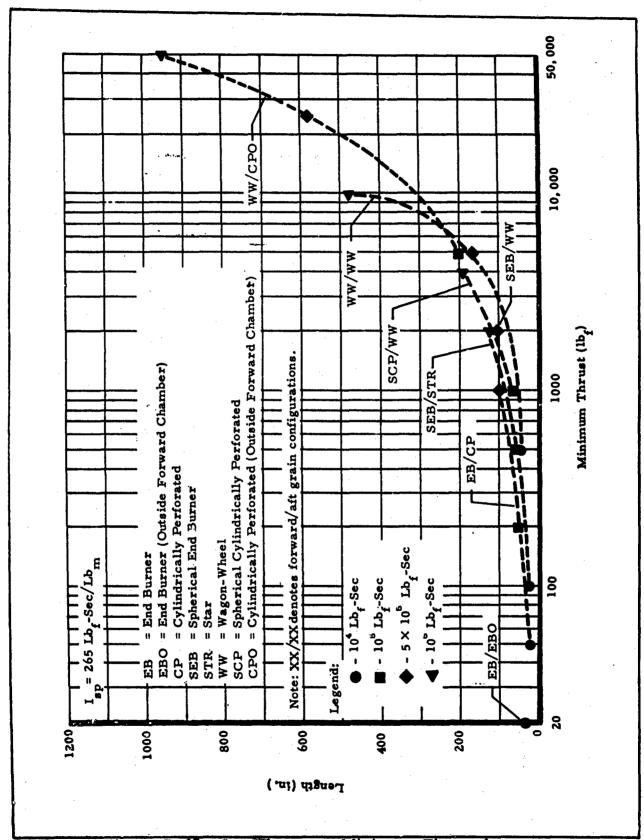


Figure B-27 - Length versus Minimum Thrust for I = 265 Lb_f-Sec/Lb_m

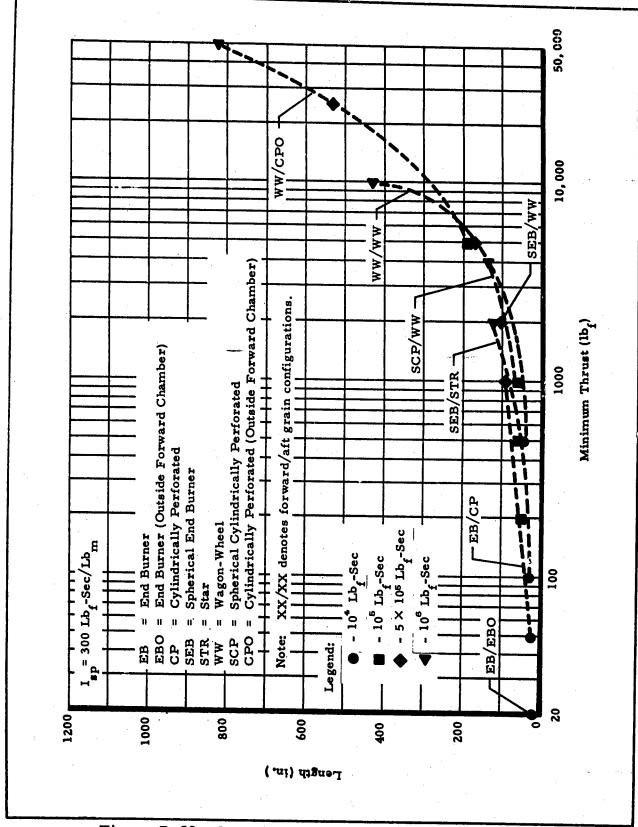


Figure B-28 - Length versus Minimum Thrust for

I = 300 Lb_f-Sec/Lb_m

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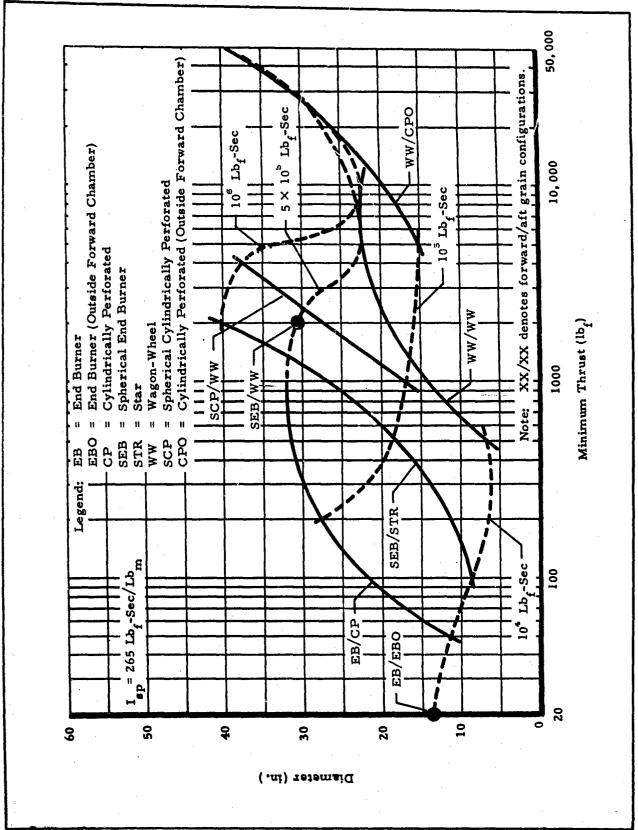


Figure B-29 - Diameter versus Minimum Thurst for I = 265 Lb_f-Sec/Lb_m
CONFIDENTIAL

B-32

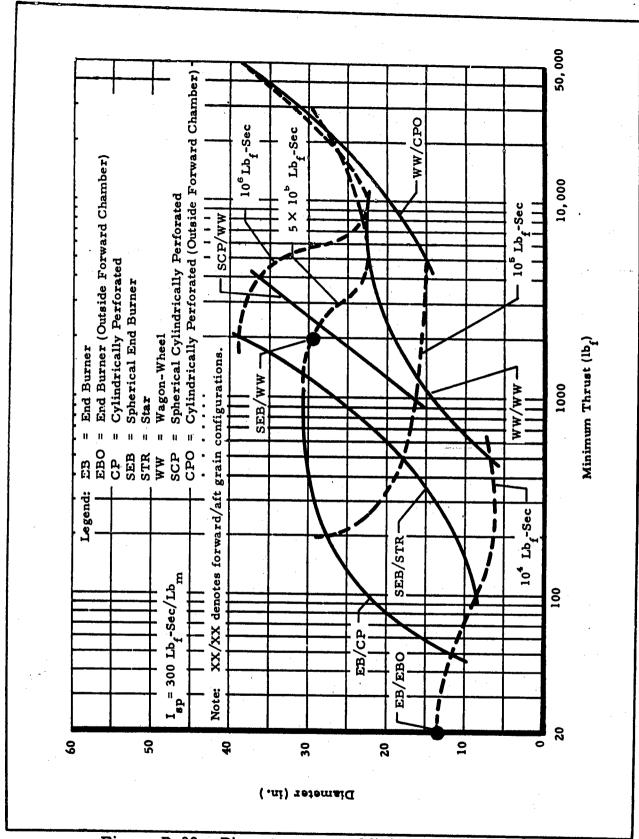


Figure B-30 - Diameter versus Minimum Thrust

B-33

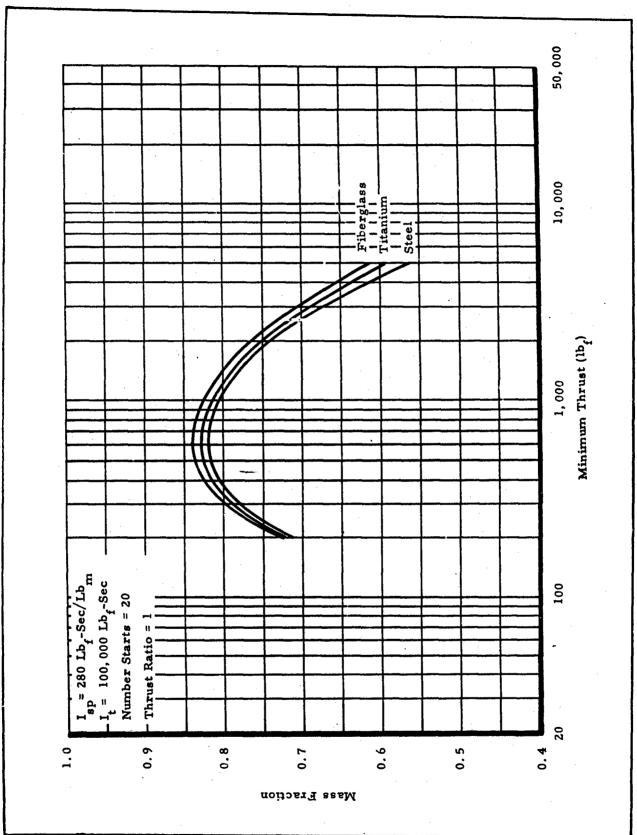


Figure B-31 - Mass Fraction versus Minimum

Thrust at Thrust Ratio of 1

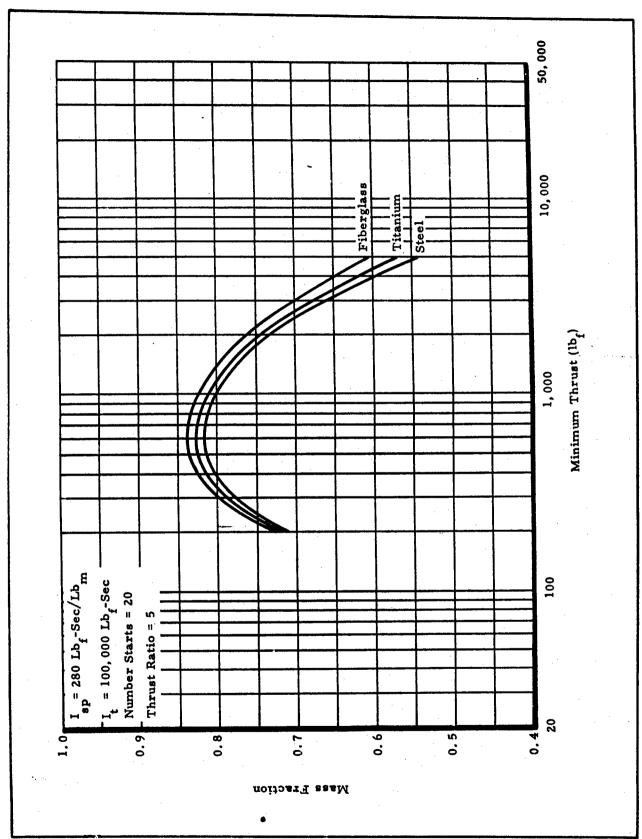


Figure B-32 - Mass Fraction versus Minimum
Thrust at Thrust Ratio of 5

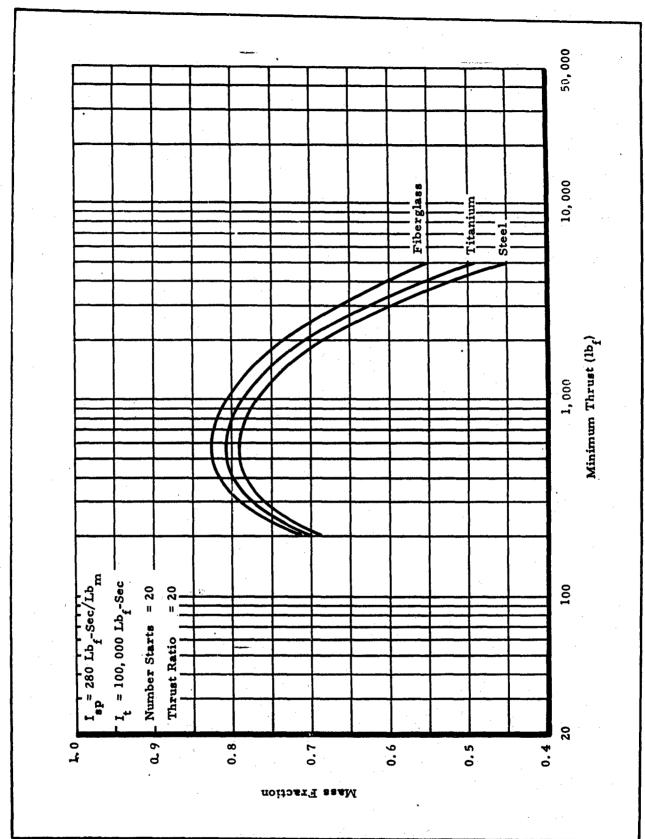


Figure B-33 - Mass Fraction versus Minimum
Thrust at Thrust Ratio of 20

B-36

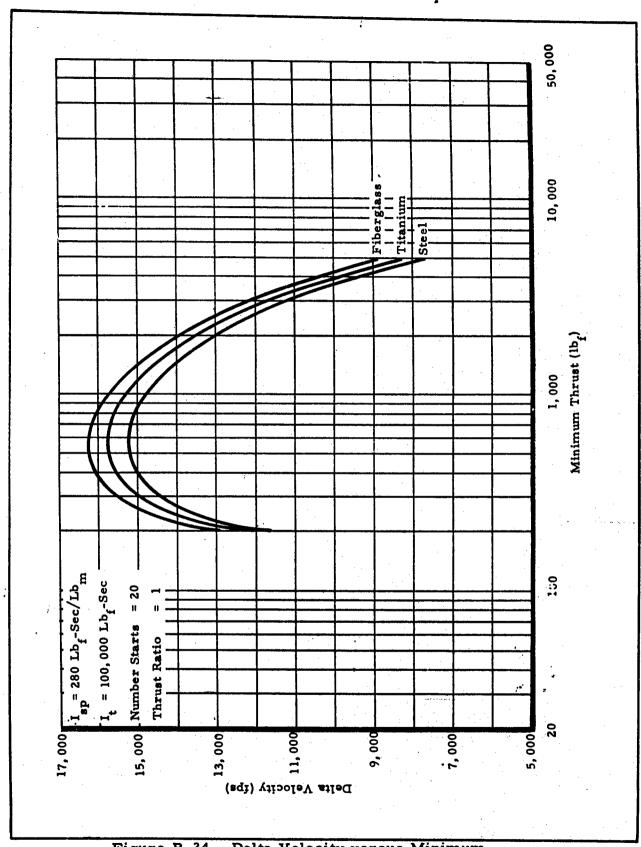


Figure B-34 - Delta Velocity versus Minimum Thrust at Thrust Ratio of 1

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B-37

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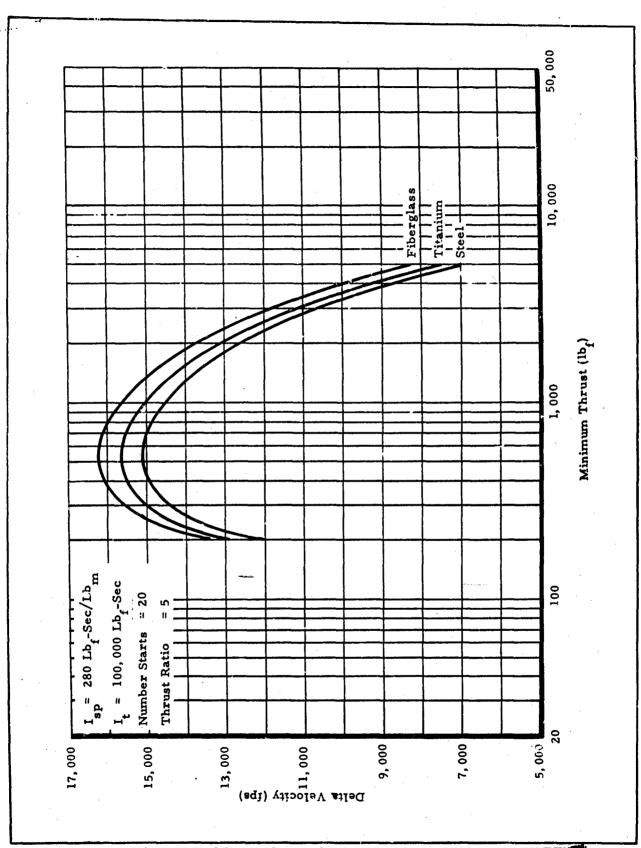


Figure B-35 - Delta Velocity versus Minimum Thrust at Thrust Ratio of 5

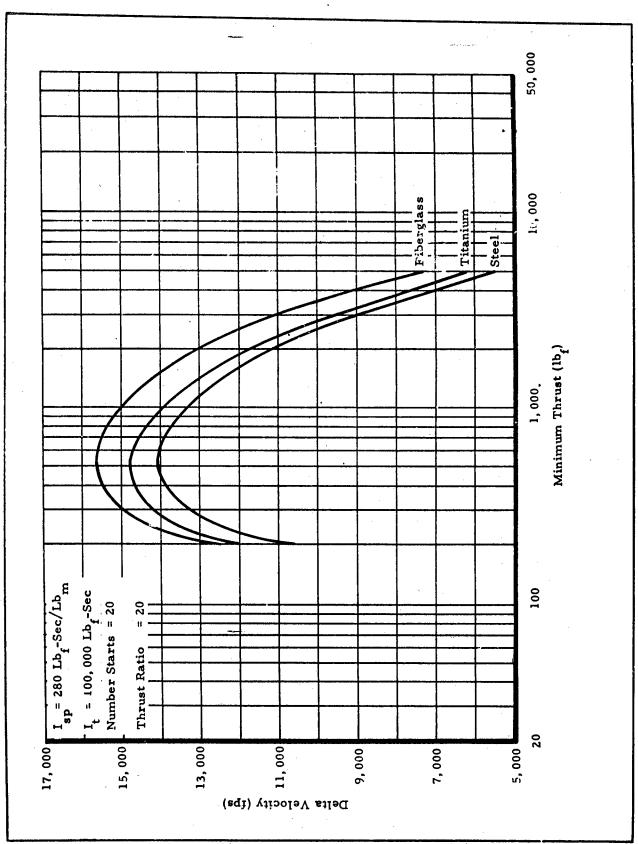


Figure B-36 - Delta Velocity versus Minimum
Thrust at Thrust Ratio of 20

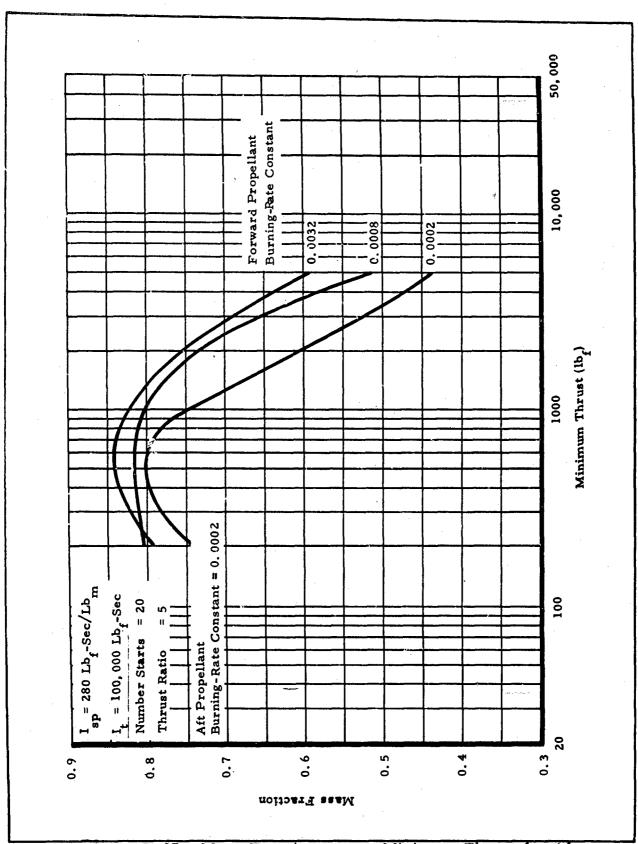


Figure B-37 - Mass Fraction versus Minimum Thrust for Aft Propellant Burning-Rate Constant of 0.0002

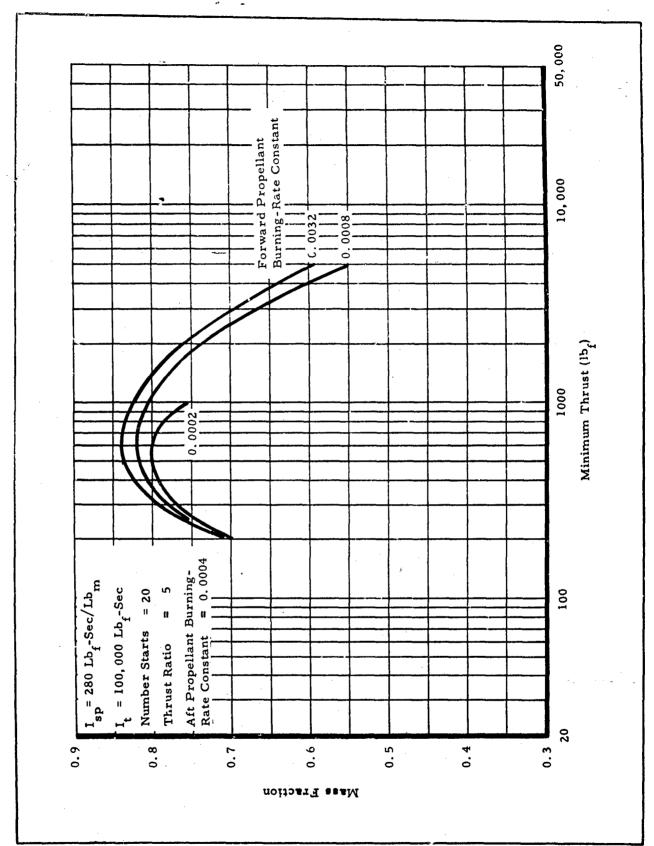


Figure B-38 - Mass Fraction versus Minimum Thrust for Aft Propellant Burning-Rate Constant of 0.0004

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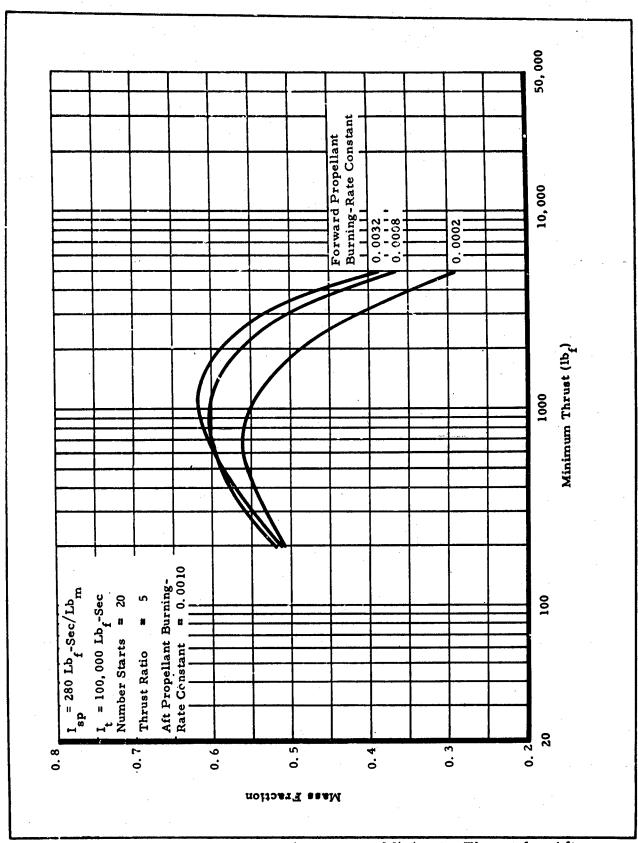


Figure B-39 - Mass Fraction versus Minimum Thrust for Aft Propellant Burning-Rate Constant of 0.0010

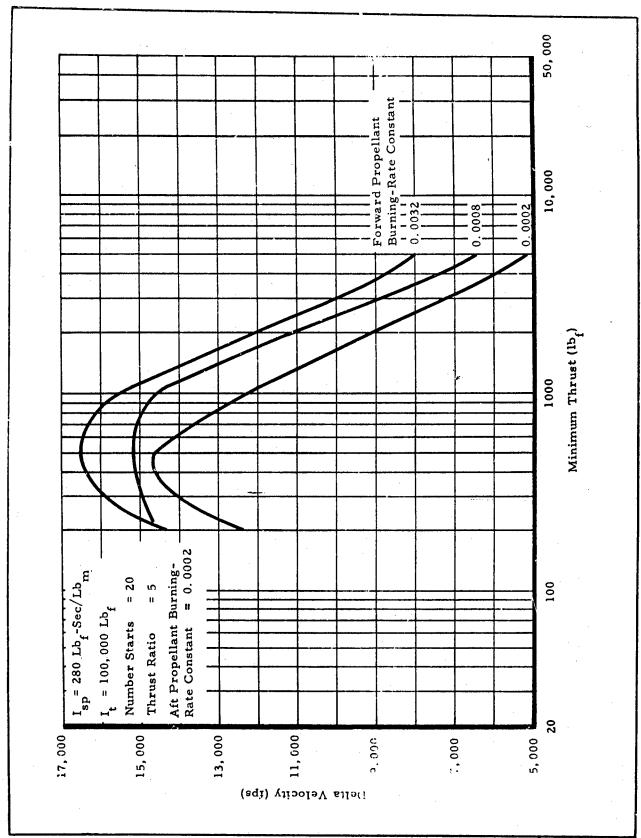


Figure B-40 - Delta Velocity versus Minimum Thrust for Aft Propellant Burning-Rate Constant of 0.0002

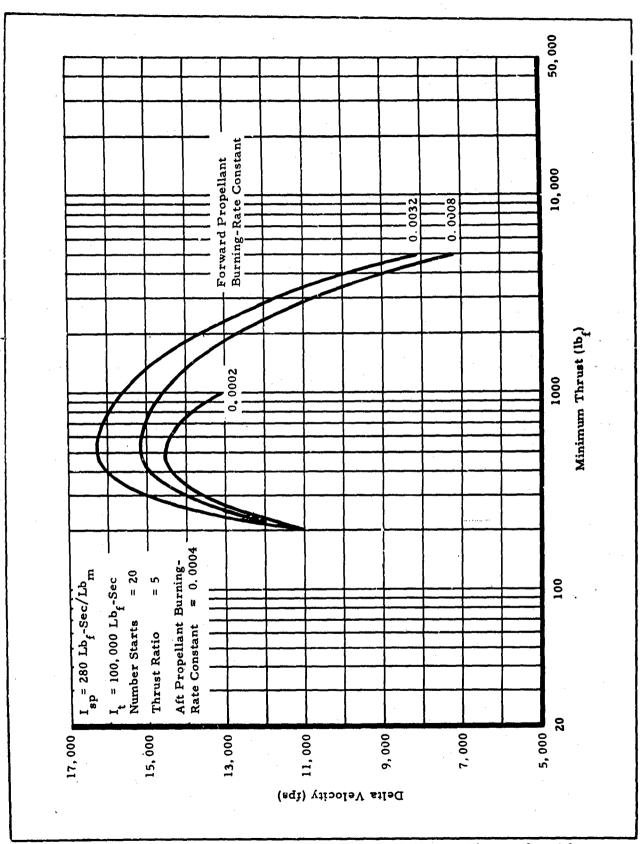


Figure B-41 - Delta Velocity versus Minimum Thrust for Aft Propellant Burning-Rate Constant of 0.0004

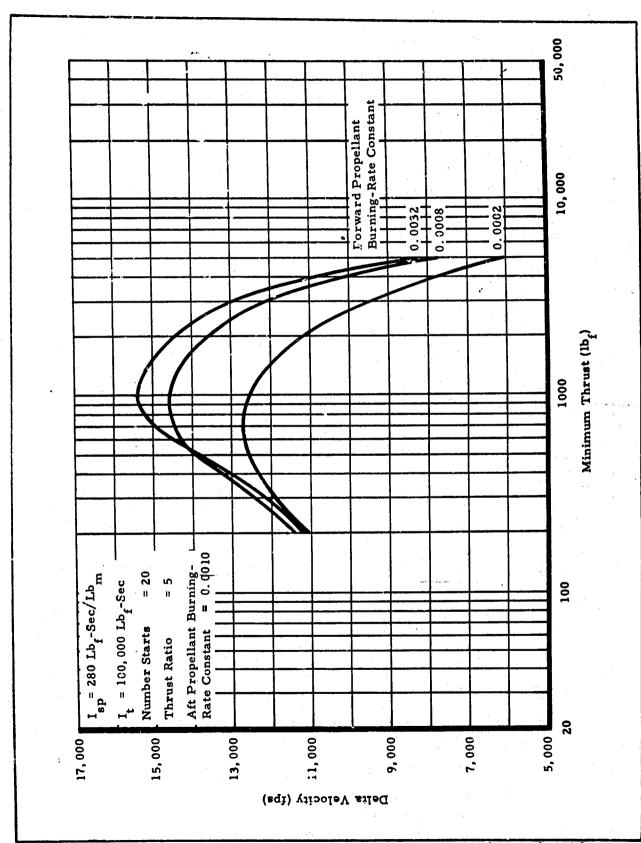


Figure B-42 - Delta Velocity versus, Minimum Thrust for Aft Propellant Burning-Rate Constant of 0.0010

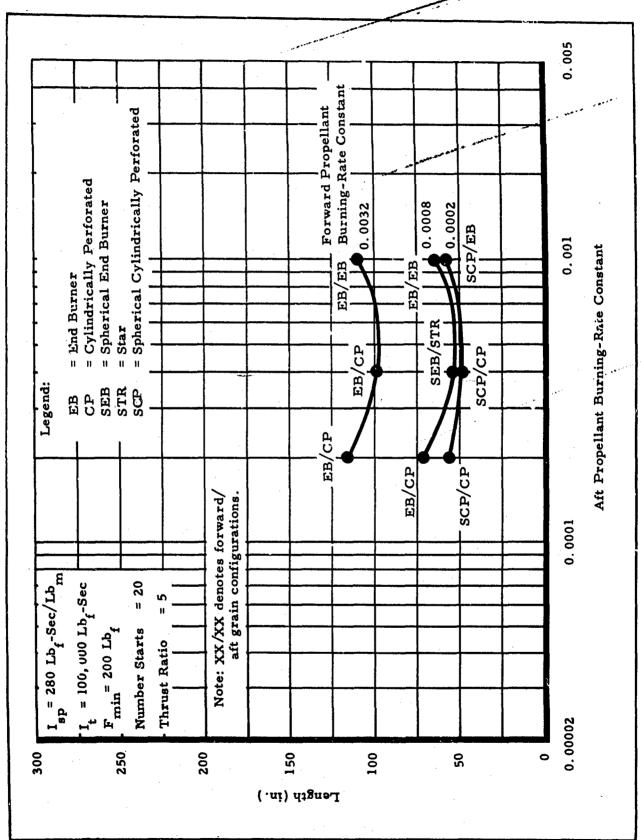


Figure B-43 - Length versus Aft Propellant Burning-Rate
Constant for F_{min} = 200 Lb_f

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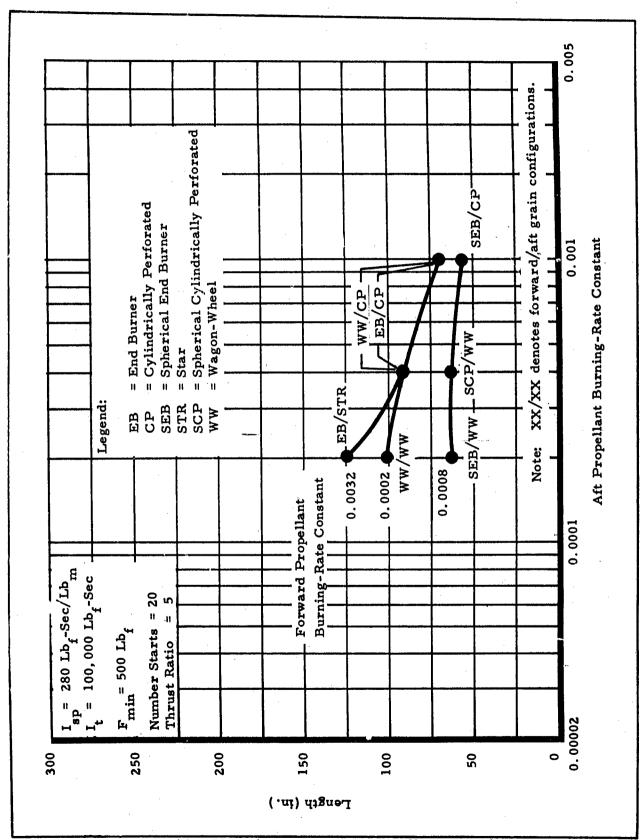


Figure B-44 - Length versus Aft Propellant Burning-Rate Constant for F_{min} = 500 Lb_f
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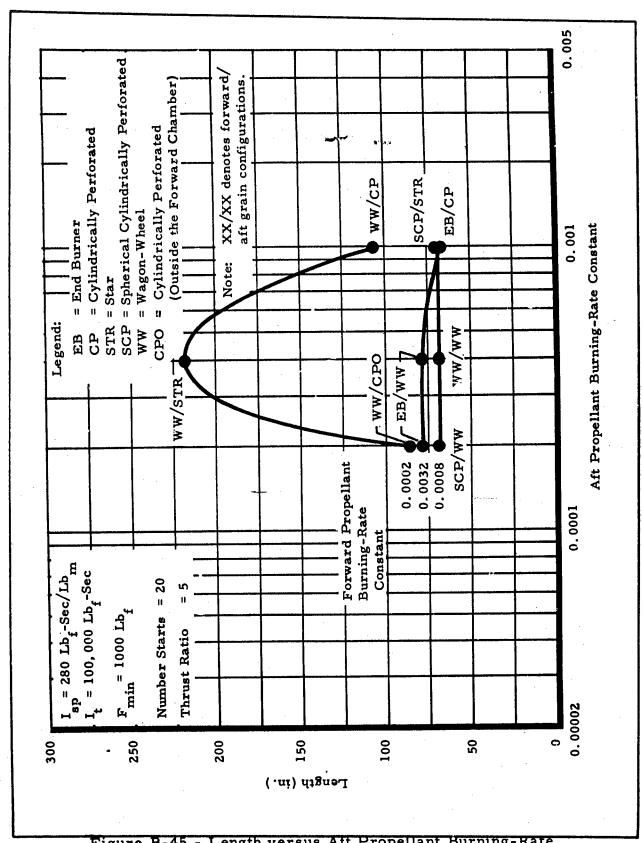


Figure B-45 - Length versus Aft Propellant Burning-Rate

Constant for F min = 1000 Lb_f

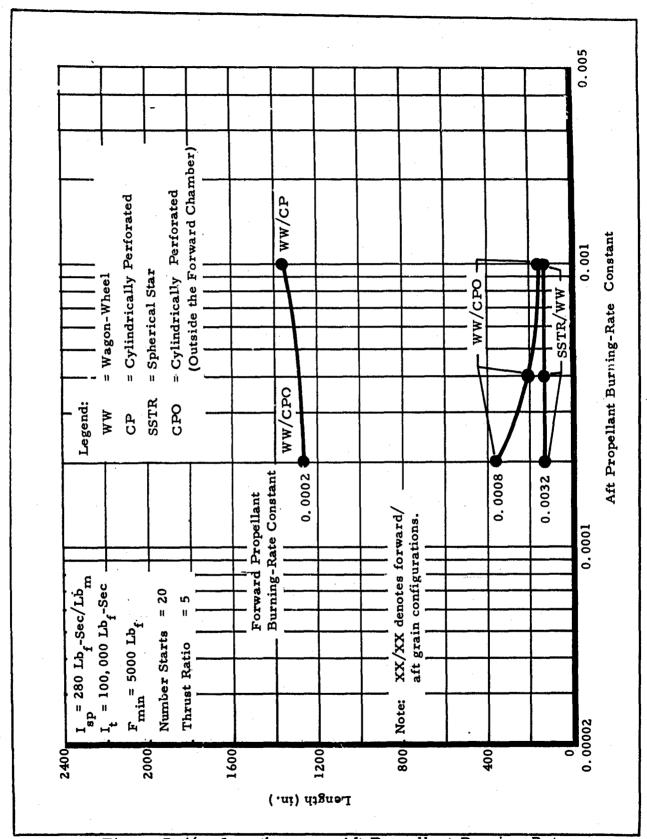


Figure B-46 - Length versus Aft Propellant Burning-Rate
Constant for F = 5000 Lb
f

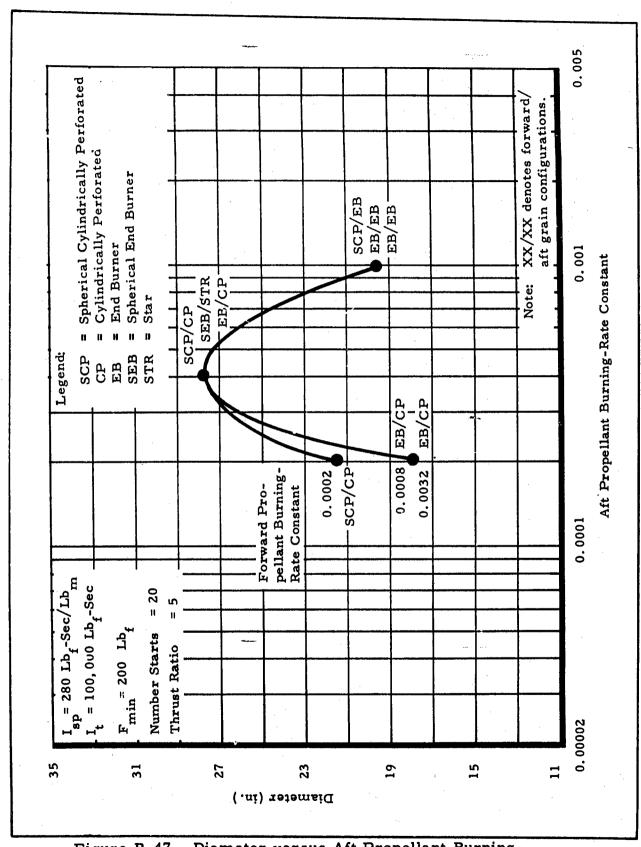


Figure B-47 - Diameter versus Aft Propellant Burning-Diameter versus I = 200 Lb_f

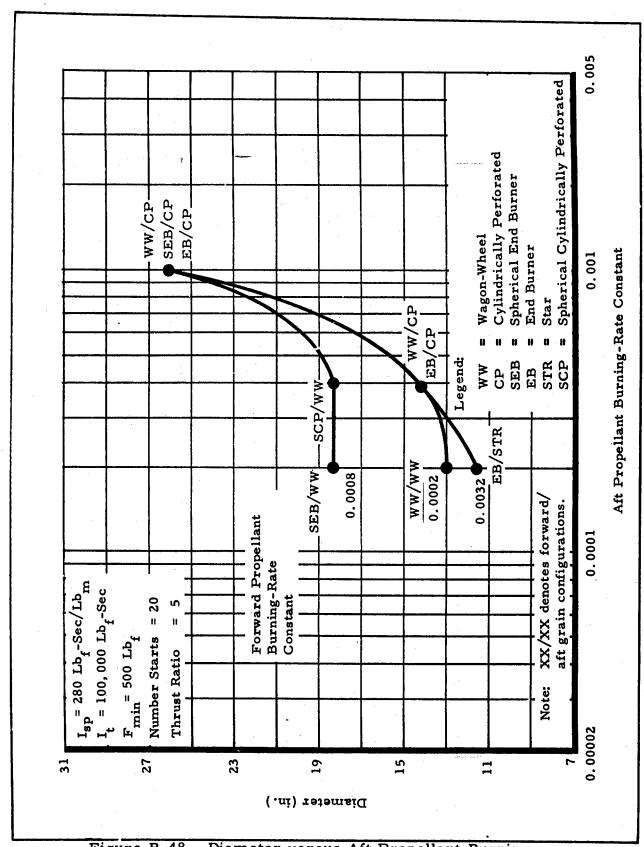


Figure B-48 - Diameter versus Aft Propellant Burning-Rate Constant for F = 500 Lb_f

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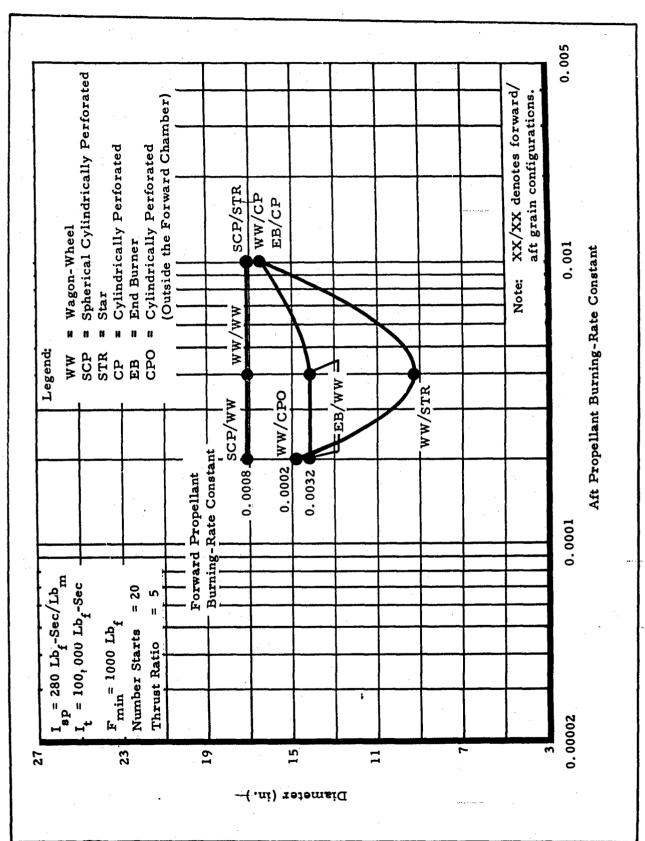


Figure B-49 - Diameter versus Aft Propellant Burning-Rate Constant for F = 1000 Lb_f

B-52

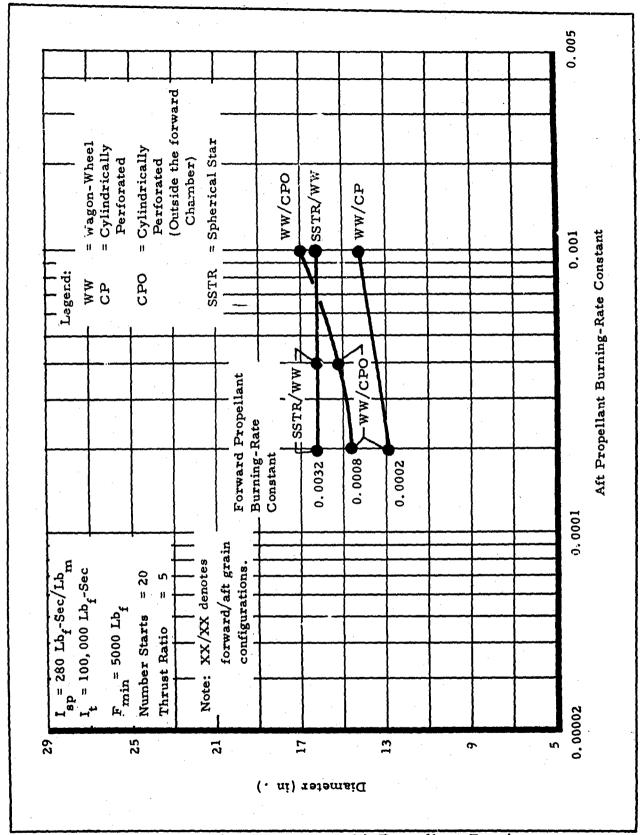


Figure B-50 - Diameter versus Aft Propellant Burning-Rate Constant for F = 5000 Lb

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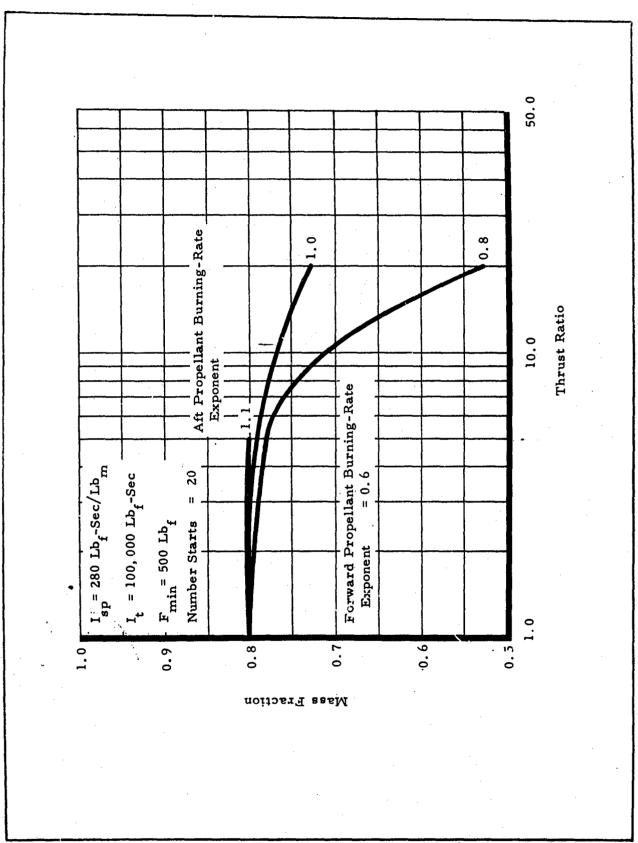


Figure B-51 - Mass Fraction versus Thrust Ratio for Forward
B-54

Propellant Burning-Rate Exponent of 0.6

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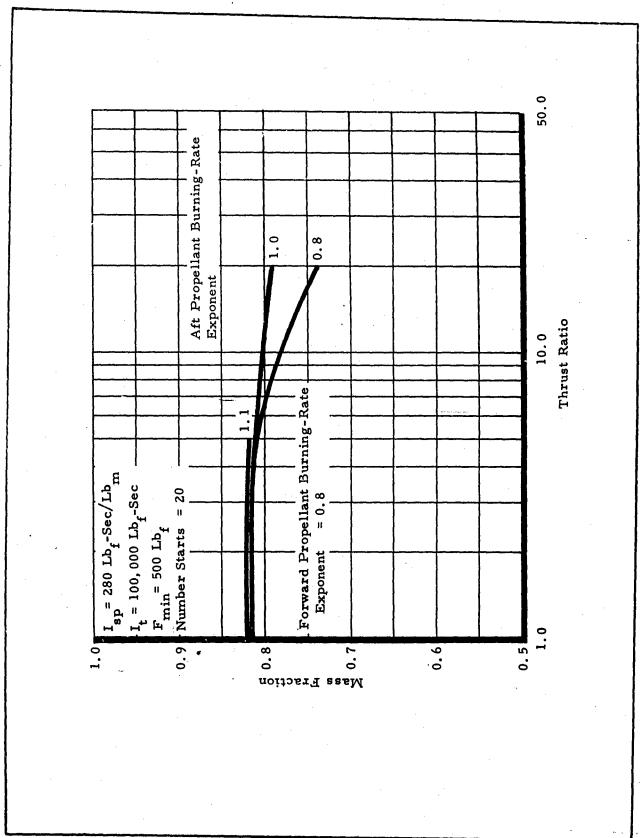


Figure B-52 - Mass Fraction versus Thrust Ratio for Forward Propellant Burning-Rate Exponent of 0.8

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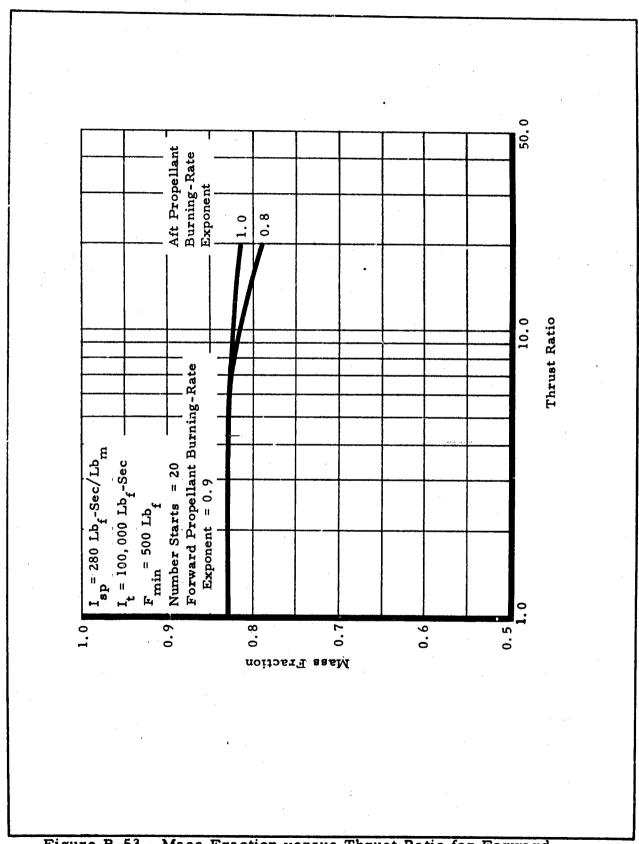


Figure B-53 - Mass Fraction versus Thrust Ratio for Forward
B-56 Propellant Burning-Rate Exponent of 0. 9

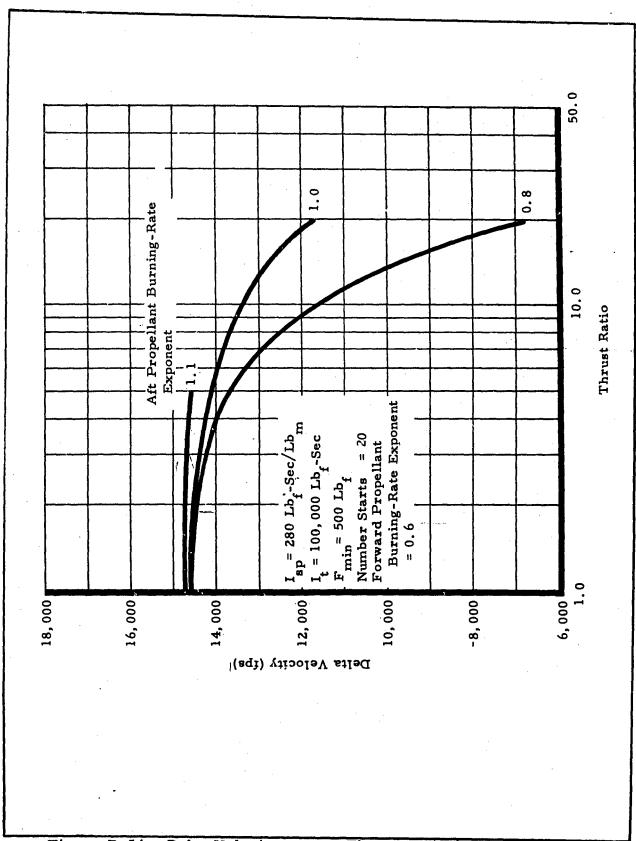


Figure B-54 - Delta Velocity versus Thrust Ratio for Forward Propellant Burning-Rate Exponent of 0.6

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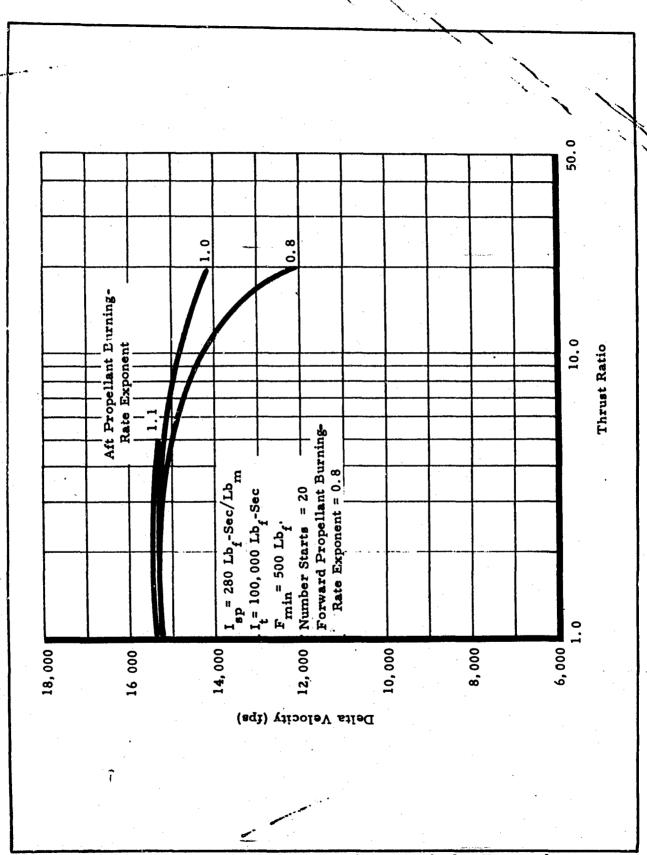


Figure B-55 - Delta Velocity versus Thrust Ratio for Forward
Propellant Burning-Rate Exponent of 0.8

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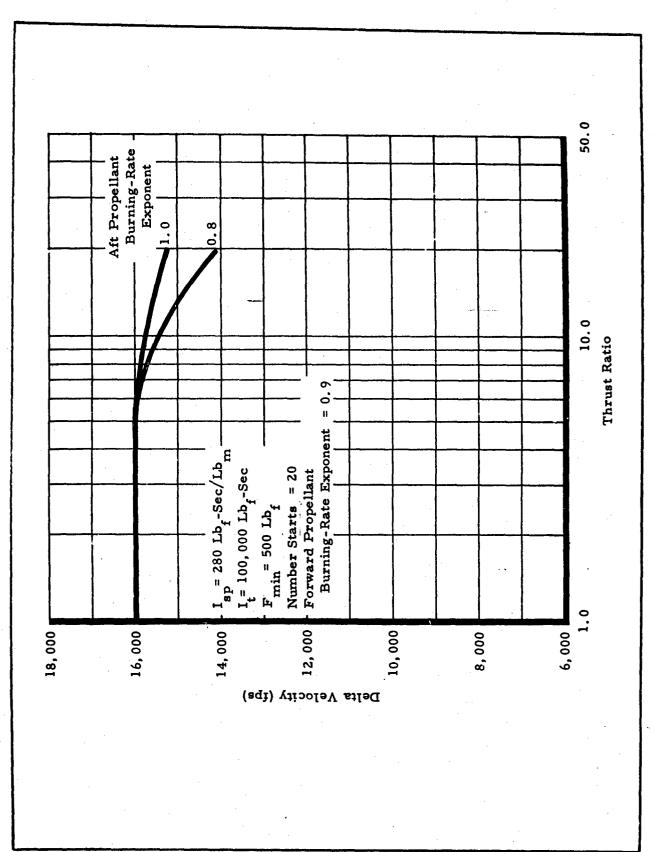


Figure B-56 - Delta Velocity versus Thrust Ratio for Forward Propellant Burning-Rate Exponent of 0.9

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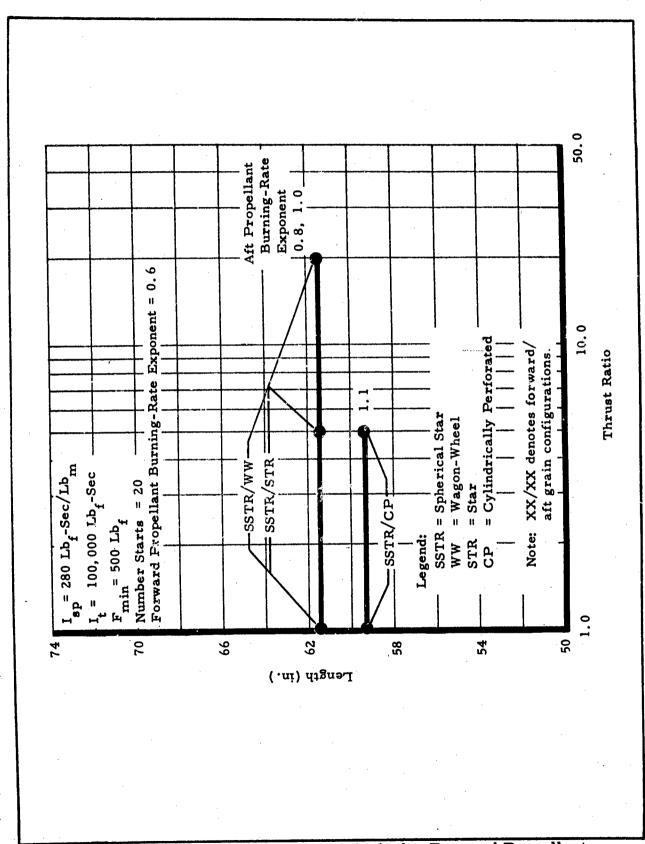


Figure B-57 - Length versus Thrust Ratio for Forward Propellant
Burning-Rate Exponent of 0. 6

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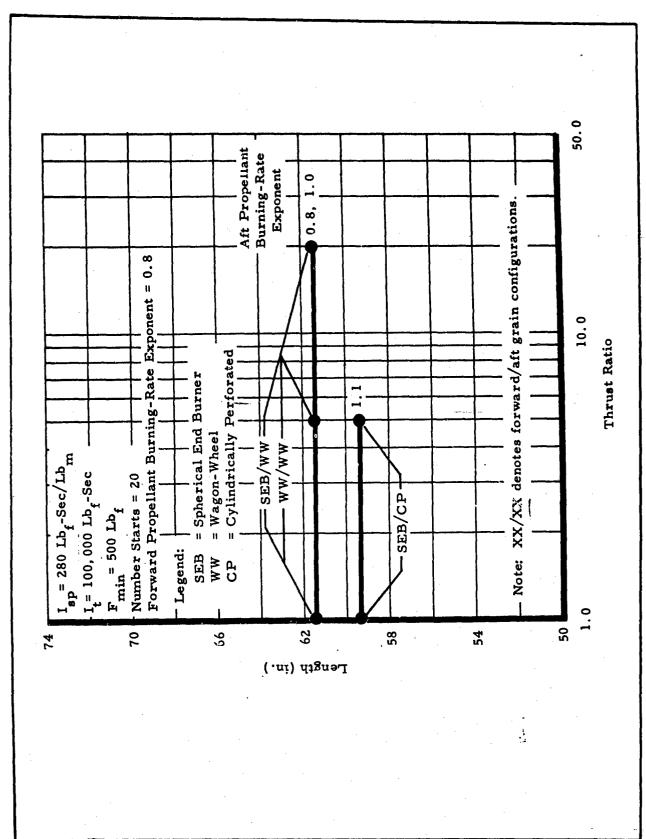


Figure B-58 - Length versus Thrust Ratio for Forward Propellant Burning-Rate Exponent of 0.8

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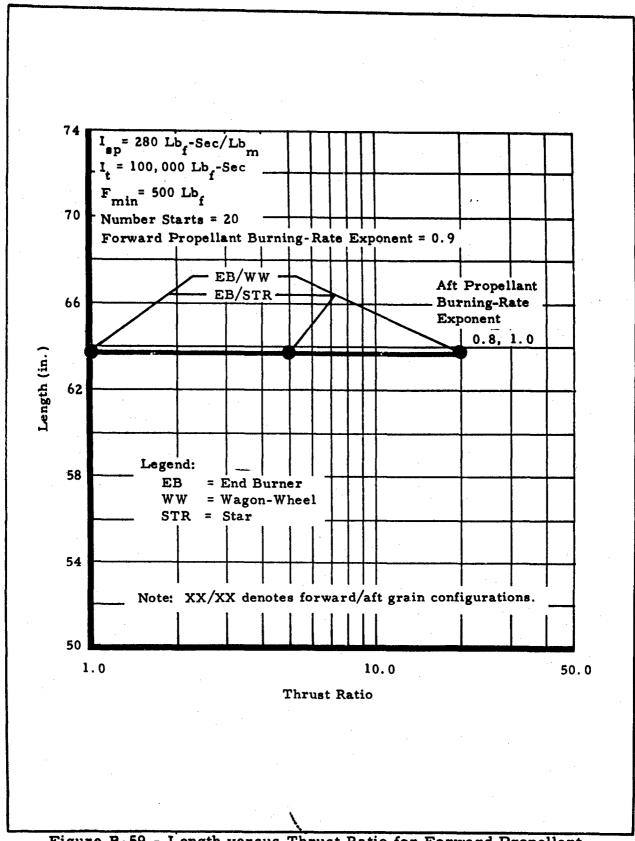


Figure B-59 - Length versus Thrust Ratio for Forward Propellant
B-62 Burning-Rate Exponent of 0.9

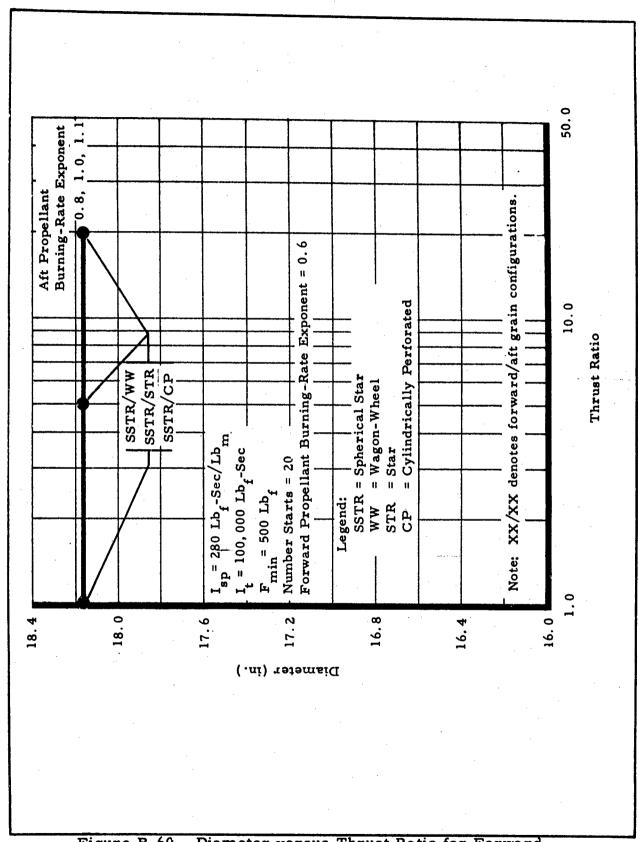


Figure B-60 - Diameter versus Thrust Ratio for Forward Propellant Burning-Rate Exponent of 0.6

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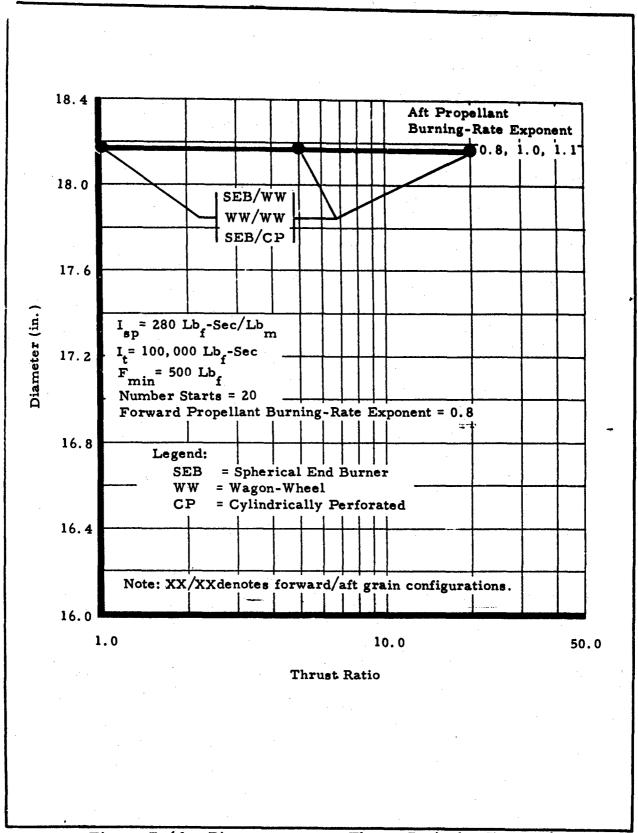
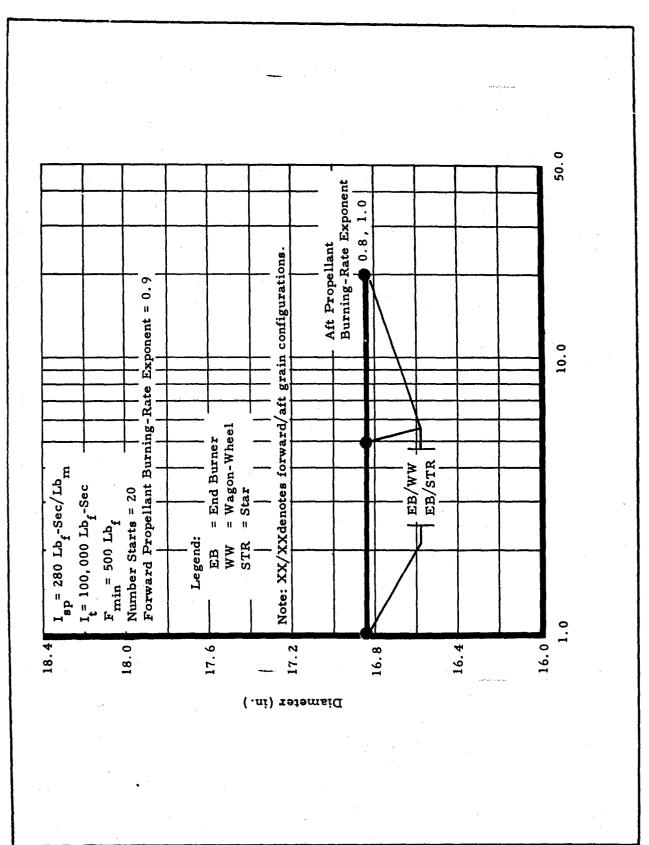


Figure B-61 - Diameter versus Thrust Ratio for Forward Propellant Burning-Rate Exponent of 0.8



'igure B-62 - Diameter versus Thrust Ratio for Forward Propellant Burning-Rate Exponent of 0.9

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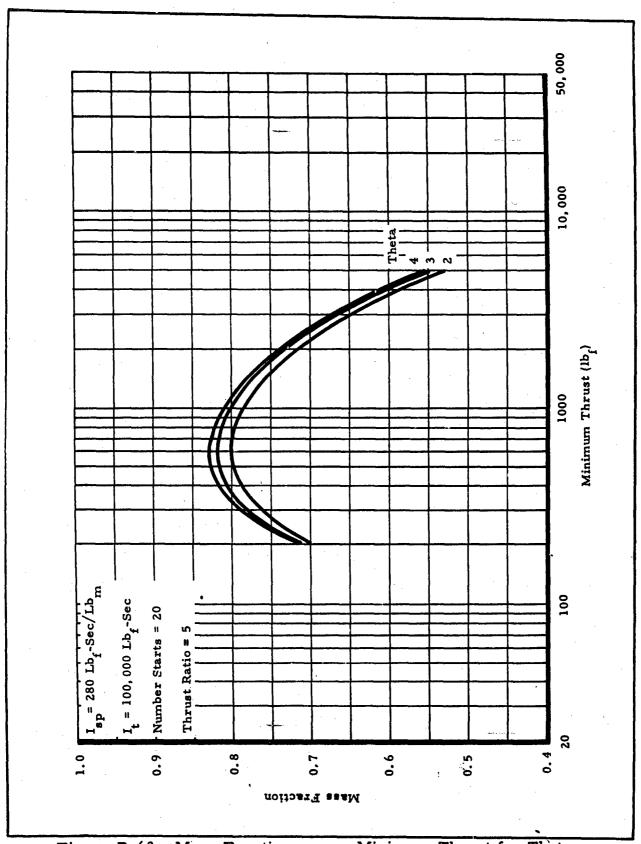


Figure B-63 - Mass Fraction versus Minimum Thrust for Theta Values of 2, 3, and 4

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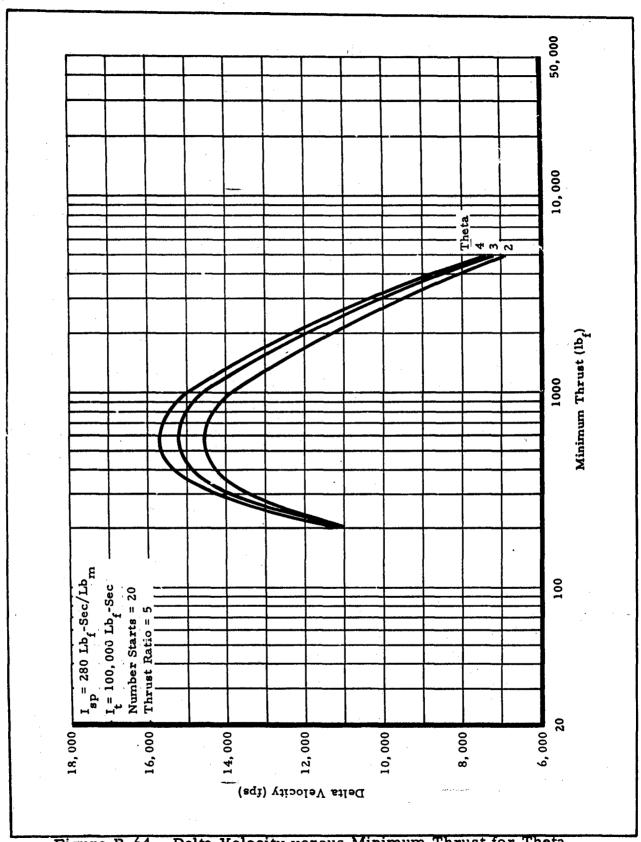


Figure B-64 - Delta Velocity versus Minimum Thrust for Theta

Values of 2, 3, and 4

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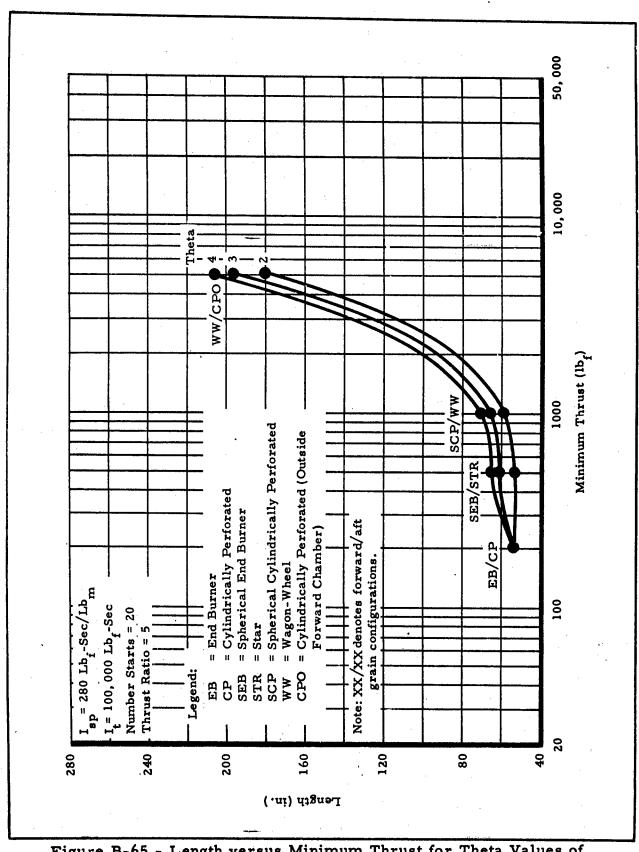


Figure B-65 - Length versus Minimum Thrust for Theta Values of 2, 3, and 4

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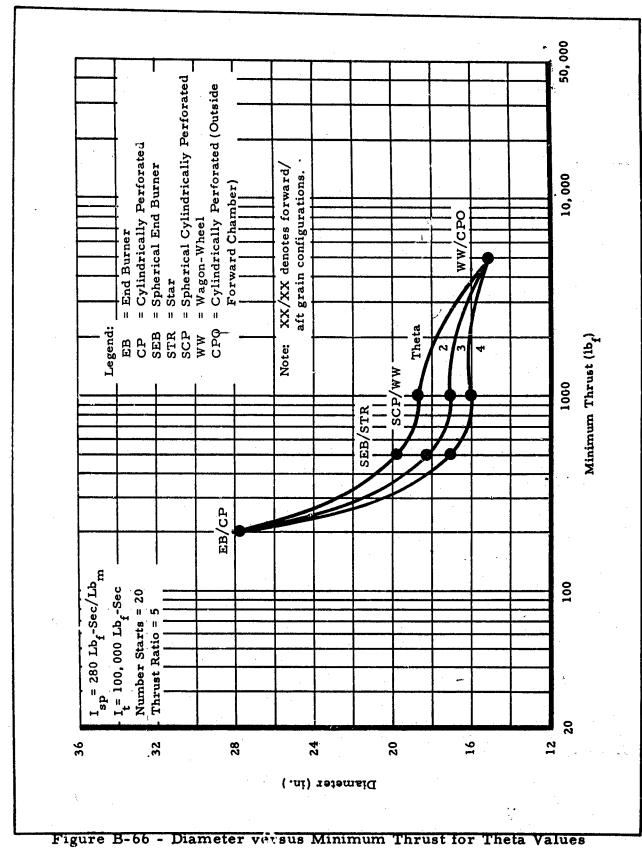


Figure B-66 - Diameter versus Minimum Thrust for Theta

of 2, 3, and 4

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